

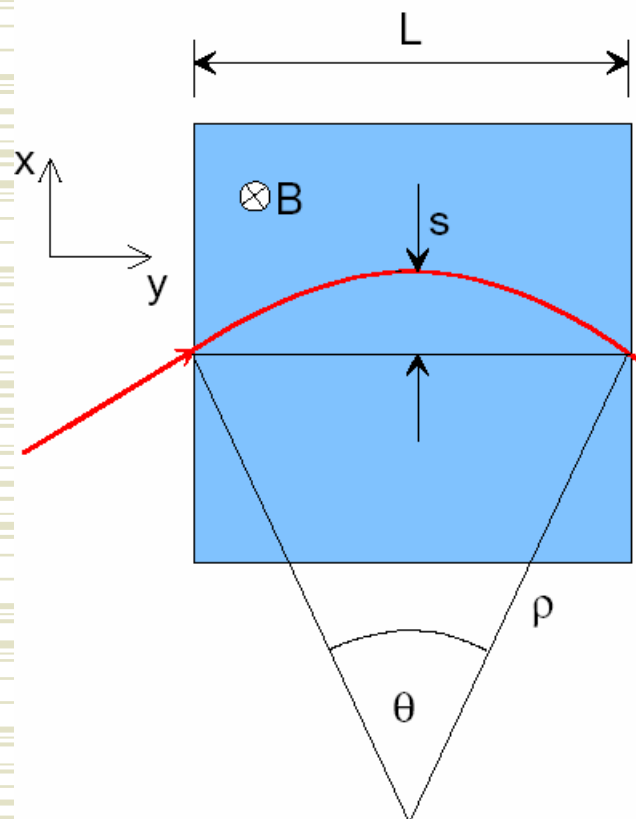
# Apparati Sperimentali

Lezione 4  
Tracciatura  
Scintillatori e fibre

# Misura delle proprietà delle particelle

- ◆ **Carica**
  - Segno:
    - Tracciatura in campo magnetico
  - Quantità
    - Altezza d'impulso (ionizzazione o luce)
- ◆ **Spin e vita media**
  - Tracciatura (molto precisa)
- ◆ **Massa**
  - dalla misura dell'impulso con la tracciatura in campo magnetico  
+
  - energia con i calorimetri
  - Velocità: TOF, Cherenkov,  $dE/dx$

# Misura dell'impulso



$$p_T = qB\rho$$

$$p_T \text{ (GeV/c)} = 0.3B\rho \quad (\text{T} \cdot \text{m})$$

$$\frac{L}{2\rho} = \sin \theta/2 \approx \theta/2 \rightarrow \theta \approx \frac{0.3L \cdot B}{p_T}$$

$$\Delta p_T = p_T \sin \theta \approx 0.3L \cdot B$$

$$s = \rho(1 - \cos \theta/2) \approx \rho \frac{\theta^2}{8} \approx \frac{0.3}{8} \frac{L^2 B}{p_T}$$

$$s = x_2 - \frac{x_1 + x_3}{2}$$



$$\frac{\sigma(p_T)}{p_T} \Big|^{meas.} = \frac{\sigma(s)}{s} = \frac{\sqrt{\frac{3}{2}}\sigma(x)}{s} = \frac{\sqrt{\frac{3}{2}}\sigma(x) \cdot 8p_T}{0.3 \cdot BL^2}$$

# Misura dell'impulso (2)

Per N punti equidistanti:

(R.L. Gluckstern, NIM 24 (1963) 381)

$$\frac{\sigma(p_T)}{p_T} \Big|^{meas.} = \frac{\sigma(x) \cdot p_T}{0.3 \cdot BL^2} \sqrt{720/(N+4)} \quad (\text{for } N \geq \approx 10)$$

ex:  $p_T=1$  GeV/c,  $L=1$ m,  $B=1$ T,  $\sigma(x)=200\mu\text{m}$ ,  $N=10$

$$\frac{\sigma(p_T)}{p_T} \Big|^{meas.} \approx 0.5\% \quad (s \approx 3.75 \text{ cm})$$

A LEP: 0.1%  $p_T$

A LHC: 0.01%  $p_T$  (ad 1 TeV)

# Effetto dello scattering multiplo

$$\Delta p^{MS} = p \sin \theta_0 \approx p \cdot 0.0136 \frac{1}{p} \sqrt{\frac{L}{X_0}}$$

$$\left. \frac{\sigma(p)}{p_T} \right|^{MS} = \frac{\Delta p^{MS}}{p_T} = \frac{0.0136 \sqrt{\frac{L}{X_0}}}{0.3BL} = 0.045 \frac{1}{B\sqrt{LX_0}}$$

Indipendente da  $p$ !

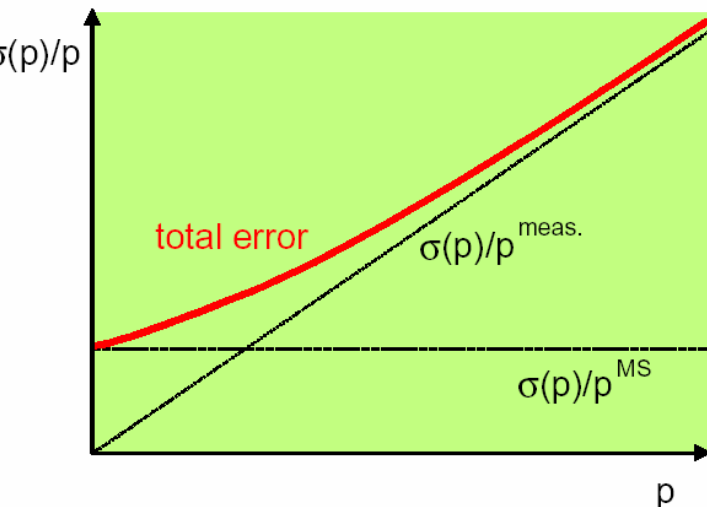
$X_0$

110 m per Ar (gas)

8.9 cm per Al

0.56 cm per Pb

Es: Ar ( $X_0=110$  m),  $L=1$  m,  $B=1$  T



$$\left. \frac{\sigma(p)}{p_T} \right|^{MS} \approx 0.5\%$$

# Misura delle coordinate

- Segnali di ionizzazione
  - Contatori Geiger-Müller
  - MWPC (Multi-Wire Proportional Chambers)
  - TPC (Time Projection Chamber)
  - Rivelatori al silicio
- Luce di scintillazione
  - Fibre scintillanti

# Rivelatori a gas

$$n_{total} = \frac{\Delta E}{W_i} = \frac{dE}{dx} \frac{\Delta x}{W_i}$$

$$n_{total} \approx 3 \dots 4 \cdot n_{primary}$$

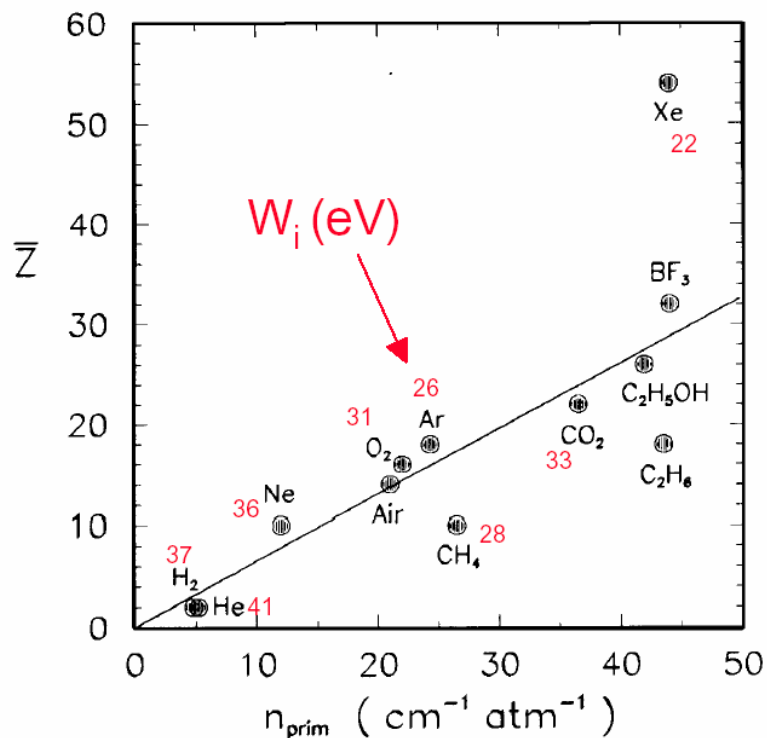
total number of created  
electron-ion pairs.

$\Delta E$  = total energy loss

$W_i$  = effective <energy loss>/pair

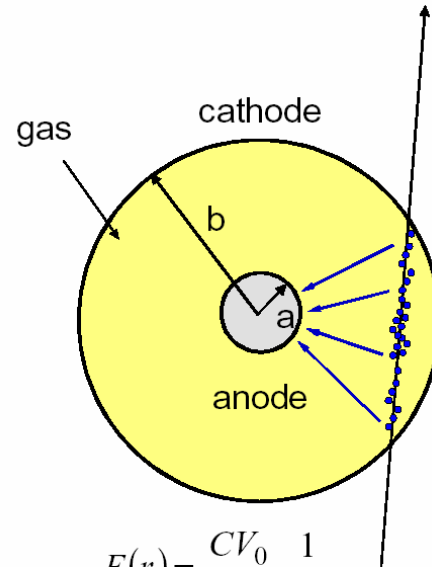
Number of  
primary  
electron/ion pairs  
in frequently  
used (detector)  
gases.

(Lohse and Witzeling,  
Instrumentation In High  
Energy Physics, World  
Scientific, 1992)



# Contatori proporzionali

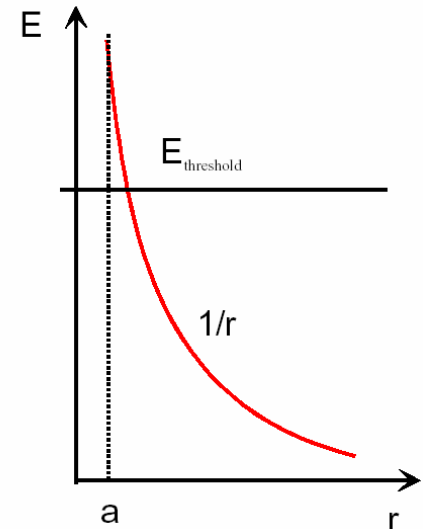
- ◆ Poche centinaia di elettroni sono troppo pochi da rivelare
- ◆ Il rumore elettronico spesso e' dello stesso ordine di grandezza ed anche piu`
- ◆ Amplificazione del segnale direttamente sul detector:
  - Meccanismo di moltiplicazione a valanga



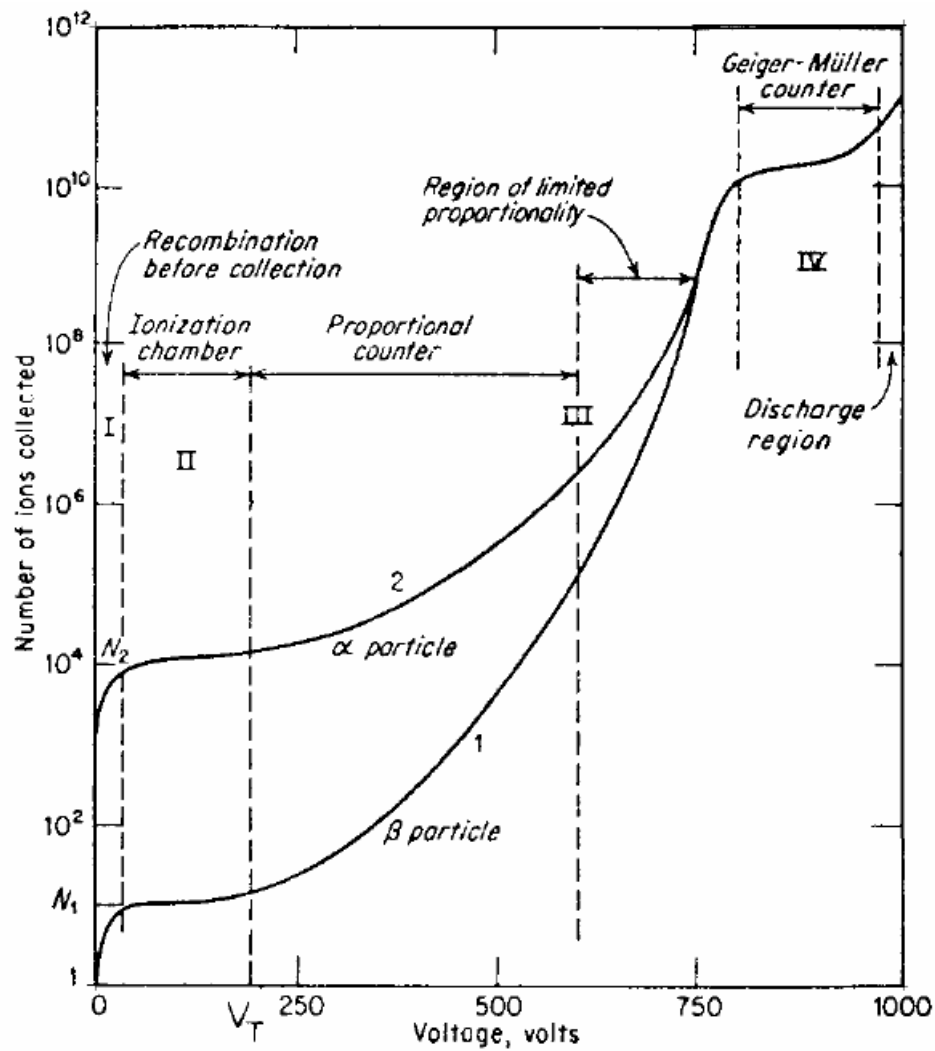
$$E(r) = \frac{CV_0}{2\pi\epsilon_0} \cdot \frac{1}{r}$$

$$V(r) = \frac{CV_0}{2\pi\epsilon_0} \cdot \ln \frac{r}{a}$$

$C$  = capacitance / unit length

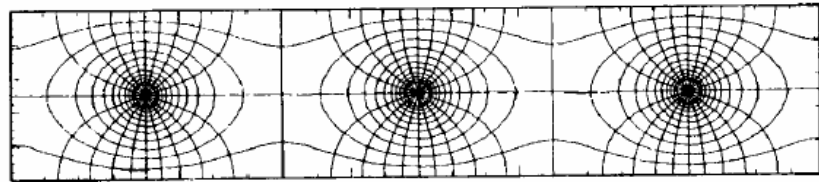
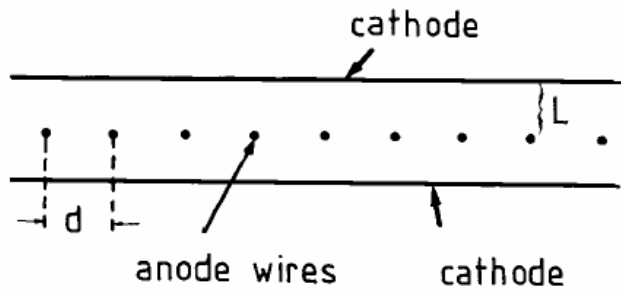




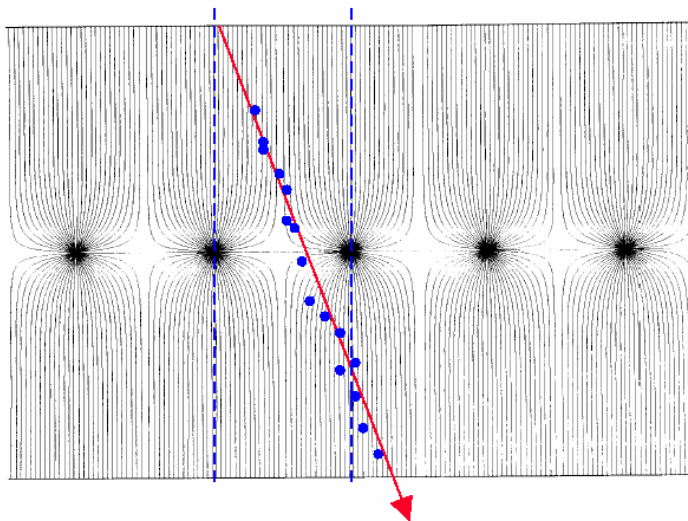


# Multi wire proportional chamber (MWPC)

(G. Charpak et al. 1968, Nobel prize 1992)



field lines and equipotentials around anode wires



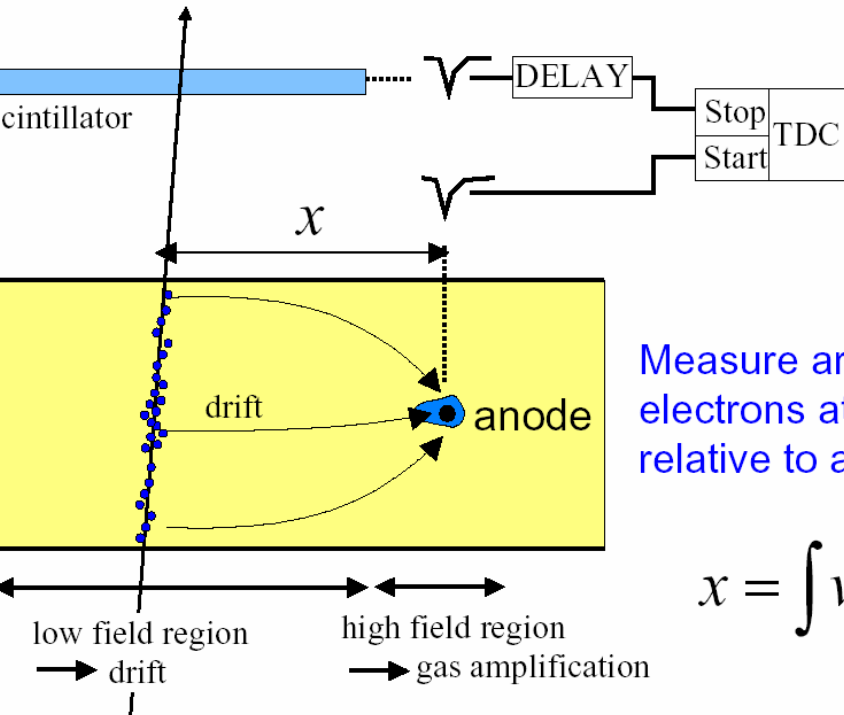
Typical parameters:  
 $L=5\text{mm}$ ,  $d=1\text{mm}$ ,  
 $a_{\text{wire}}=20\text{mm}$ .

