Experimental techniques in high-energy nuclear and particle physics

"Dottorato di Ricerca in Ingegneria dell'Informazione"

LECTURE 3.

Accelerators - 2

Prof. Rino Castaldi INFN-Pisa

rino.castaldi@pi.infn.it

Accelerators and LHC experiments at CERN



The energies in the CERN accelerators range from 100 keV to soon 7 TeV

(now at 3.5 TeV).

 To do this the beam energy is increased in a staged way using
 5 different accelerators.

> Energies: Linac 50 MeV PSB 1.4 GeV PS 28 GeV SPS 450 GeV LHC 7 TeV (now 3.5TeV)



The CERN Large Hadron Collider

first collisions in Autumn 2009



9300 Superconductor magnets 1232 Dipoles (15m, 1.9°K) 8.4Tesla 11700 A 448 Main Quads, 6618 Correctors. Circonference 26.7 km











Basic concepts







⇒ A particle, with a constant energy, describes a circle in equilibrium between the centripetal magnetic force and the centrifugal force



TRANSVERSE BEAM DYNAMICS

◆ LEP vs LHC magnets (in same tunnel) ⇒ A change in technology

	LEP	LHC
ρ [m]	3096.175	2803.95
<i>p</i> ₀ [GeV/c]	104	7000
<i>B</i> [T]	0.11	8.33
	1	
Room-temperature coils		Superconducting coils









Two particles in a dipole field

✓ What happens with two particles that travel in a dipole field with different initial angles, but with equal initial position and equal momentum ?

Particle A

- Particle B

✓ Assume that Bp is the same for both particles.
✓ Lets unfold these circles.....

The 2 trajectories unfolded

✓ The horizontal displacement of particle B with respect to particle A.



- ✓ Particle B oscillates around particle A.
- ✓ This type of oscillation forms the basis of all transverse motion in an accelerator.
- ✓ It is called 'Betatron Oscillation'

The mechanical equivalent

The gutter below illustrates how the particles in our accelerator behave due to the quadrupolar fields.

✓ Whenever a particle beam diverges too far away from the central orbit the quadrupoles focus them back towards the central orbit.

> How can we represent the focusing gradient of a quadrupole in this mechanical equivalent ?





A Quadrupole has 4 poles,
2 north and 2 south



- They are symmetrically arranged around the centre of the magnet
- ✓ There is no magnetic field along the central axis.





Quadrupole (LEP)







Transverse focusing is achieved with **quadrupole** magnets, which act on the beam like an optical lens.

Linear increase of the magnetic field along the axes (no effect on particles on axis).

Focusing in one plane, **de-focusing** in the other!

S. Redaelli, LPCC lectures, 07/09-04-2010



R. Steerenberg, 28-Jan-2008

Focusing and Stable motion

- Using a combination of focusing (QF) and defocusing (QD) quadrupoles solves our problem of 'unstable' vertical motion.
- ✓ It will keep the beams focused in both planes when the position in the accelerator, type and strength of the quadrupoles are well chosen.
- ✓ By now our accelerator is composed of:
 - <u>Dipoles</u>, constrain the beam to some closed path (orbit).
 - Focusing and Defocusing Quadrupoles, provide horizontal and vertical focusing in order to constrain the beam in transverse directions.
- ✓ A combination of focusing and defocusing sections that is very often used is the so called: <u>FODO lattice</u>.
- This is a configuration of magnets where focusing and defocusing magnets alternate and are separated by nonfocusing drift spaces.

FODO cell

✓ The 'FODO' cell is defined as follows:





Alternating gradient lattice





One can find an arrangement of quadrupole magnets that provides net focusing in both planes ("strong focusing").

Dipole magnets keep the particles on the circular orbit.

Quadrupole magnets focus alternatively in both planes.

S. Redaelli, LPCC lectures, 07/09-04-2010

The particle characterized

✓ A particle during its transverse motion in our accelerator is characterized by:

x = displacement

ds

dx

x' = angle = dx/ds

- <u>Position</u> or displacement from the central orbit.
- Angle with respect to the central orbit.

✓ This is a motion with a <u>constant restoring force</u>, like in the first lecture on differential equations, with the <u>pendulum</u>

AXEL - 2008

X

TRANSVERSE BEAM DYNAMICS (6/27)

QUADRUPOLE = Focusing magnet



In *x* (and Defocusing in *y*) ⇒ F-type. Permutating the N- and S- poles gives a D-type

Linear force in x&y

$$\Rightarrow x''(s) + K x(s) = 0 : \mathbf{E}$$

Equation of a harmonic oscillator

 From this equation, one can already anticipate the elliptical shape of the particle trajectory in the phase space (x, x') by integration

$$x'^{2}(s) + K x^{2}(s) = \text{Constant}$$

Hill's equation (2)

✓ In a real accelerator K varies strongly with 's'.
 ✓ Therefore we need to solve Hill's equation for K varying as a function of 's'

$$\frac{d^2x}{ds^2} + K(s)x = 0$$

- ✓ Remember what we concluded on the mechanical equivalent concerning the shape of the gutter.....
 - ✓ The phase advance and the amplitude modulation of the oscillation are determined by the shape of the gutter.
 - ✓ The overall <u>oscillation amplitude</u> will depend on the <u>initial</u> <u>conditions</u>, I.e. how the motion of the ball started.