Normally digital readout:  
spatial resolution limited to

$$\sigma_x \approx \frac{d}{\sqrt{12}}$$

(  $d=1\text{mm}$ ,  
 $\sigma_x=300\ \mu\text{m}$  )

# Camere a deriva



Measure arrival time of electrons at sense wire relative to a time  $t_0$ .

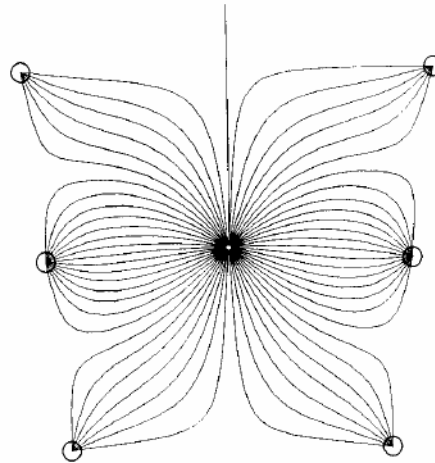
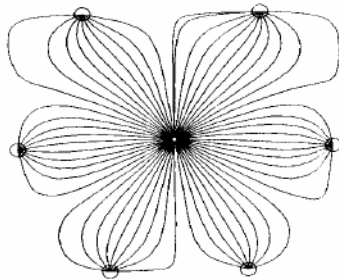
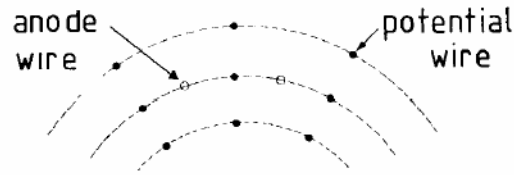
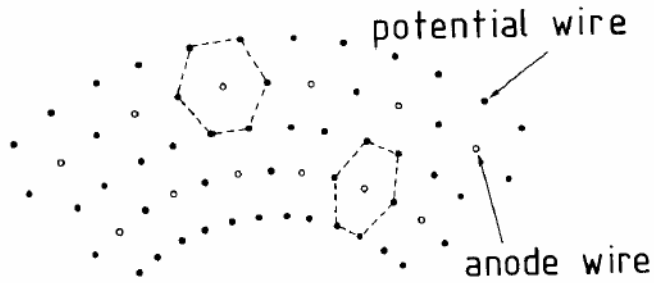
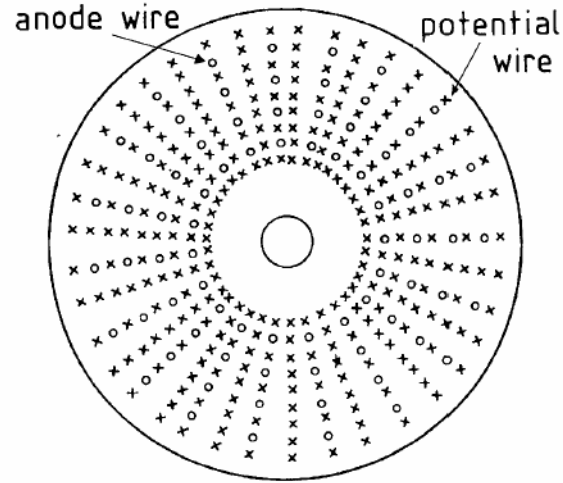
$$x = \int v_D(t) dt$$

Hanno il vantaggio di avere meno fili, meno elettronica, e meno strutture di supporto rispetto alle MWPC

La risoluzione non e' limitata dalla dimensione della cella

Se si controlla la miscela di gas si ottengono buone risoluzioni  $\geq 50$  micron

# Various geometries of cylindrical drift chambers

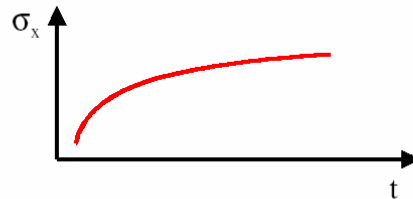


# Diffusione

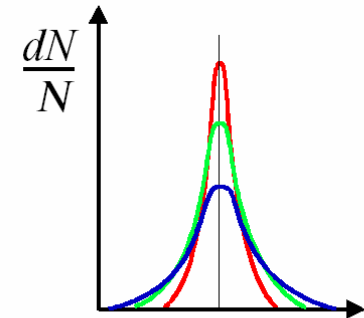
In assenza di campo elettrico gli elettroni e gli ioni diffondono

$$\frac{dN}{N} = \frac{1}{\sqrt{4\pi Dt}} e^{-(x^2/4Dt)} dx$$

$$\sigma_x(t) = \sqrt{2Dt} \quad \text{or} \quad D = \frac{\sigma_x^2(t)}{2t}$$



$D$ : diffusion coefficient

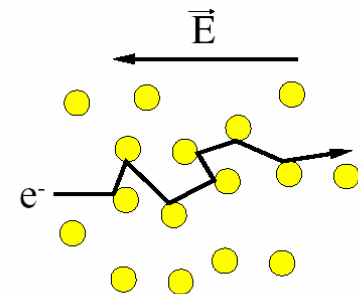


External electric field:

“stop and go” traffic due to scattering from gas atoms

→ drift

$$\vec{v}_D = \mu \vec{E} \quad \mu = \frac{e\tau}{m} \quad (\text{mobility})$$



# Moto in un campo (E,B)

$$\frac{\vec{v}_D}{\tau} + \frac{e\vec{B} \times \vec{v}_D}{m_e} = \frac{eE}{m_e}$$

$$\vec{v}_D = \frac{\mu E}{1 + \omega^2 \tau^2} \left[ \vec{E} + \frac{\vec{E} \times \vec{B}}{|\vec{B}|} \omega \tau + \frac{(\vec{E} \cdot \vec{B}) \cdot \vec{B}}{|\vec{B}|^2} \omega^2 \tau^2 \right]$$

$$\omega = \frac{e|\vec{B}|}{m_e} \quad (\text{Frequenza di ciclotrone})$$

$\tau$  = tempo medio di collisione

$\omega\tau \ll 1$  e<sup>-</sup> seguono E

$\omega\tau \gg 1$  e<sup>-</sup> seguono B

Velocita' tipica per elettroni nei gas

~ 5 cm/ $\mu$ s

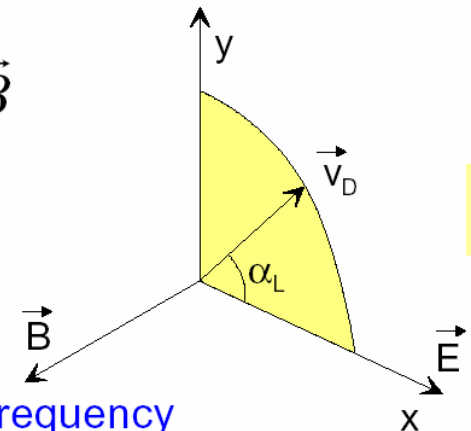
Per gli ioni 1000 volte minore

Special case:  $\vec{E} \perp \vec{B}$

$$\tan \alpha_L = \omega\tau$$

$\alpha_L$ : Lorentz angle

$$\omega = \frac{e\vec{B}}{m} \quad \text{cyclotron frequency}$$



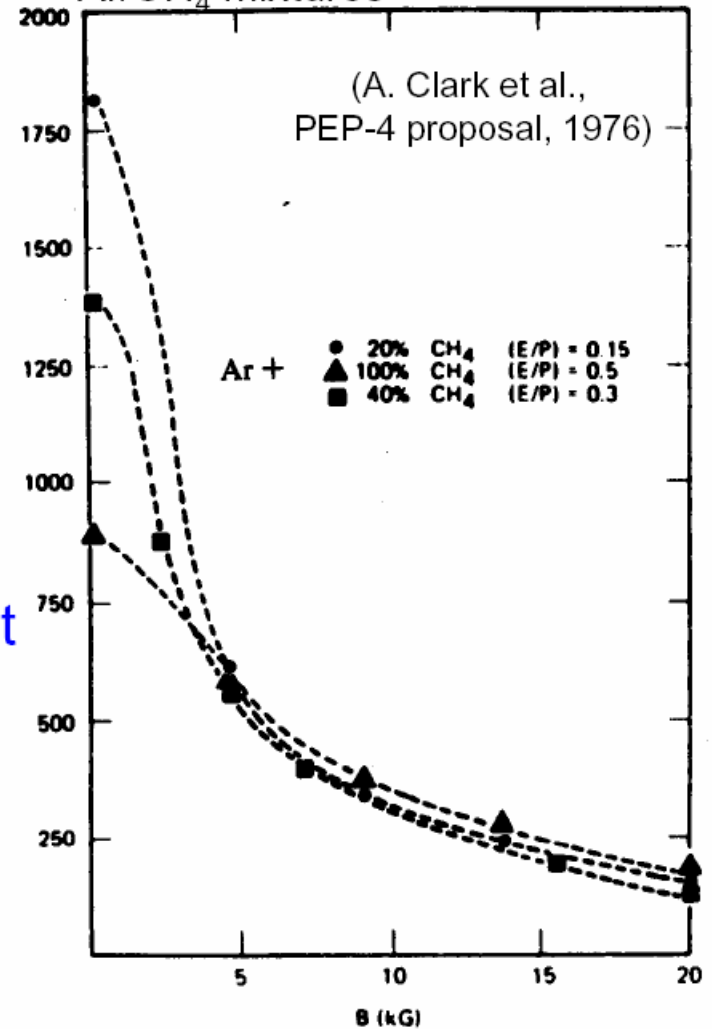
Special case:  $\vec{E} \parallel \vec{B}$

The longitudinal diffusion (along B-field) is unchanged.

In the transverse projection the electrons are forced on circle segments with the radius  $v_T/\omega$ . The transverse diffusion coefficient appears reduced

$$D_T(B) = \frac{D_0}{1 + \omega^2 \tau^2}$$

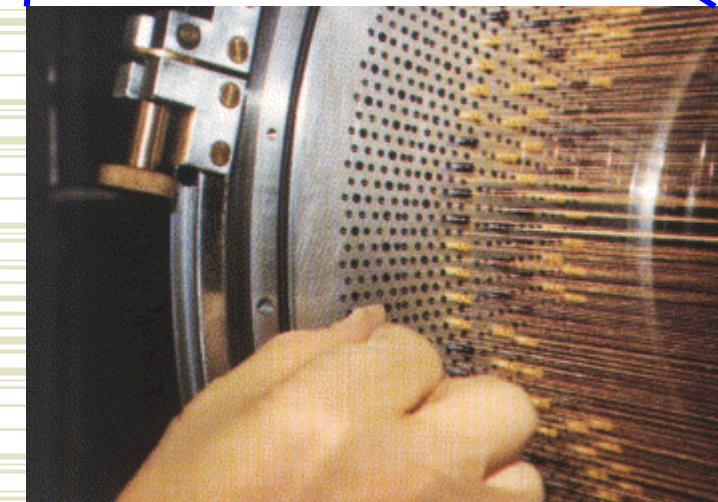
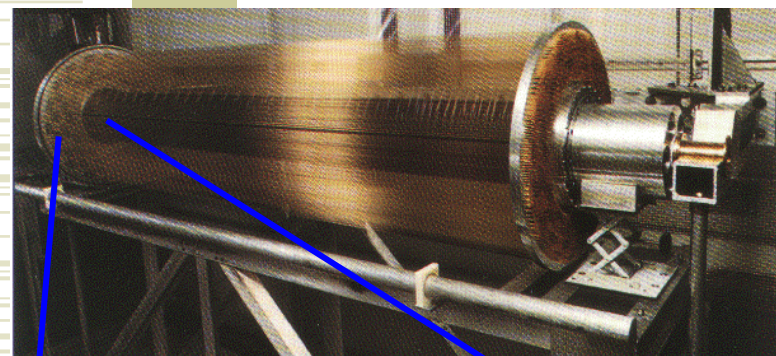
Transverse diffusion  $\sigma$  ( $\mu\text{m}$ ) for a drift of 15 cm in different Ar/CH<sub>4</sub> mixtures



# ITC (ALEPH)

Inner Tracking Chamber

# Esempi

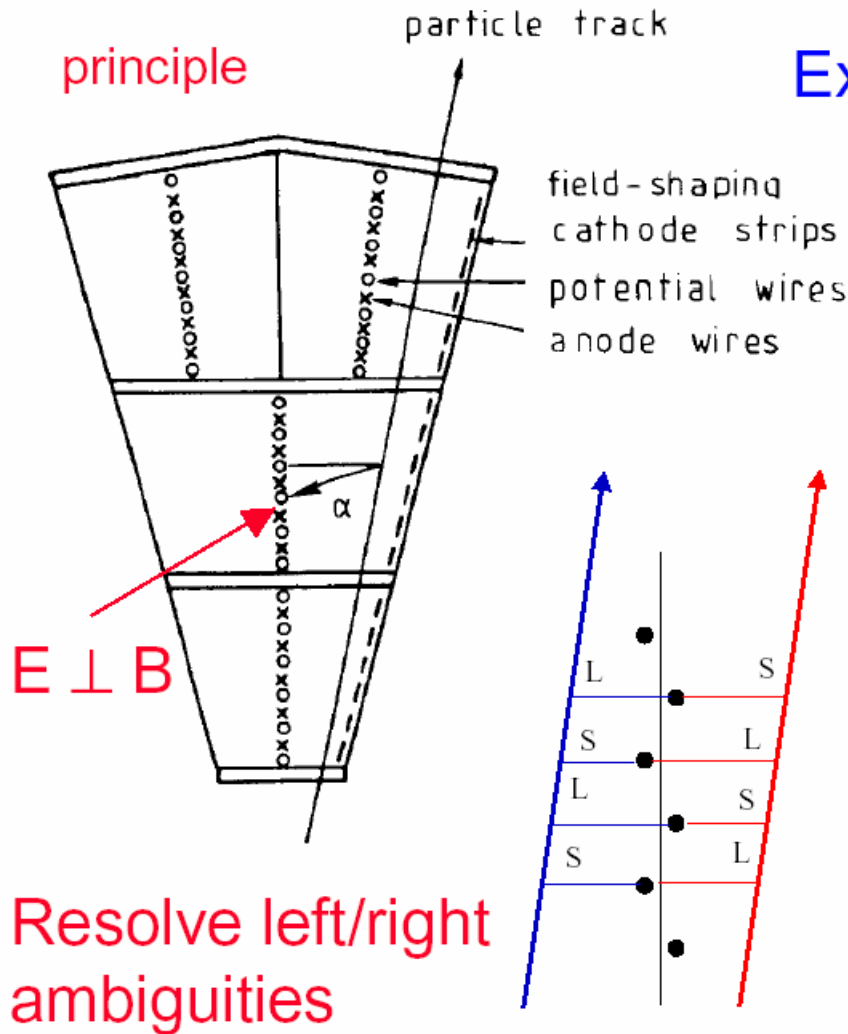




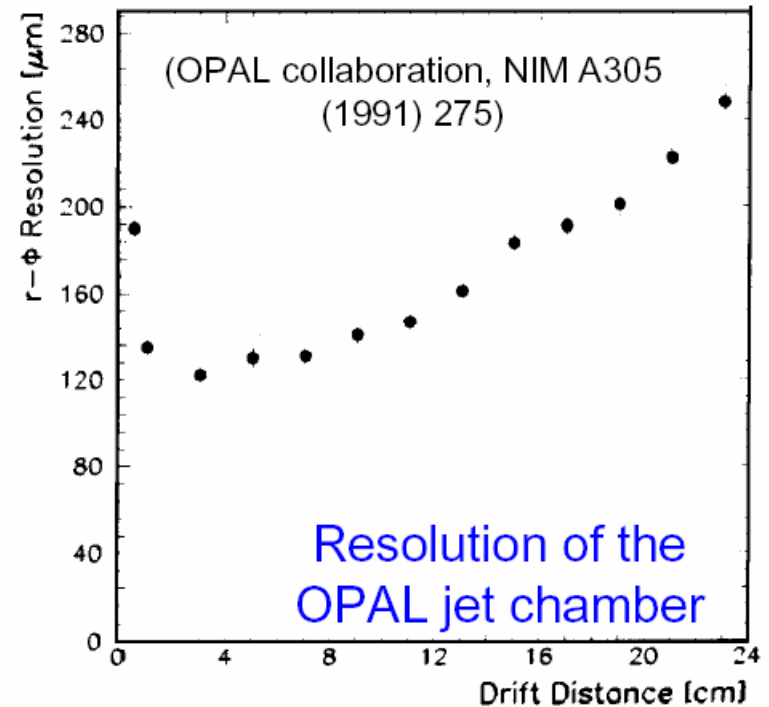
# Jet chambers: Optimized for maximum number of measurements in radial direction

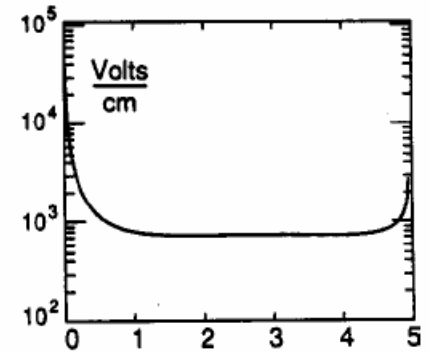
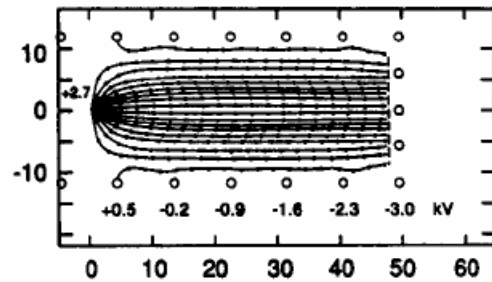
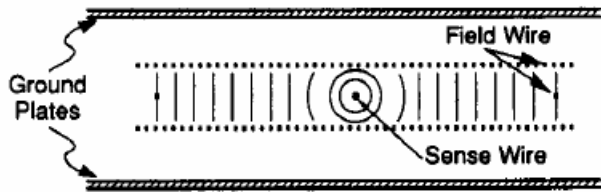
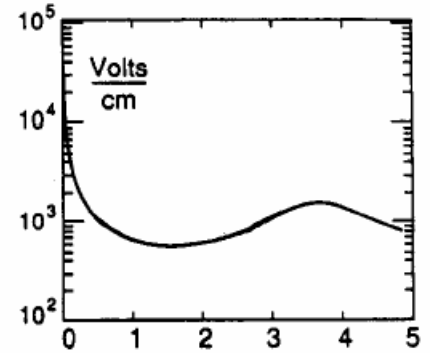
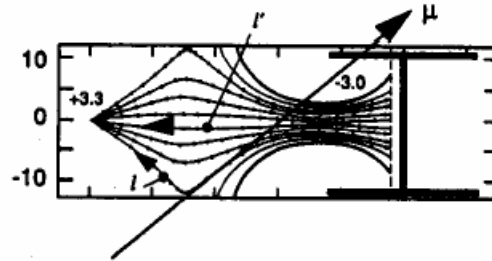
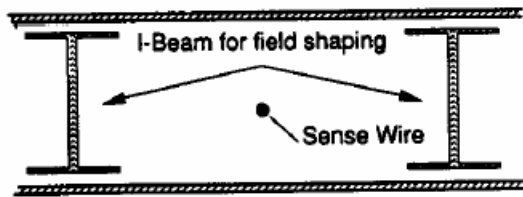
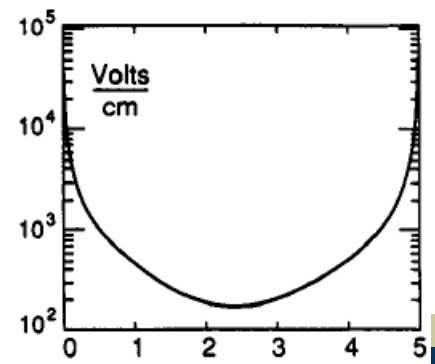
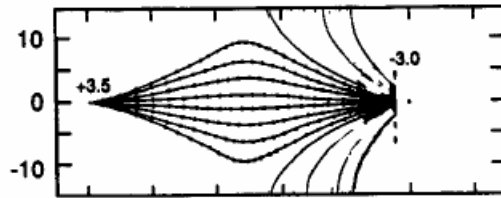
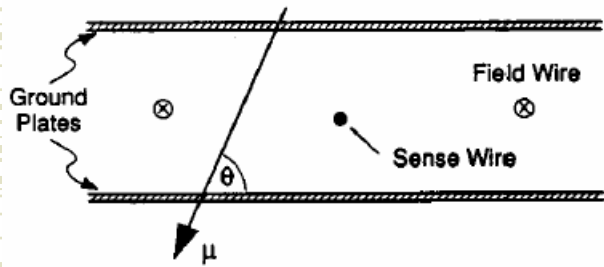
principle

Example: OPAL Jet chamber



$\varnothing=3.7\text{m}$ ,  $L=4\text{m}$ , 24 sectors à  
159 sense wires ( $\pm 100\ \mu\text{m}$   
staggered).  $3\ \text{cm} < l_{\text{drift}} < 25\ \text{cm}$

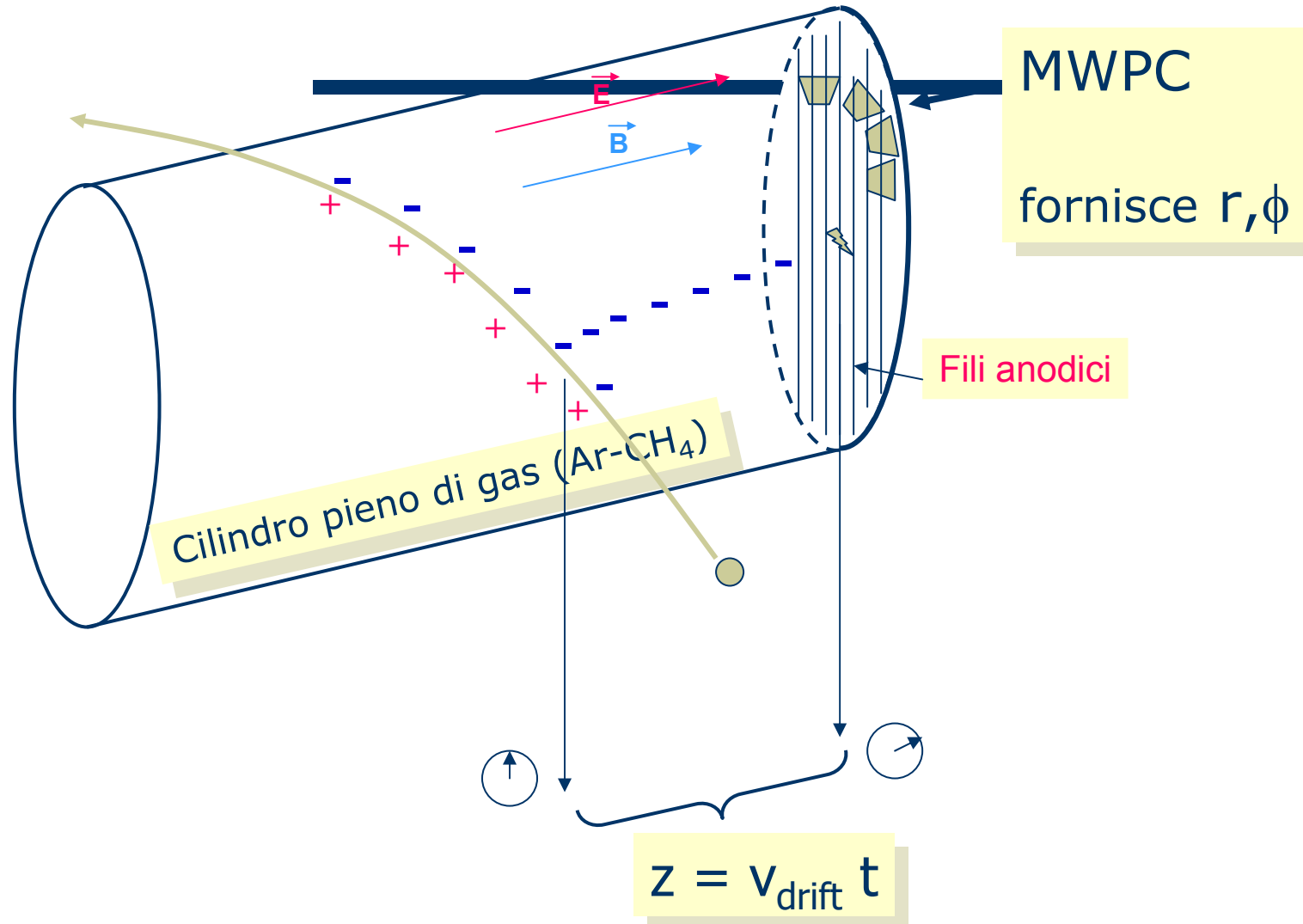




[mm]

[cm]

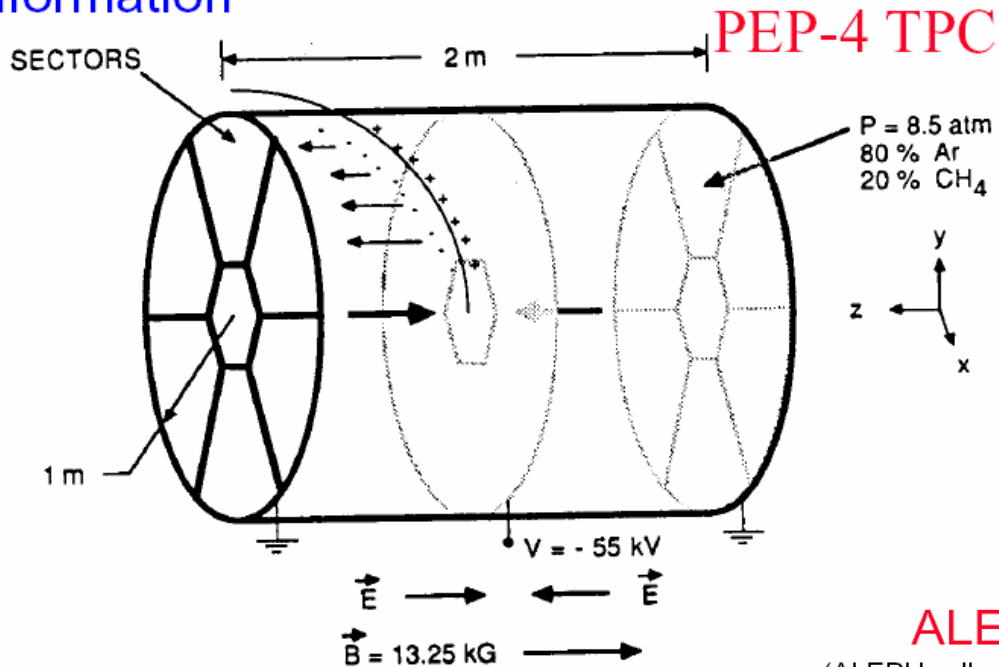
# La Time Projection Chamber (TPC)



- ▶ x-y from wires and segmented cathode of MWPC
- ▶ z from drift time
- ▶ in addition dE/dx information

Diffusion significantly reduced by B-field.

Requires precise knowledge of  $v_D$  → LASER calibration + p, T corrections

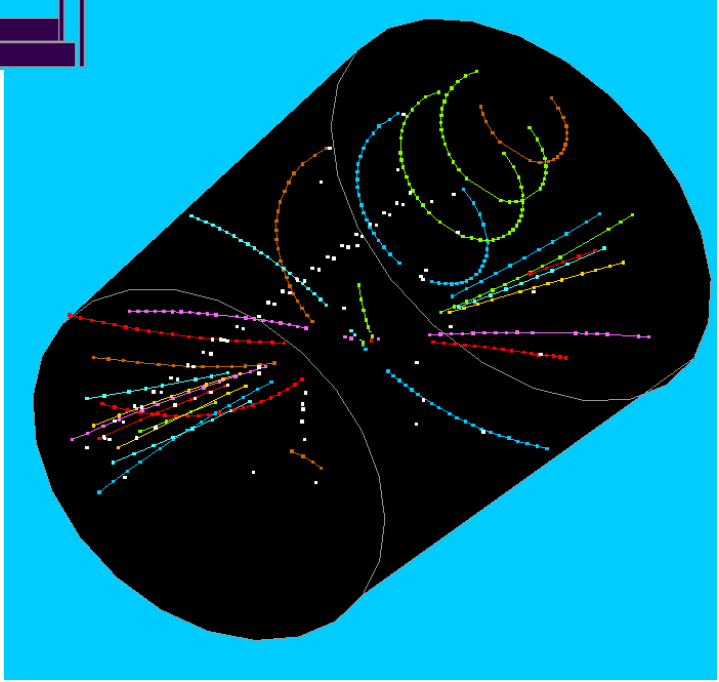
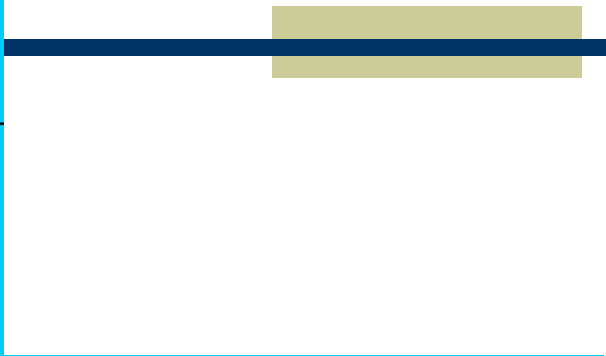
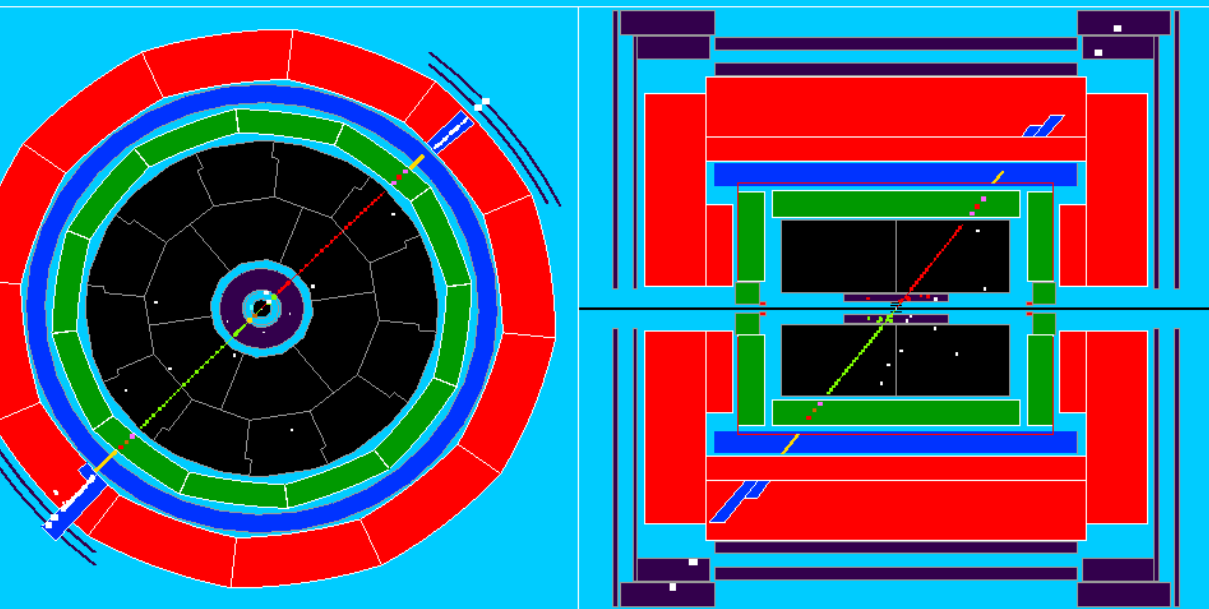


### ALEPH TPC

(ALEPH coll., NIM A 294 (1990) 121,  
W. Atwood et. Al, NIM A 306 (1991) 446)

Ø 3.6M, L=4.4 m

$\sigma_{R\phi} = 173 \mu\text{m}$   
 $\sigma_z = 740 \mu\text{m}$   
(isolated leptons)

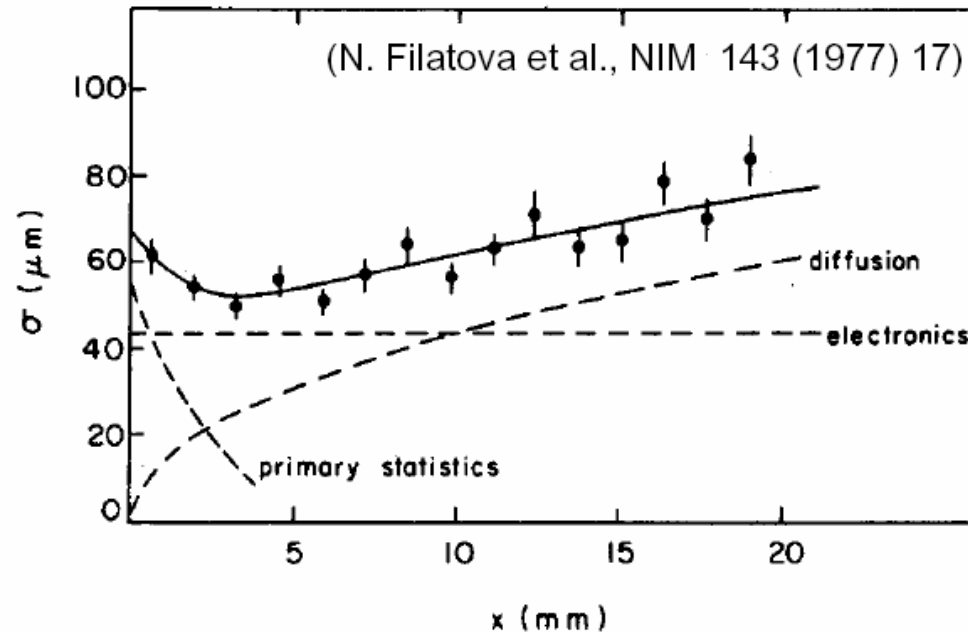


# Limitazioni

- ◆ **Risoluzione determinata da**
  - Statistica della ionizzazione primaria  $\propto \sqrt{N}$
  - Spaziatura tra i fili  $\propto s/\sqrt{12}$
  - Diffusione
  - Fluttuazioni nel percorso
  - Rumore elettronico

Per una maggiore precisione  
occorrono rivelatori a passo piu'  
piccolo

E' possibile sia con rivelatori a gas (MSGC,  
GEM ecc), (Lezioni di G. Spandre), ma meglio  
con i rivelatori al silicio (Lezioni di R. Dell'Orso)



# Rivelatori al silicio

👉 Band gap:  $E_g = 1.12 \text{ V}$ .