Solution of Hill's equation (1)

$$\frac{d^2x}{ds^2} + K(s)x = 0$$

- ✓ This is a 2nd order differential equation.
- ✓ In order to solve it lets try to guess a solution:

 $x = \sqrt{\varepsilon \cdot \beta(s)} \cos(\phi(s) + \phi_0)$

- \checkmark $\beta(s)$ = the <u>amplitude modulation</u> due to the changing focusing strength.
- \$\phi(s)\$ = the phase advance, which also depends on focusing strength.

TRANSVERSE BEAM DYNAMICS





$x = \sqrt{\varepsilon \cdot \beta(s)} \cos(\phi(s) + \phi_0)$

- ✓ $\beta(s)$ = the <u>amplitude modulation</u> due to the changing focusing strength.
- \checkmark $\phi(s)$ = the phase advance, which also depends on focusing strength.
- \checkmark ε and ϕ_0 are constants, which depend on the <u>initial conditions</u>.

Hill's equation

- The <u>betatron oscillations</u> exist in both horizontal and vertical planes.
- ✓ The number of betatron oscillations per turn is called the <u>betatron tune</u> and is defined as <u>Qx</u> and <u>Qy</u>.
- ✓ Hill's equation describes this motion mathematically

$$\frac{d^2x}{ds^2} + K(s)x = 0$$

✓ If the restoring force, K is constant in 's' then this is just a <u>Simple Harmonic Motion</u>.

Matrix Formalism

 Lets represent the particles transverse position and angle by a column matrix.

- As the particle moves around the machine the values for x and x' will vary under influence of the dipoles, quadrupoles and drift spaces.
- These modifications due to the different types of magnets can be expressed by a <u>Transport Matrix M</u>
- ✓ If we know x_1 and x_1' at some point s_1 then we can calculate its position and angle after the next magnet at position S_2 using:

$$\binom{x(s_2)}{x(s_2)'} = M\binom{x(s_1)}{x(s_1)'} = \binom{a}{c} \begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} x(s_1) \\ x(s_1)' \end{pmatrix}$$

How to apply the formalism

✓ If we want to know how a particle behaves in our machine as it moves around using the matrix formalism, we need to:

 Split our machine into separate element as dipoles, focusing and defocusing quadrupoles, and drift spaces.

- Find the matrices for all of these components
- ✓ Multiply them all together
- Calculate what happens to an individual particle as it makes one or more turns around the machine

Matrix for a drift space

✓ A <u>drift space</u> contains <u>no magnetic field</u>.
✓ A <u>drift space</u> has <u>length L</u>.

 X_1



$$x_{1}' \text{ small}$$

$$x_{2} = x_{1} + Lx_{1}'$$

$$x_{2}' = 0 + x_{1}'$$

$$x_{2}' = 0 + x_{1}'$$

$$x_{2}' = 0 + x_{1}'$$

R. Steerenberg, 29-Jan-2008

Matrix for a quadrupole deflection ✓ A quadrupole of length L. X_1 X_2 X_1' X_2 Remember $B_v \propto x$ and the deflection due to the magnetic field is: $\frac{LB_y}{(B\rho)} = -\frac{LK}{(B\rho)} \cdot x$

Provided L is small





Matrix for a quadrupole (2)

✓ We found :

$$\begin{pmatrix} x_2 \\ x_2' \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ -\frac{LK}{(B\rho)} & 1 \end{pmatrix} \begin{pmatrix} x_1 \\ x_1' \end{pmatrix}$$

✓ Define the focal length of the quadrupole as $f = \frac{(B\rho)}{KL}$

$$\begin{pmatrix} x_2 \\ x_2 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ -\frac{1}{f} & 1 \end{pmatrix} \begin{pmatrix} x_1 \\ x_1 \end{pmatrix}$$

How now further?

- For our purpose we will treat dipoles as simple drift spaces as they bend all the particles by the same amount.
- ✓ We have <u>Transport Matrices</u> corresponding to <u>drift spaces</u> and <u>quadrupoles</u>.
- These matrices describe the real discrete focusing of our quadrupoles.
- ✓ Now we must <u>combine these matrices with</u> our solution to <u>Hill's equation</u>, since they describe the same motion.....

A quick recap.....

✓ We solved <u>Hill's equation</u>, which led us to the definition of <u>transverse emittance</u> and allowed us to describe particle motion in <u>phase space</u> in terms of β , α etc...

✓ We constructed the <u>Transport Matrices</u> corresponding to <u>drift spaces</u> and <u>guadrupoles</u>.