👉  $E(\text{e-hole pair}) = 3.6 \text{ eV}$ , ( $\approx 30 \text{ eV}$  for gas detectors).

👉 High specific density ( $2.33 \text{ g/cm}^3$ )  $\rightarrow \Delta E/\text{track length}$  for

M.I.P.'s.:  $390 \text{ eV}/\mu\text{m} \approx 108 \text{ e-h}/\mu\text{m}$  (average)

👉 High mobility:  $\mu_e = 1450 \text{ cm}^2/\text{Vs}$ ,  $\mu_h = 450 \text{ cm}^2/\text{Vs}$

👉 Detector production by microelectronic techniques  $\rightarrow$  small dimensions  $\rightarrow$  fast charge collection ( $< 10 \text{ ns}$ ).

👉 Rigidity of silicon allows thin self supporting structures.

Typical thickness  $300 \mu\text{m} \rightarrow \approx 3.2 \cdot 10^4 \text{ e-h}$  (average)

👉 But: No charge multiplication mechanism!

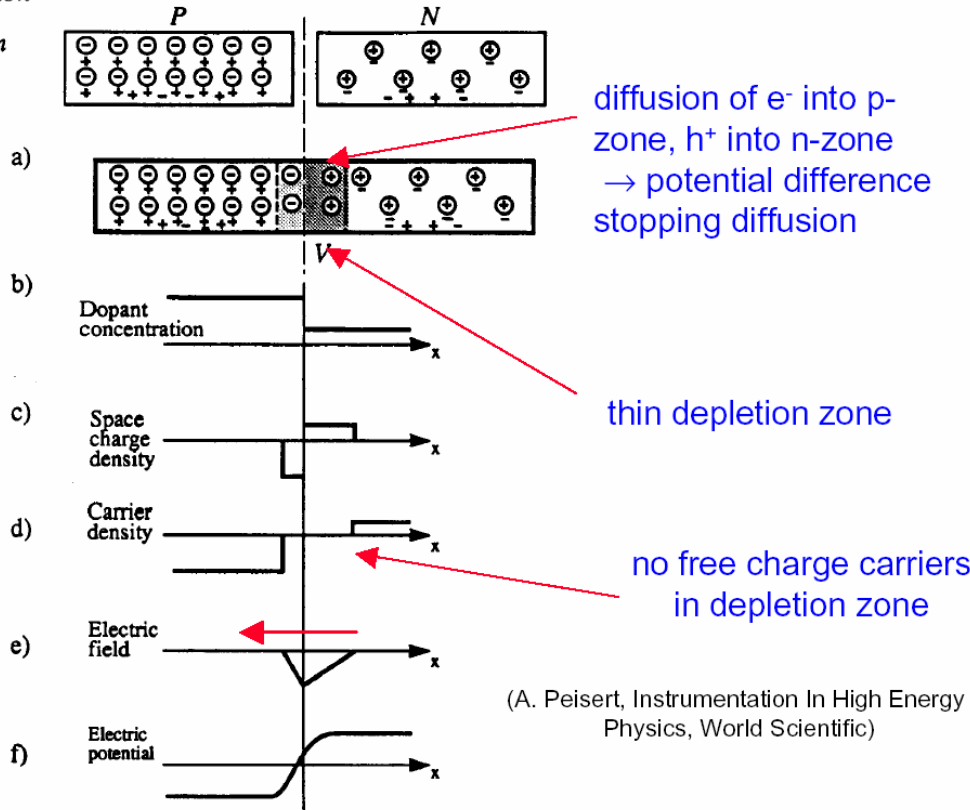
## ● Tempo di collezione di carica, diffusione

- ♦ Velocità di deriva dei portatori di carica  $v = \mu E$ , drift time,  $t_d = d/v = d/\mu E$
- ♦ Valori tipici:  $d = 300 \mu\text{m}$ ,  $E = 2.5 \text{ kV/cm}$ ,  $\mu_e = 1350 \text{ cm}^2/\text{V}\cdot\text{s}$ ,  $\mu_h = 450 \text{ cm}^2/\text{V}\cdot\text{s}$ ,

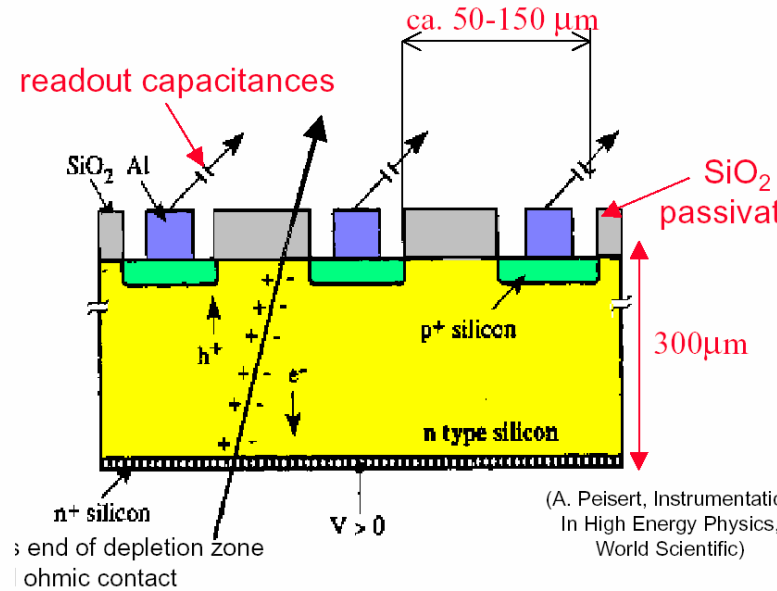
♦  $t_d(e) = 9 \text{ ns}$ ,  $t_d(h) = 27 \text{ ns}$

Acceptor ion  
Donor ion  
hole  
electron

# THE PN JUNCTION



(A. Peisert, Instrumentation In High Energy Physics, World Scientific)



(A. Peisert, Instrumentation In High Energy Physics, World Scientific)

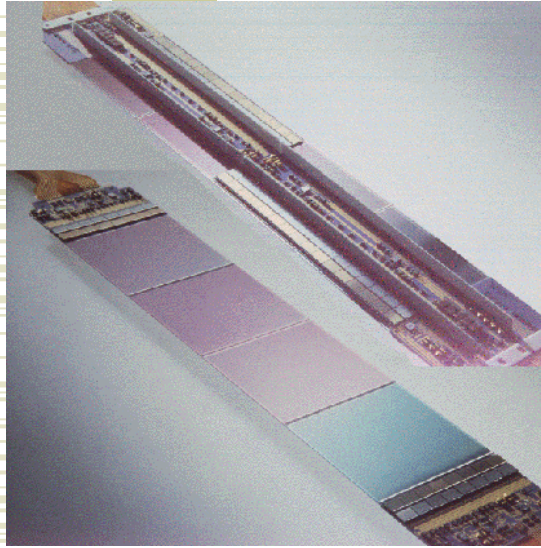
$$dE/dx_{Si} = 3.88 \text{ MeV/cm, per } 300\mu m \text{ spessore} \Rightarrow 116 \text{ keV}$$

**Questa e' l'energia media, la perdita piu' probabile e' data dal picco della Landau: (0.7 × media) ⇒ 81 keV**

**3.6eV per formare una coppia elettrone lacuna:**

**Carica collezionata ⇒ 22500 e (=3.6fC)**

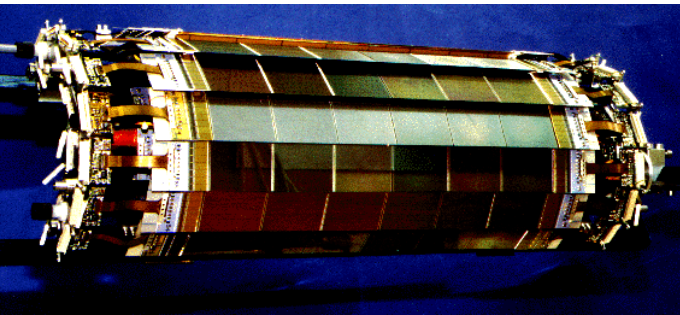
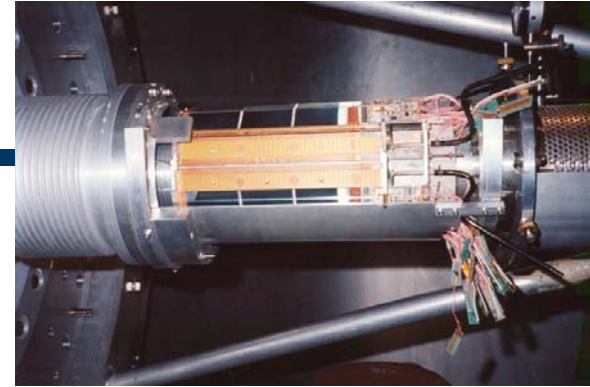


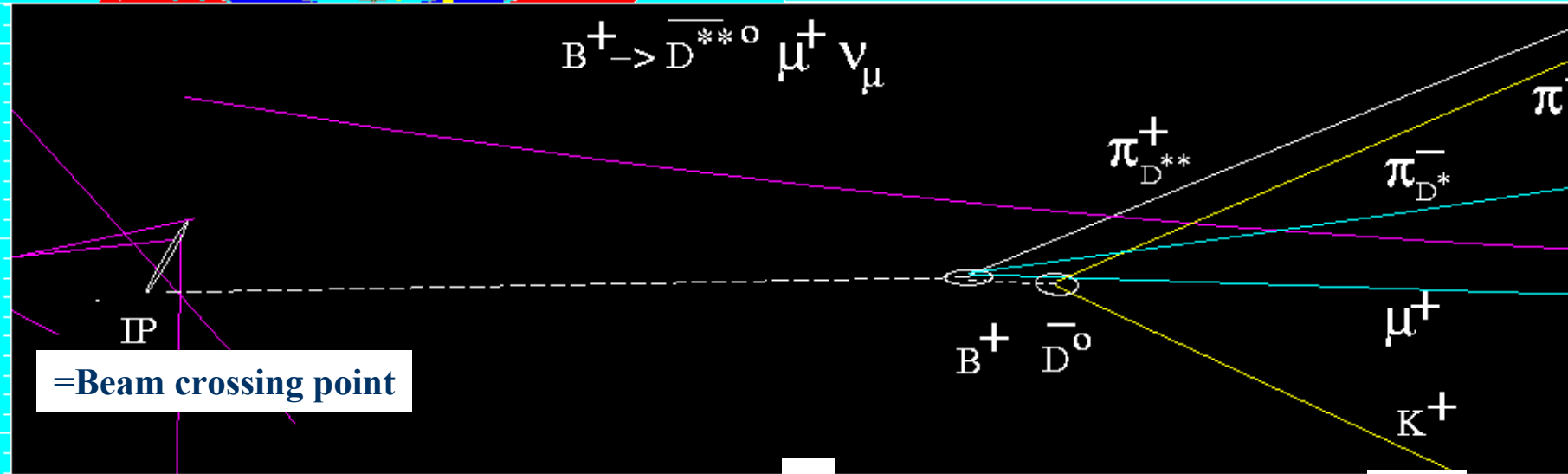
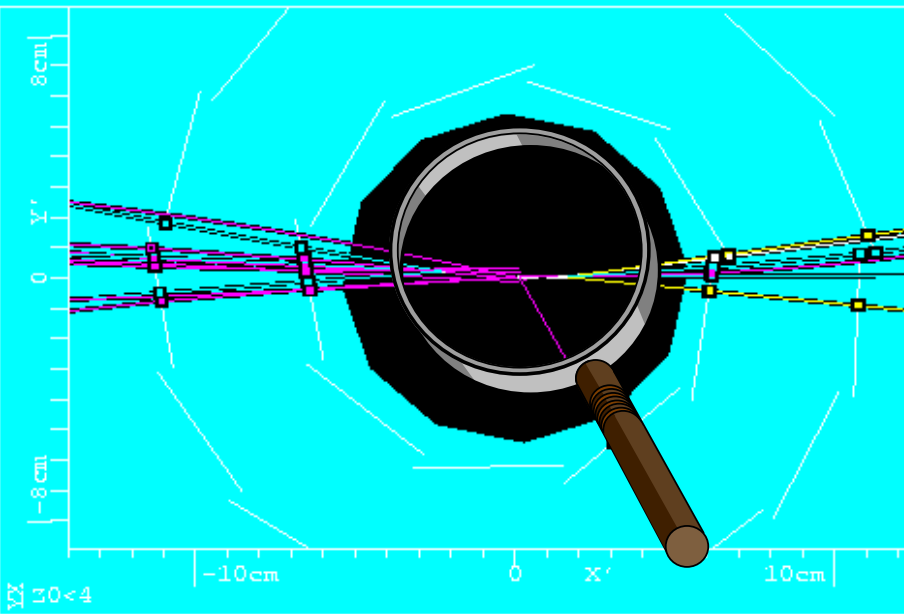
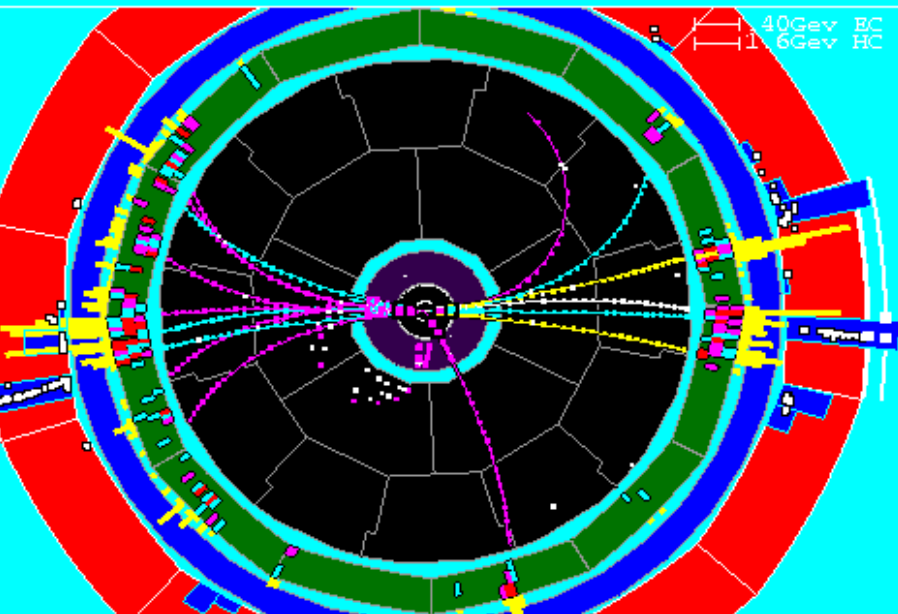


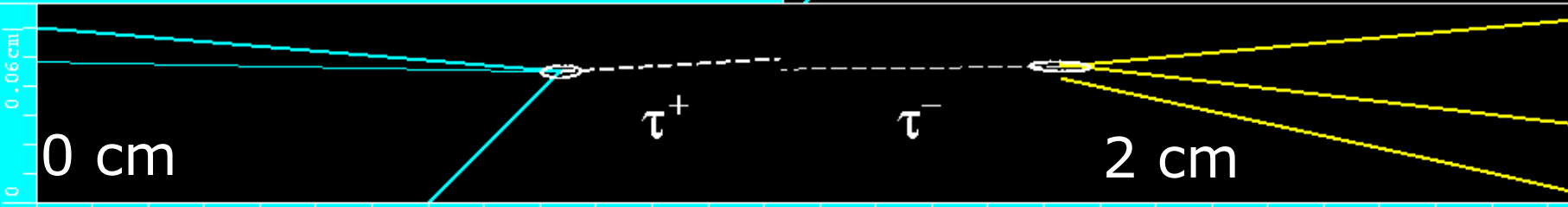
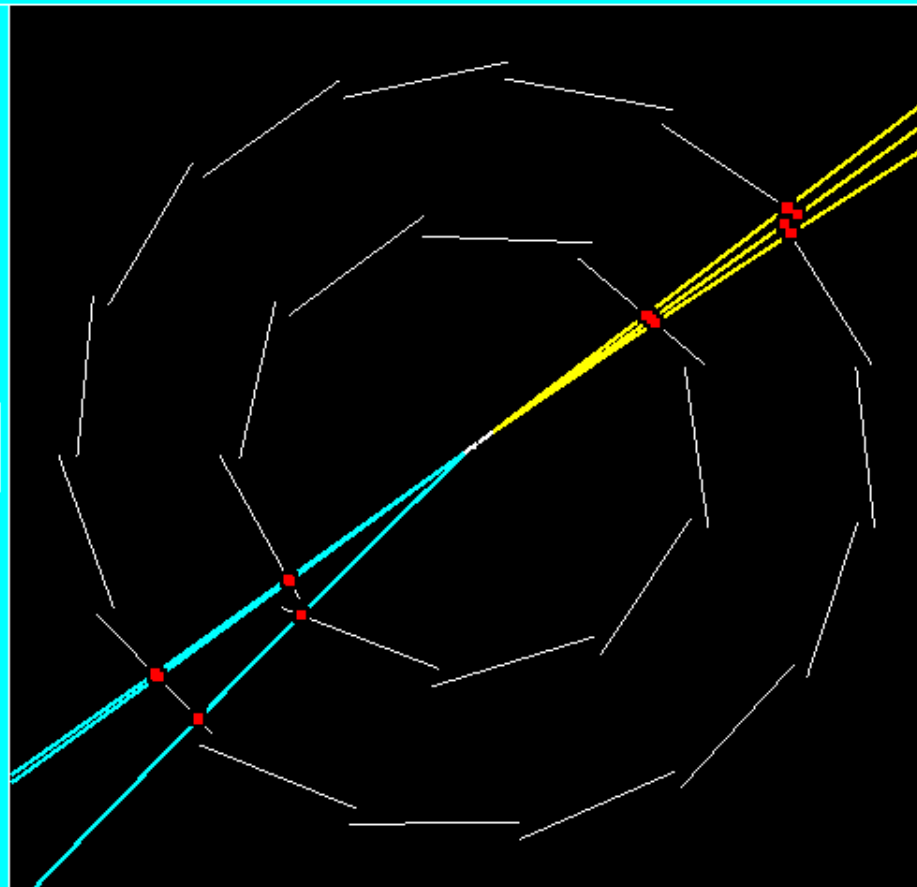
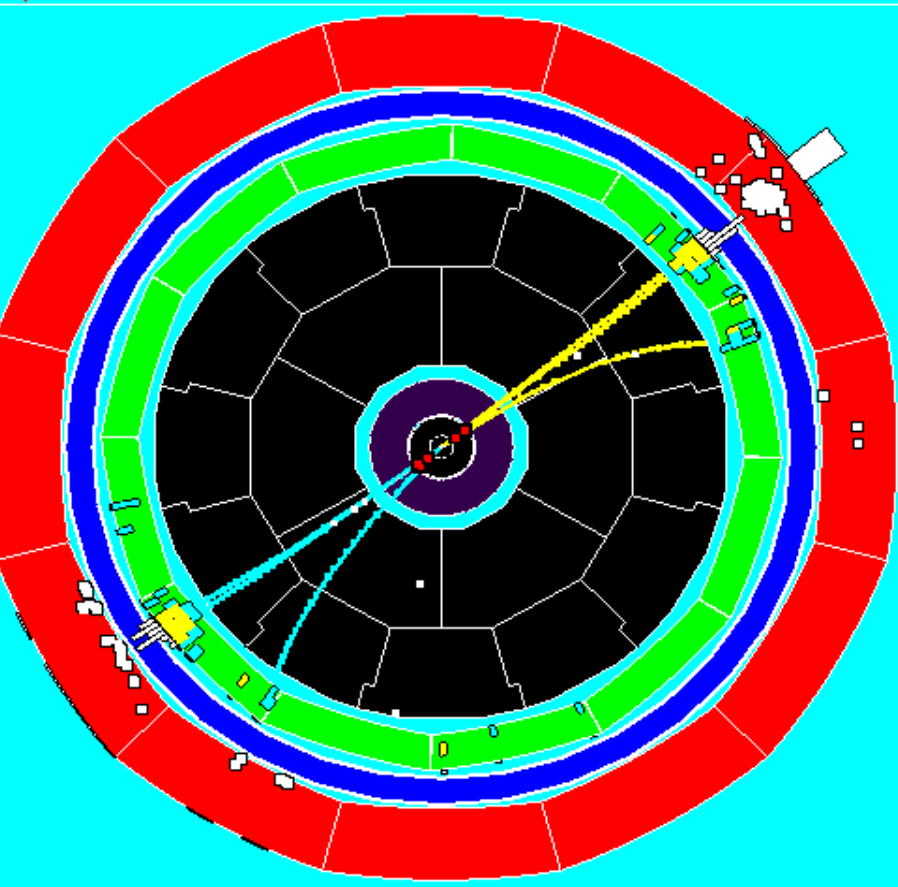
**ALEPH VDET**



**OPAL VDET**



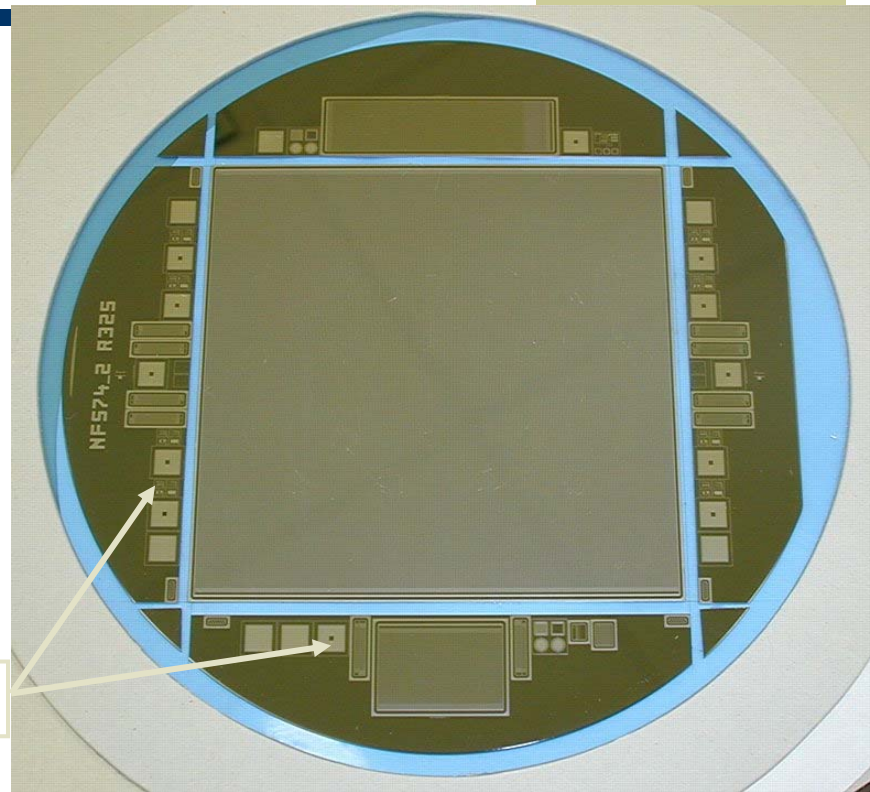




Vita media del tau  $\tau=290 \times 10^{-15}$  sec !! -->  $c\tau = 87 \mu\text{m}$

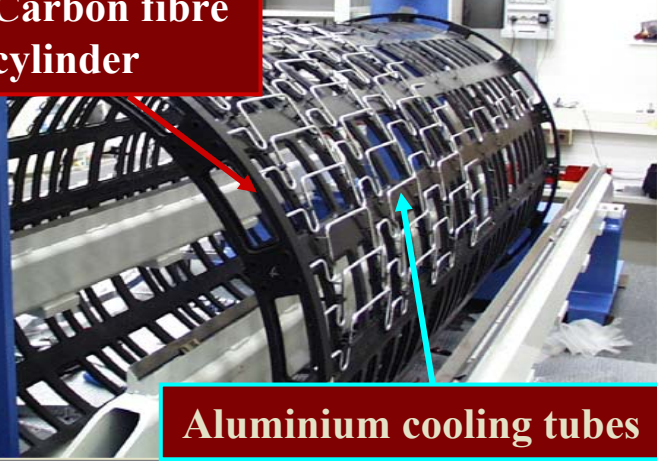
## CMS silicon strip sensor from 6" wafer

Test structures



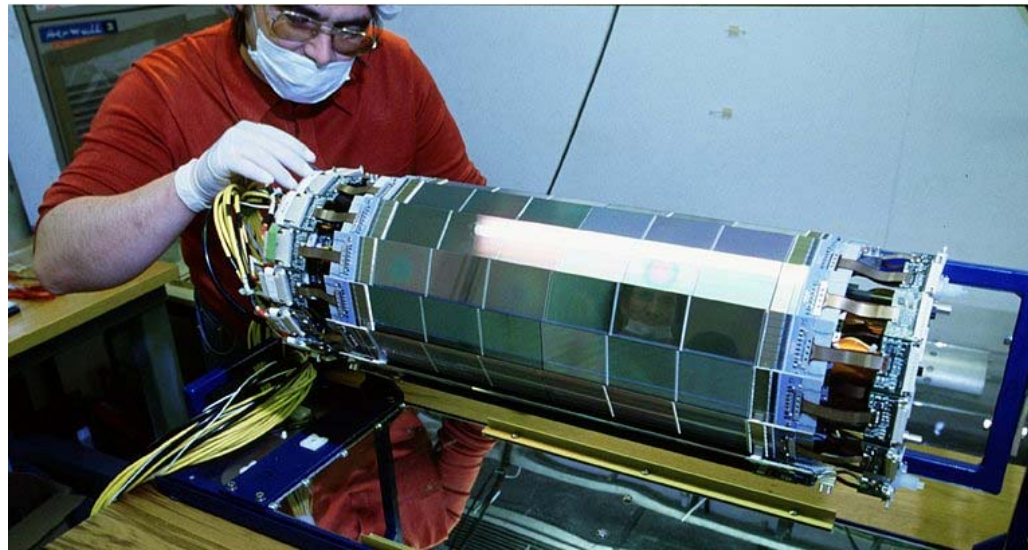


**Carbon fibre  
cylinder**



**Aluminium cooling tubes**

**CMS prototype structure**



**ALEPH 1998**

## OPAL (LEP) module

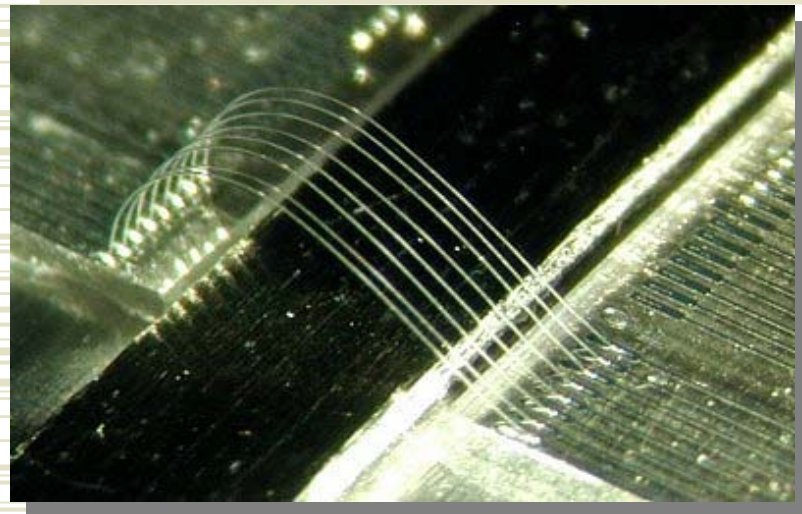
~200 wire bonds

4 x 640 wire bonds

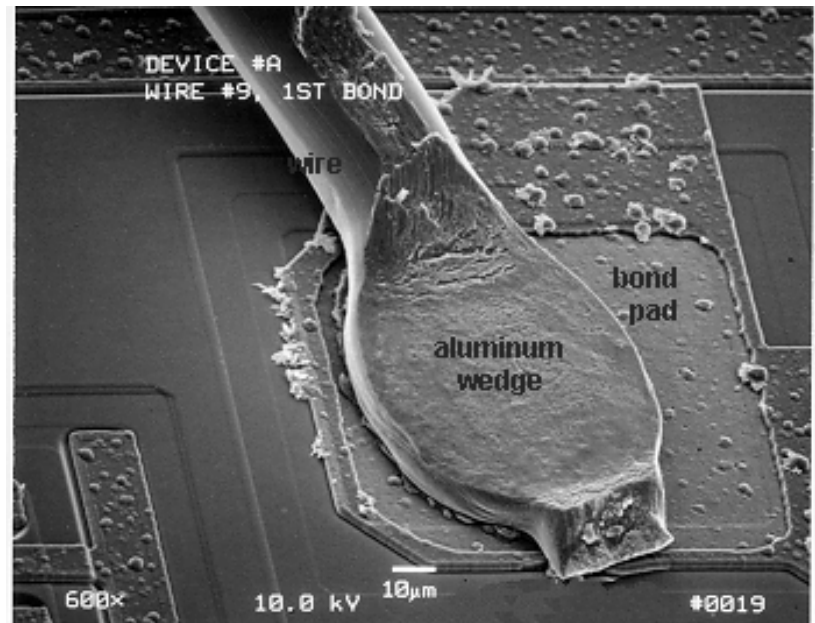
Total ~2700 wire bonds



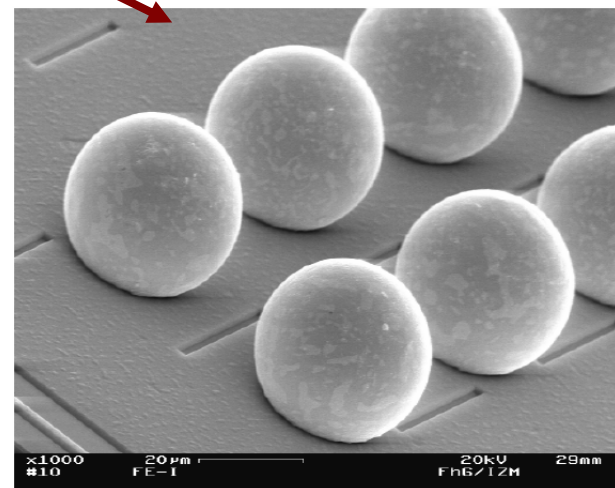
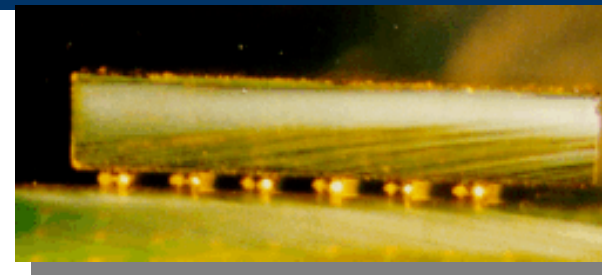
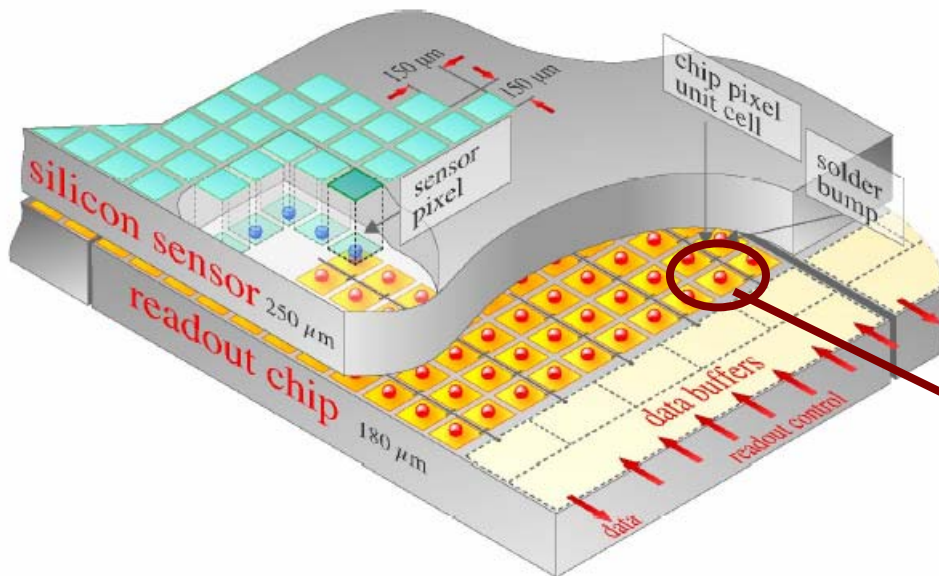
Vista al microscopio delle connessioni dei fili tra il sensore e l'elettronica di uscita



Electron micrograph of bond "foot"



# Pixel detectors



Risoluzioni  $\sim 15 \mu\text{m}$

Punti 3-dimensionali

Possibile equipaggiare grandi aree ( $\sim 1\text{m}^2$ )

Veloci

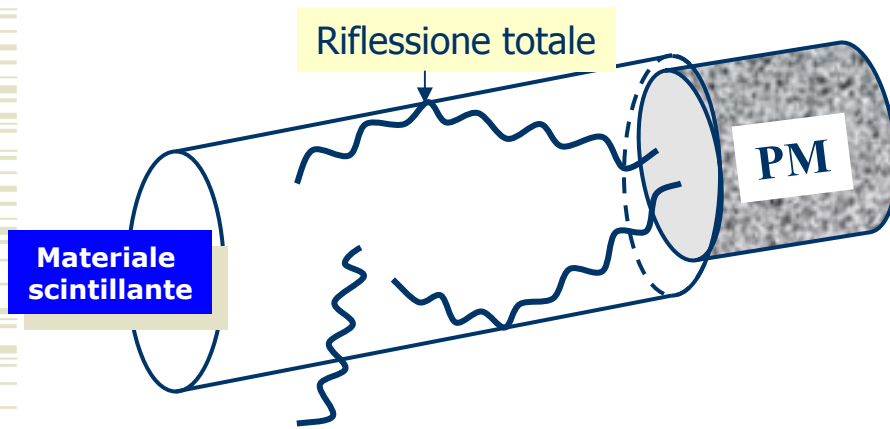
Resistenti alla radiazione

Verranno utilizzati a LHC

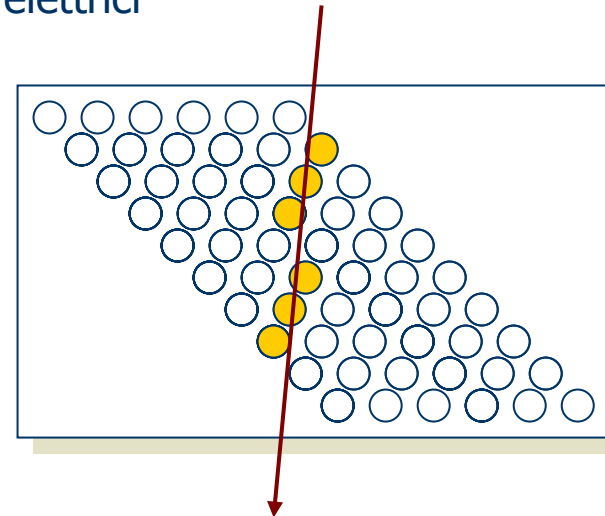


# Fibre scintillanti

- ◆ Certi materiali emettono luce al passaggio di una particella carica  
(scintillatori plastici, polimeri aromatici ...)
- ◆ Possono essere estremamente veloci! (pochi ns)



fotomoltiplicatore: conversione della luce in segnali elettrici



Molte fibre vicine  
→ Rivelazione della traccia

**risoluzione** : pochi 100  $\mu\text{m}$ /punto,  
giu' a  $< 50\mu\text{m}$  nel futuro



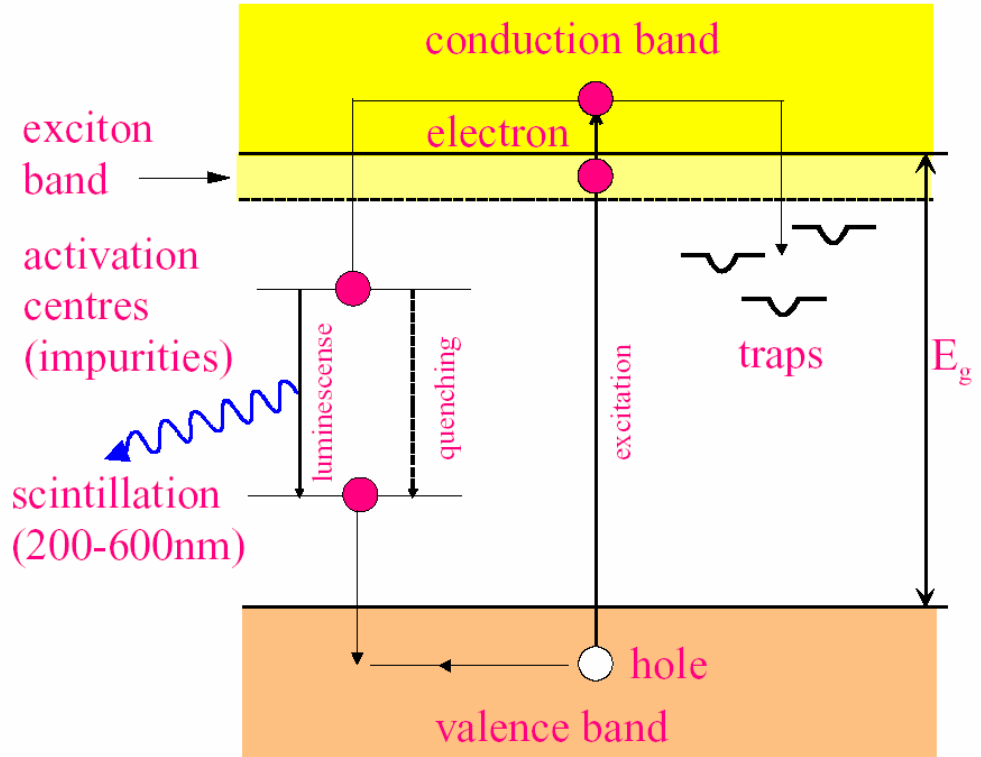
# Fibre scintillanti



Usate per

- Timing
- Calorimetria
- tracciatura

# 1a. Inorganic crystalline scintillators (NaI, CsI, BaF<sub>2</sub>...)



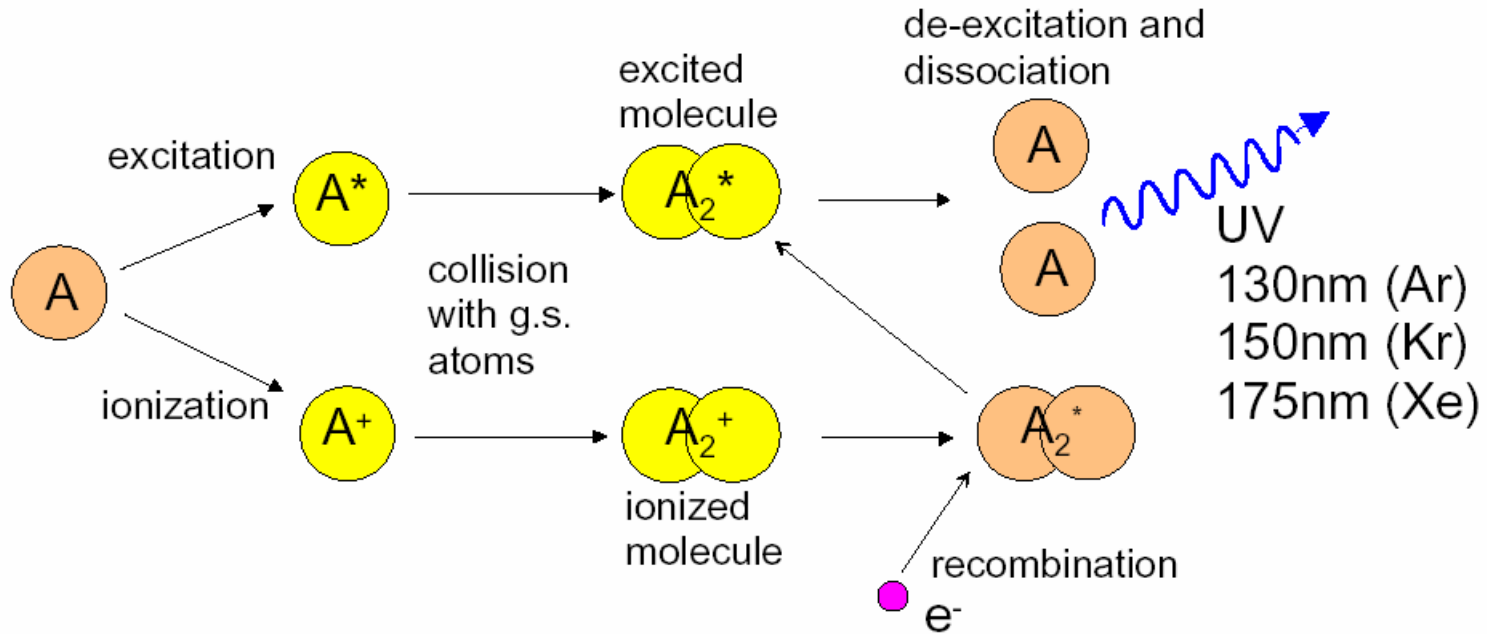
Le particelle ionizzanti attraversando il materiale creano coppie elettrone-lacuna nella banda di eccitazione. Quando questi trovano un centro attivatore (impurezza) o una trappola allora emettono fotoni di scintillazione

often  $\geq 2$  time constants:

- fast recombination (ns- $\mu$ s) from activation centre
- delayed recombination due to trapping ( $\approx 100$  ms)

Due to the high density and high Z inorganic scintillators are well suited for detection of charged particles, but also of  $\gamma$ .

## 1b. Liquid noble gases (LAr, LXe, LKr)



also here one finds 2 time constants: few ns and 100-1000 ns, but same wavelength.

Table A6.2 Properties of some inorganic scintillators

scintillator composition	density (g/cm <sup>3</sup> )	index of refraction	wavelength of maximum emission (nm)	decay time constant (μs)	scintillation pulse height <sup>1)</sup>	notes	Photons/ MeV	
NaI	3.67	1.78	303	0.06	190	2)	1.1 × 10 <sup>4</sup>	
NaI(Tl)	3.67	1.85	410	0.25	100	3)		
CsI	4.51	1.80	310	0.01	6	3)		
CsI(Tl)	4.51	1.80	565	1.0	45	3)		
CaI(Na)	4.51	1.84	420	0.63	85	3)		
KI(Tl)	3.13	1.71	410	0.24/2.5	24	3)		
<sup>6</sup> LiI(Eu)	4.06	1.96	470-485	1.4	35	3)		1.4 × 10 <sup>4</sup>
CaF <sub>2</sub> (Eu)	3.19	1.44	435	0.9	50			
BaF <sub>2</sub>	4.88	1.49	190/220 310	0.0006 0.63	5 15			6.5 × 10 <sup>3</sup> 2 × 10 <sup>3</sup>
Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub>	7.13	2.15	480	0.30	10			2.8 × 10 <sup>3</sup>
CaWO <sub>4</sub>	6.12	1.92	430	0.5/20	50			
ZnWO <sub>4</sub>	7.87	2.2	480	5.0	26			
CdWO <sub>4</sub>	7.90	2.3	540	5.0	40			
CsF	4.65	1.48	390	0.005	5	3)		
CeF <sub>3</sub>	6.16	1.68	300 340	0.005 0.020	5			
ZnS(Ag)	4.09	2.35	450	0.2	150	4)		
GSO	6.71	1.9	440	0.060	20			
ZnO(Ga)	5.61	2.02	385	0.0004	40	4)		
YSO	4.45	1.8	420	0.035	50			
YAP	5.50	1.9	370	0.030	40			

<sup>1)</sup> relative to NaI(Tl) <sup>2)</sup> at 80 K <sup>3)</sup> hygroscopic <sup>4)</sup> polycrystalline

PbWO <sub>4</sub>	8.28	1.82	440, 530	0.01			100
-------------------	------	------	----------	------	--	--	-----

LAr	1.4	1.29 <sup>5)</sup>	120-170	0.005 / 0.860			
LKr	2.41	1.40 <sup>5)</sup>	120-170	0.002 / 0.085			
LXe	3.06	1.60 <sup>5)</sup>	120-170	0.003 / 0.022			4 × 10 <sup>4</sup>

<sup>5)</sup> at 170 nm

CLEO (CESR)

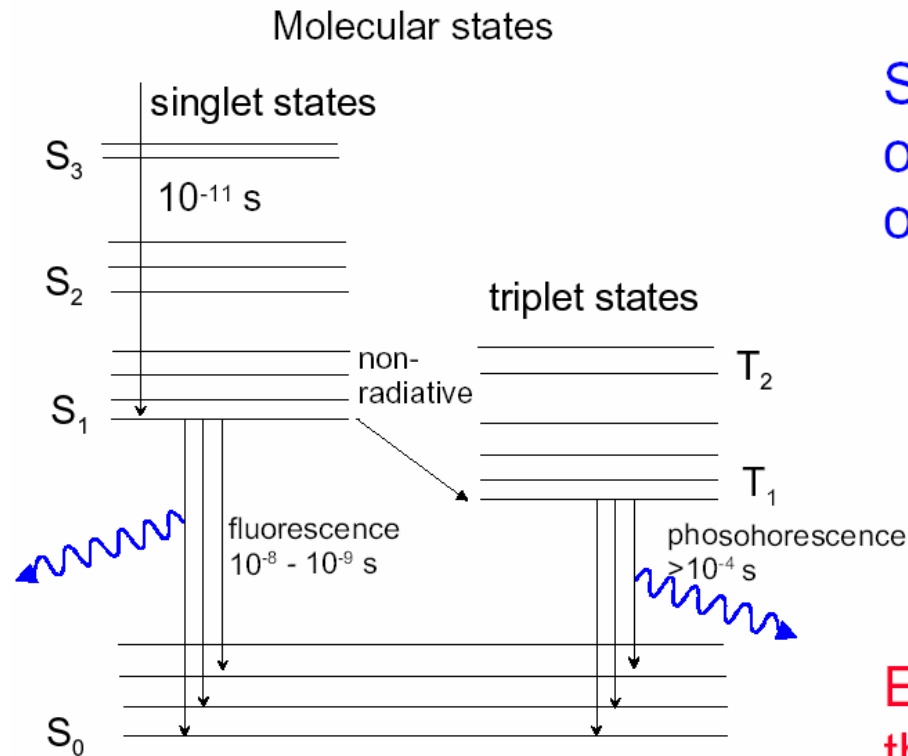
L3 (LEP)

CMS (CERN)

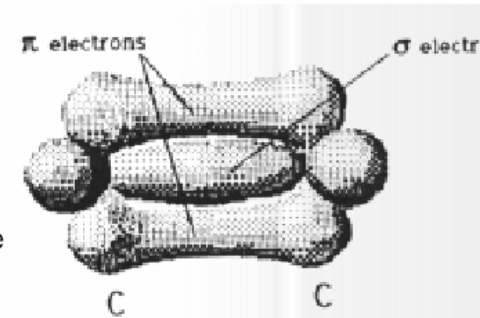
NA48 (CERN)

## 2. Organic scintillators: Monocrystals or liquids or plastic solutions

Nel caso di scintillatori organici i livelli interessati sono quelli molecolari



Scintillation is based on the 2  $\pi$  electrons of the C-C bonds.



Emitted light is in the UV range.

scintillator	density (g/cm <sup>3</sup> )	index of refraction	wavelength of maximum emission (nm)	decay time constant (ns)	scintillation pulse height <sup>1)</sup>	H/C ratio <sup>2)</sup>	yield/ NaI
Monocrystals							
naphthalene	1.15	1.58	348	11	11	0.800	0.5
anthracene	1.25	1.59	448	30-32	100	0.714	
trans-stilbene	1.16	1.58	384	3-8	46	0.857	
p-terphenyl	1.23		391	6-12	30	0.778	
lastics <sup>3)</sup>							
NE 102 A	1.032	1.58	425	2.5	65	1.105	
NE 104	1.032	1.58	405	1.8	68	1.100	
NE 110	1.032	1.58	437	3.3	60	1.105	
NE 111	1.032	1.58	370	1.7	55	1.096	
lastics <sup>4)</sup>							
BC-400	1.032	1.581	423	2.4	65	1.103	
BC-404	1.032	1.58	408	1.8	68	1.107	
BC-408	1.032	1.58	425	2.1	64	1.104	
BC-412	1.032	1.58	434	3.3	60	1.104	
BC-414	1.032	1.58	392	1.8	68	1.110	
BC-416	1.032	1.58	434	4.0	50	1.110	
BC-418	1.032	1.58	391	1.4	67	1.100	
BC-420	1.032	1.58	391	1.5	64	1.100	
BC-422	1.032	1.58	370	1.6	55	1.102	
BC-422Q	1.032	1.58	370	0.7	11	1.102	
BC-428	1.032	1.58	480	12.5	50	1.103	
BC-430	1.032	1.58	580	16.8	45	1.108	
BC-434	1.049	1.58	425	2.2	60	0.995	

relative to anthracene  
ratio of hydrogen to carbon atoms  
Nuclear Enterprises Ltd. Sighthill, Edinburgh, U.K.  
Bicron Corporation, Newbury, Ohio, USA

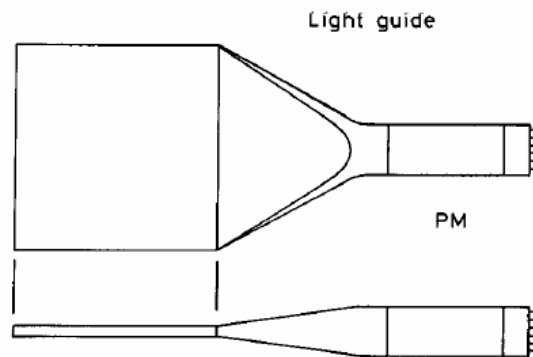
• Scintillatori organici hanno basso Z (H,C).

• Bassa efficienza di rivelazione per fotoni (praticamente solo effetto Compton).

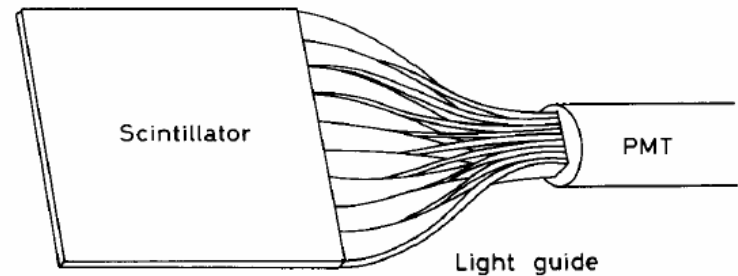
• Alta efficienza per neutroni grazie a reazione (n,p).

# Metodi di lettura

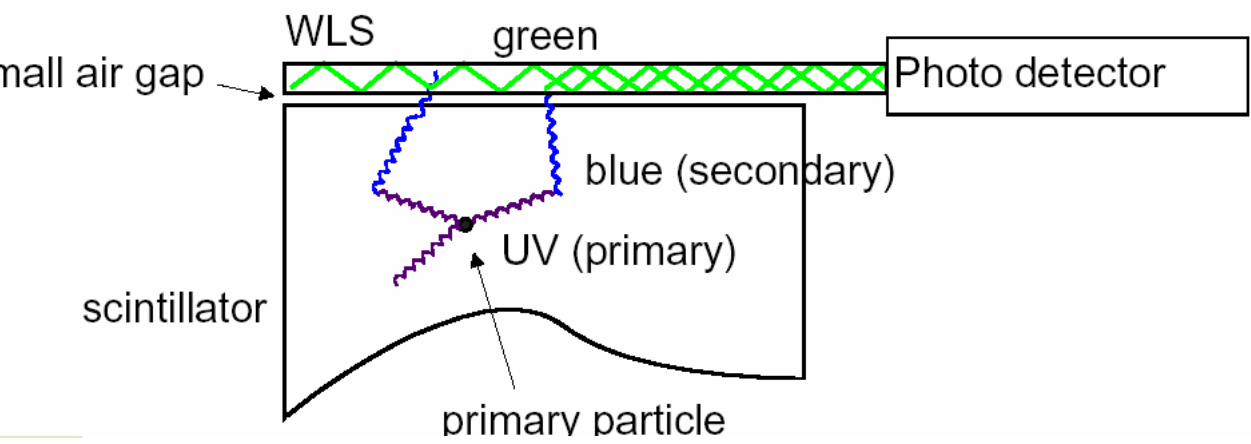
- ◆ **Guide di luce :**
  - riflessione interna totale



**“fish tail”**

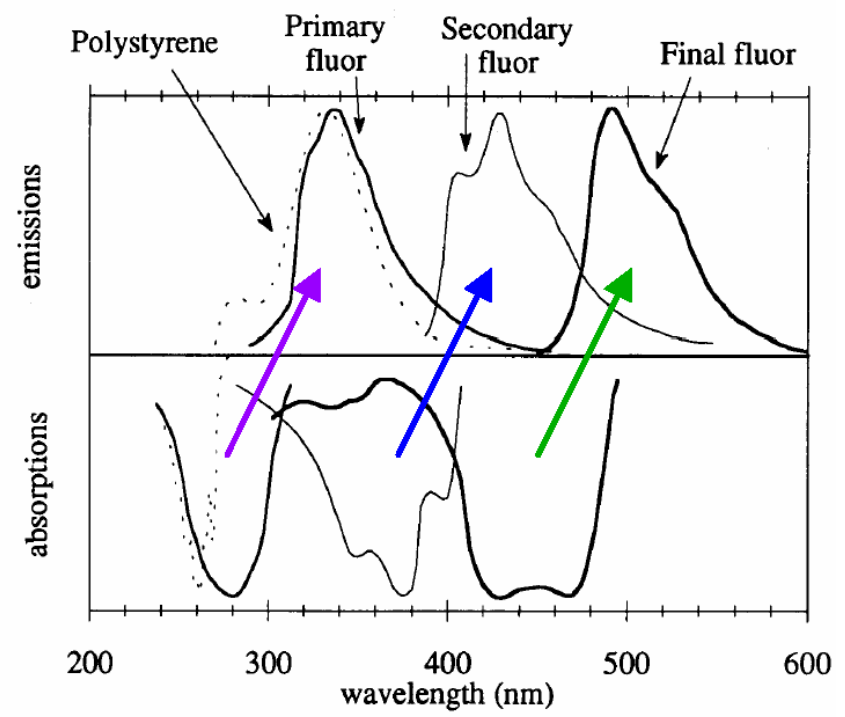


**adiabatic**



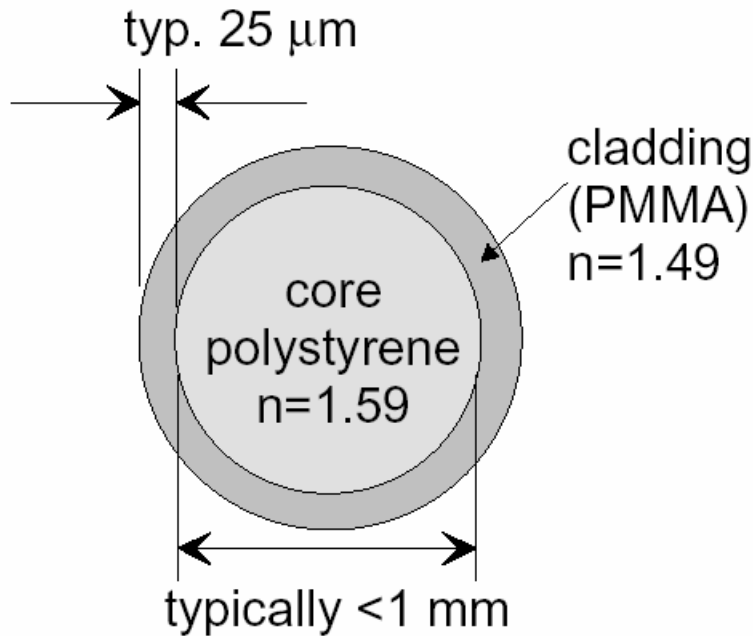
Schematic representation of wave length shifting principle

(C. Zorn, Instrumentation In High Energy Physics, World Scientific, 1992)

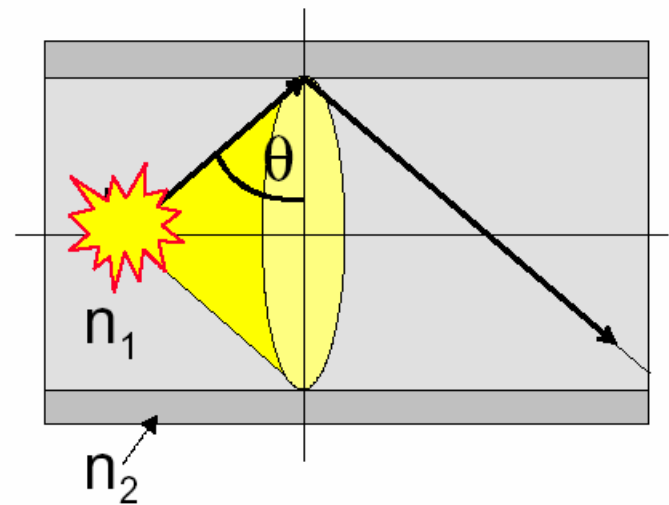




## ◆ Optical fibers



light transport by total internal reflection



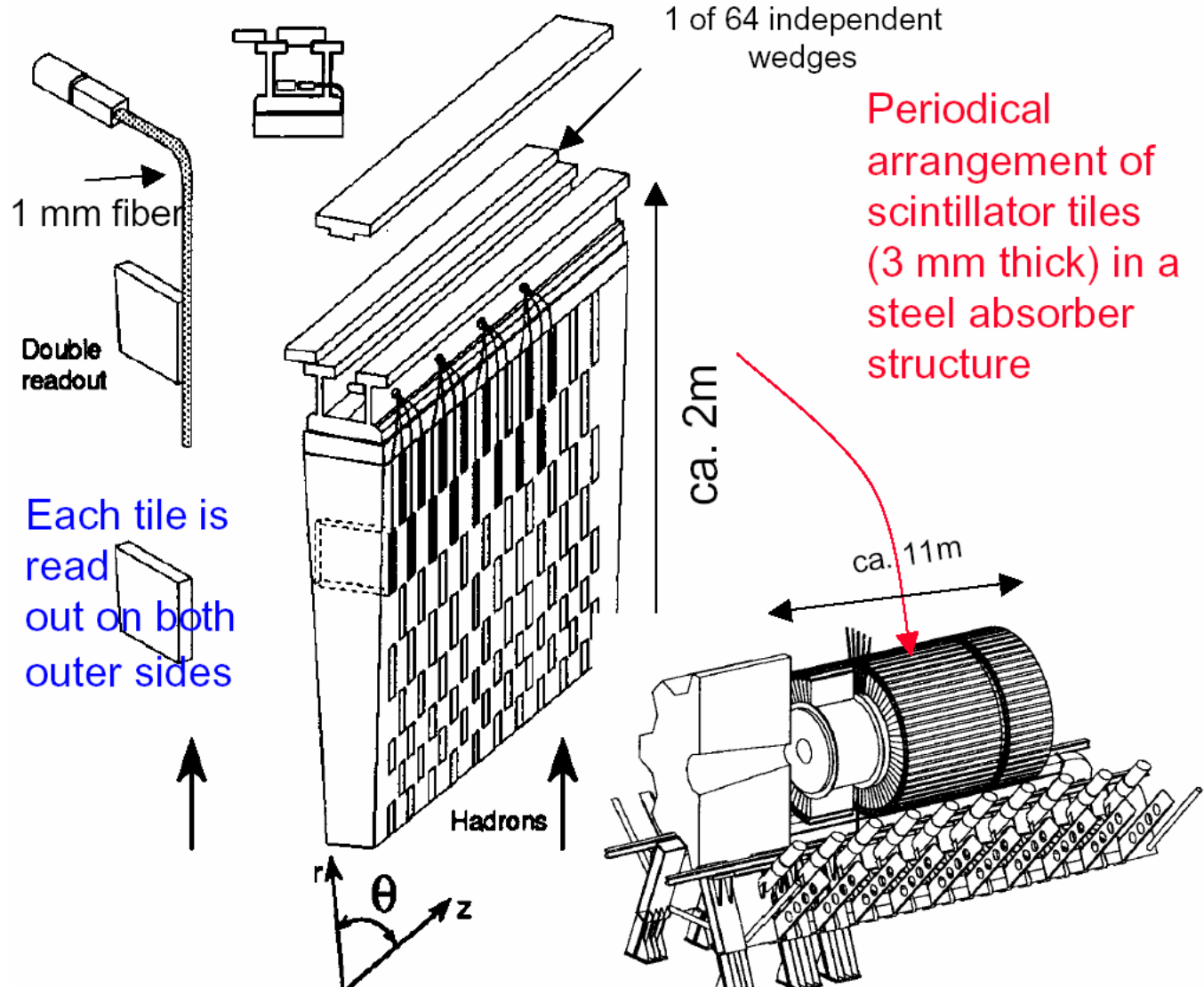
$$\theta \geq \arcsin \frac{n_2}{n_1} \approx 69.6^\circ$$

$$\frac{d\Omega}{4\pi} = 3.1\% \quad \text{in one direction}$$

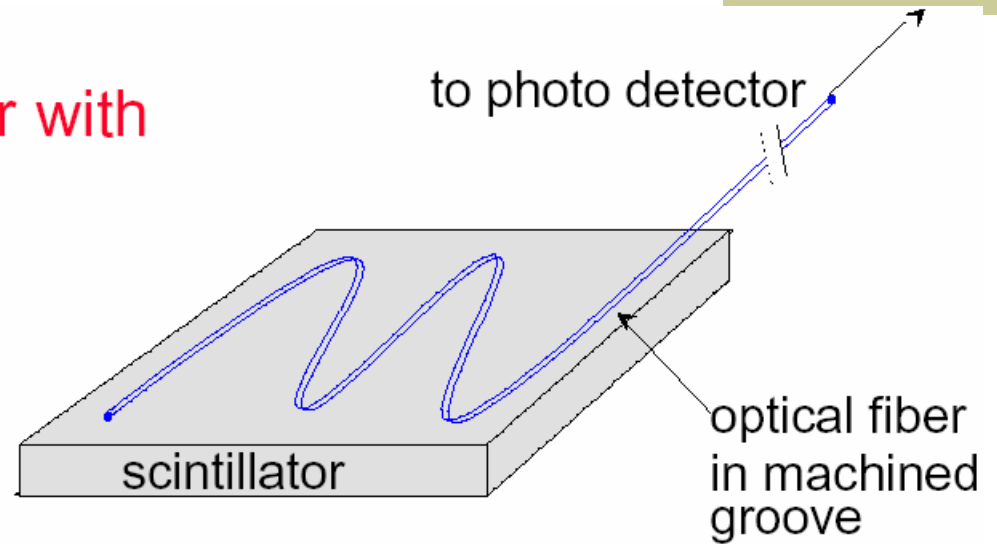
minimize  $n_{\text{cladding}}$ .

Ideal: air ( $n=1$ ), but impossible due to surface imperfections

# Calorimetro adronico di ATLAS



readout of a scintillator with  
a fiber (schematically)

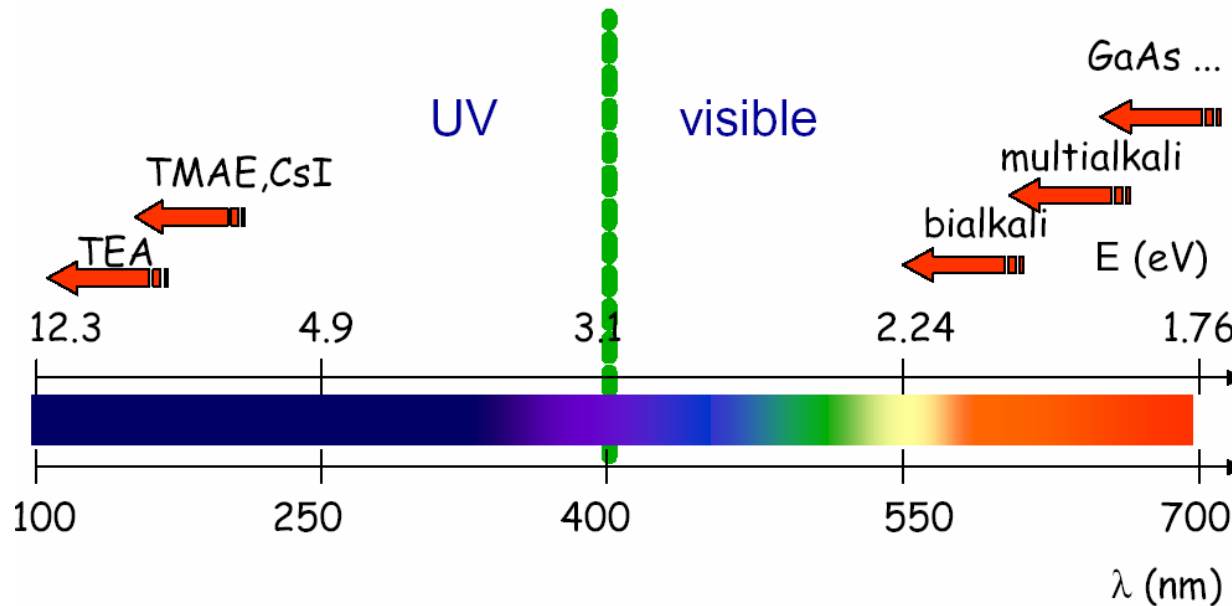


# Photo Detectors

**Purpose:** Convert light into detectable electronics signal

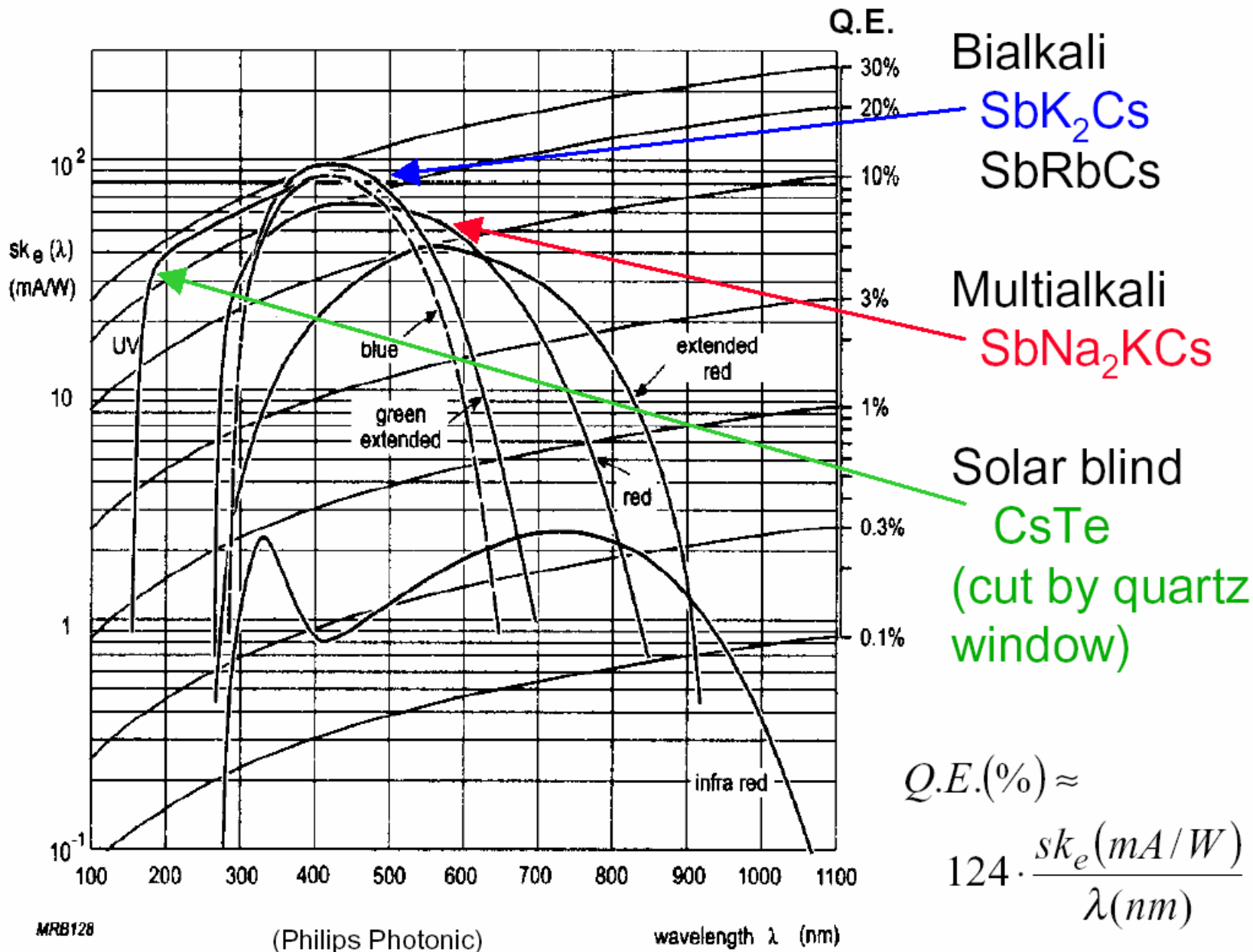
**Principle:** Use Photoelectric Effect to convert photons to photoelectrons

Threshold of some photosensitive material

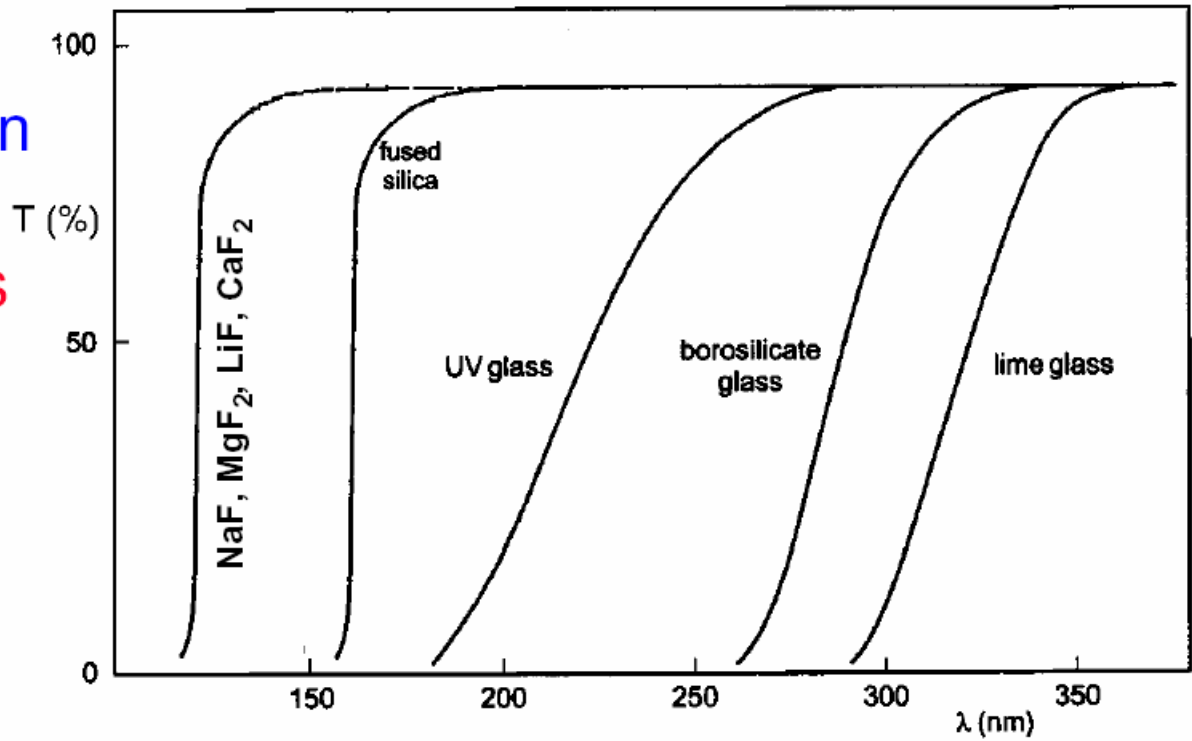


**standard requirement**

- high sensitivity, usually expressed as quantum efficiency  $Q.E. = N_{p.e.} / N_{photons}$



Transmission  
of various  
PM windows



# Photo Multiplier Tube (PMT)

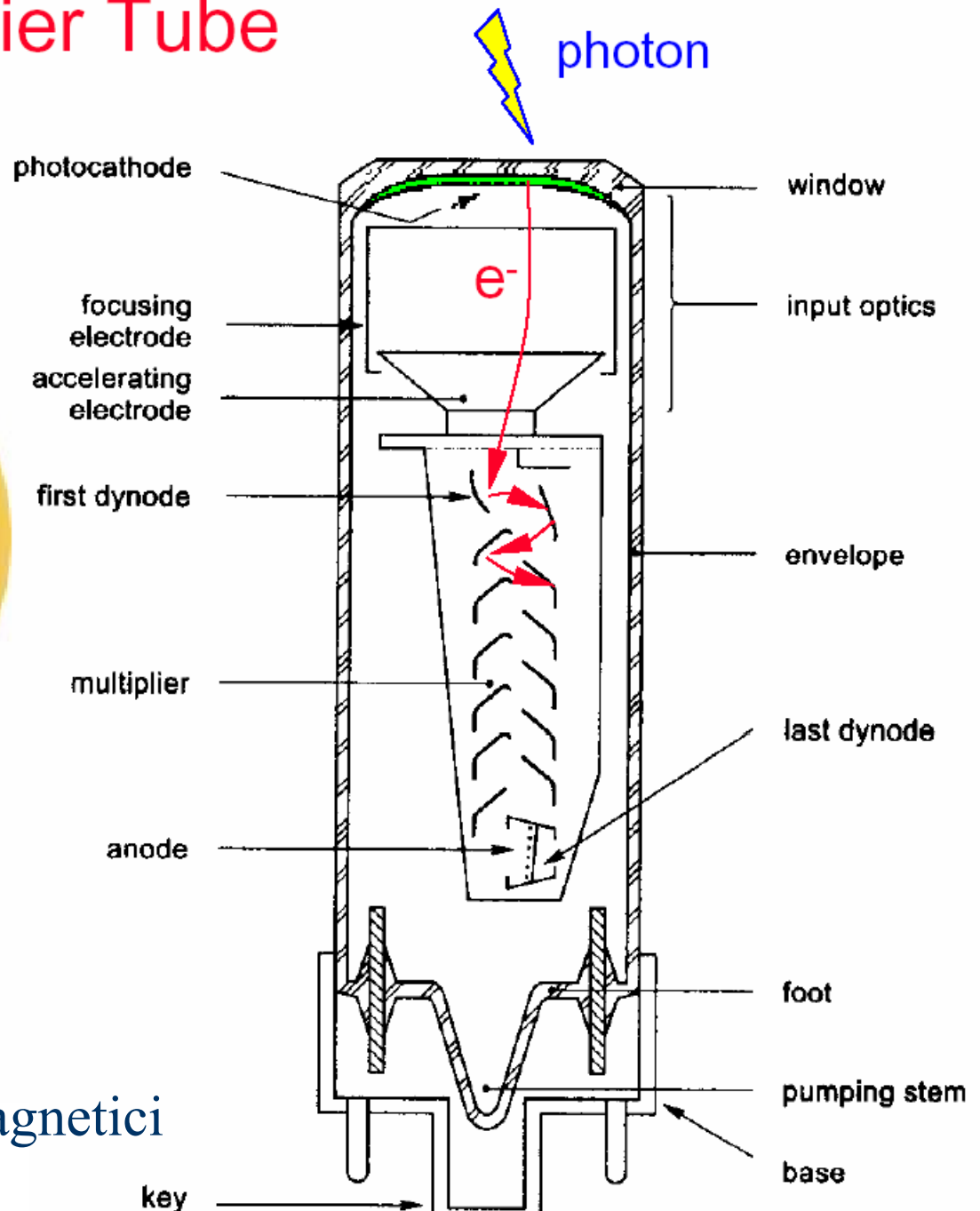


(Philips  
Photonic)

Guadagni  $\sim 10^6$

Sensibili a campi magnetici

Mu-shield



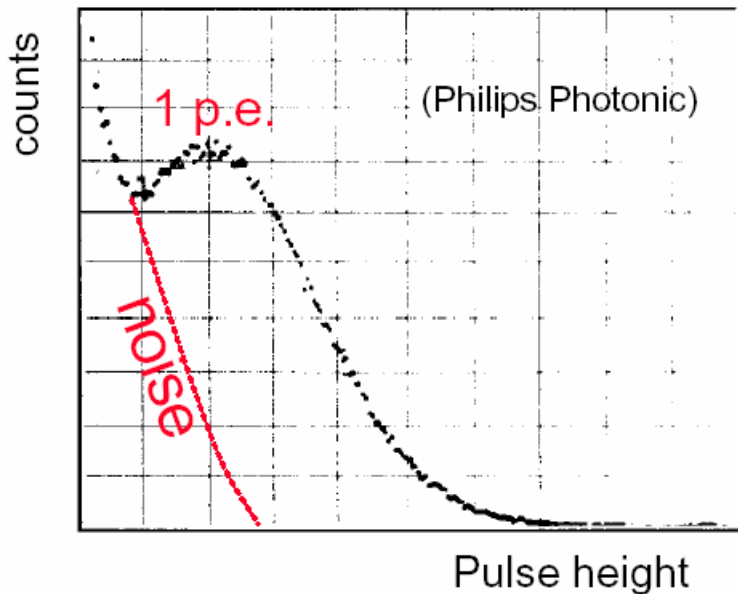
# RISOLUZIONE ENERGETICA dei PMT

determinata principalmente dalle fluttuazioni del numero di elettroni secondari dai dinodi

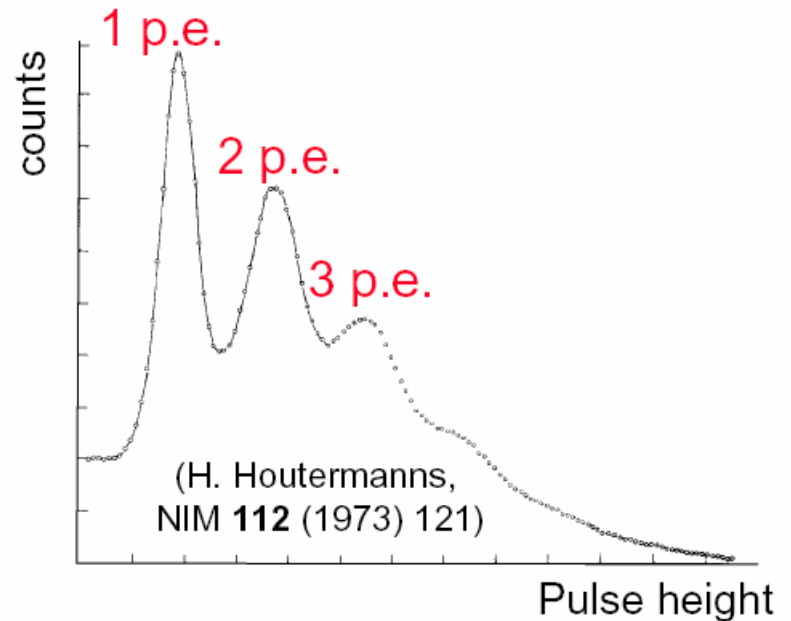
$$\text{Poisson distribution: } P(\bar{n}, m) = \frac{\bar{n}^m e^{-m}}{m!}$$

$$\text{Relative fluctuation: } \frac{\sigma_n}{\bar{n}} = \frac{\sqrt{\bar{n}}}{\bar{n}} = \frac{1}{\sqrt{\bar{n}}}$$

Single photons.  
Pulse height spectrum of a PMT with Cu-Be dynodes.



Pulse height spectrum of a PMT with NEA dynodes.





## ◆ Hybrid photo diodes (HPD)

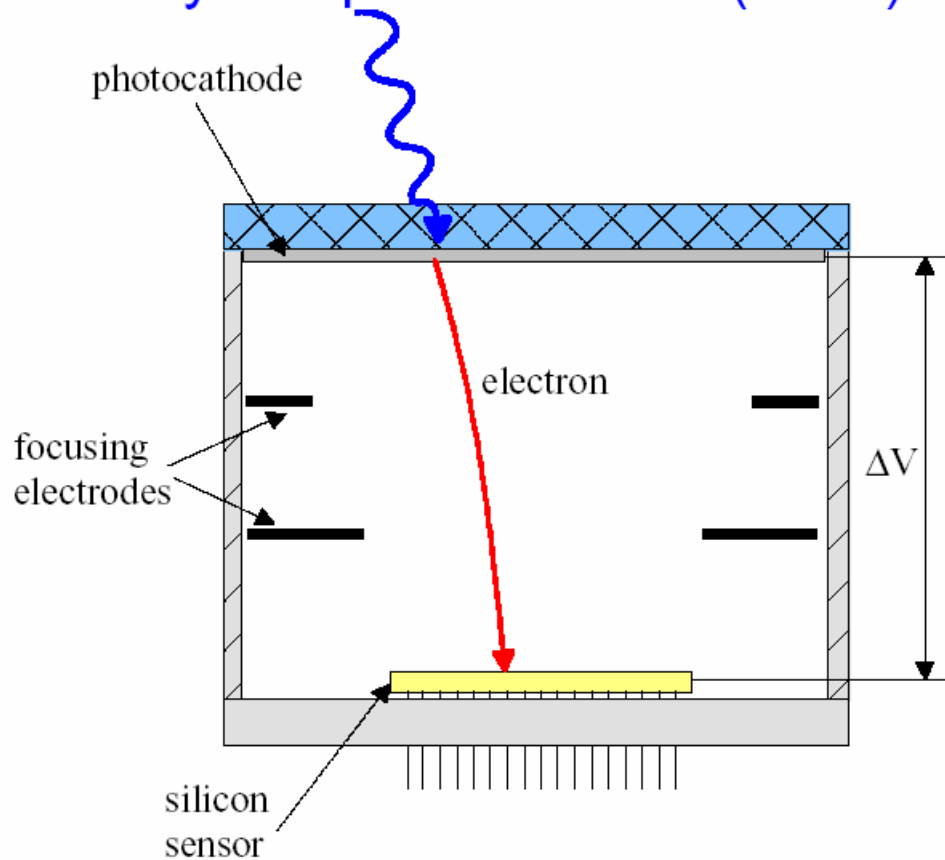


photo cathode + p.e.  
acceleration + silicon  
det. (pixel, strip, pads)

Photo cathode like in PMT,  $\Delta V$  10-20 kV

$$G = \frac{e\Delta V}{W_{Si}} = \frac{20 \text{ keV}}{3.6 \text{ eV}} \approx 5 \cdot 10^3 \quad (\text{for } \Delta V = 20 \text{ kV})$$

# Single photon detection with high resolution

Poisson statistics  
with  $\bar{n} = 5000$  !

Background from  
electron backscattering  
from silicon surface