✓ Now we must <u>combine</u> these <u>matrices</u> with the solution of <u>Hill's equation</u> to evaluate β , α etc

Matrices & Hill's equation

- ✓ We can multiply the matrices of our drift spaces and quadrupoles together to form a transport matrix that describes a larger section of our accelerator.
- ✓ These matrices will move our particle from one point $(x(s_1),x'(s_1))$ on our phase space plot to another $(x(s_2),x'(s_2))$, as shown in the matrix equation below.

$$\begin{pmatrix} x(s_2) \\ x'(s_2) \end{pmatrix} = \begin{pmatrix} a & b \\ c & d \end{pmatrix} \cdot \begin{pmatrix} x(s_1) \\ x'(s_1) \end{pmatrix}$$

✓ The elements of this matrix are fixed by the elements through which the particles pass from point s_1 to point s_2 .

✓ However, we can also express (x,x') as solutions of Hill's equation.

$$x = \sqrt{\varepsilon \cdot \beta} \cos \phi$$
 and $x' = -\alpha \sqrt{\varepsilon \cdot \beta} \cos \phi - \sqrt{\varepsilon \cdot \beta} \sin \phi$

1n Ø

Chromaticity

 The chromaticity relates the tune spread of the transverse motion with the momentum spread in the beam.











$$Q' = \frac{\Delta Q}{\Delta p / p}$$

Particles with different energies have different betatron tunes.

Bad for the beam:

- Adds a tune spread
- Instabilities ("head-tail")

Focusing error from momentum errors ~ -*K* Δ*p/p*

Chromaticity corrections is done with **sextupole** magnets. The field changes as x^2 .

LHC:

2 sextupole families per plane per beam for chromaticity correction.



Sextupole Magnets



- Conventional Sextupole from LEP, but looks similar for other 'warm' machines.
- ~ 1 meter long and a few hundreds of kg.

- ✓ Correction Sextupole of the LHC
- ✓ 11cm, 10 kg, 500A at 2K for a field of 1630 T/m²

R. Steerenberg, 29-Jan-2008





Machine imperfections



The Q-value gives the number of oscillations the particles make in one turn. If this value in an integer, the beam "sees" the same magnet-error over and over again and we may have a resonance phenomenon. (Resonance) Therefore the Q-value is not an integer.

The magnets have to be good enough so that resonance phenomena do not occur.

Q = 3.333 in more detail

1st turn

2nd turn

3rd turn

Third order resonant betatron oscillation 3Q = 10, Q = 3.333, q = 0.333

Q = 3.333 in Phase Space

/ Third order resonance on a normalised phase space plot


Machine Imperfections

- There are many things in our machine, which will excite resonances:
 - The magnets themselves
 - Unwanted higher order field components in our magnets
 - ✓ Tilted magnets
 - Experimental solenoids (LHC experiments)
- ✓ The trick is to reduce and compensate these effects as much as possible and then find some point in the tune diagram where the beam is stable.



 \hat{y}, \hat{x}

I€





Betatron phase advance over 1 turn:



-turn

Betatron tune:

0.45

0.4

0.35

0.3

0.2

0.15

0.1

0.05

0

0.05

0.1

0.15

0.2

 Q_y 0.25



(0.31, 0.32)

0.3

 \mathcal{Q}_x

0.35

0.4

0.45

0.5

0.25

S

 $nQ_x + mQ_y = p$

The tune is the **number of betatron oscillations per turn**.

We *normally* only care about the **fractional part** of the tune! 64.31 is 0.31!

The operating tune values (working point) must be chosen to avoid resonance.

The tune values must be controlled to within better than 10⁻³, during all machine phases (ramp, squeeze, ...)

Acceleration Concepts

• Lorentz Force: $\frac{dp}{dt} = q \cdot \left(\vec{E} + \vec{v} \times \vec{B}\right)$

energy gain only due to electric fields!

Scalar and Vector Potential:

$$\vec{E} = -grad\phi - \frac{1}{c}\frac{\partial \vec{A}}{\partial t}$$

Electrostatic acceleration $\longrightarrow A = 0$ Acceleration with time varying fields $\longrightarrow \phi = 0$







Acceleration is performed with electric fields fed into **Radio-Frequency (RF) cavities**. RF cavities are basically resonators tuned to a selected frequency.

In circular accelerators, the acceleration is done with small steps at each turn.

LHC: 8 RF cavities per beam (400 MHz), located in point 4

At the LHC, the acceleration from **450 GeV** to **7 TeV** lasts ~ 20 minutes (nominal!), with an average energy gain of ~ 0.5 MeV on each turn.

[Today, we ramp at a factor 4 less energy gain per turn than nominal!]



RF Cavities



LEP cavities





LHC Superconductive cavities

Acceleration or compensation

- We have to provide energy to the particles either to accelerate them or to compensate for the losses accumulated during one turn.
- This energy is not provided by electrostatic plates, but by RF cavities.
- The ideal particle has to arrive at the cavity exactly at the same moment turn after turn (synchroneous particle).





CAS Bruges 16-25 June 2009

Beam Dynamics



LONGITUDINAL BEAM DYNAMICS (3/12)

TRANSITION ENERGY: The increase of energy has 2 contradictory effects

- An increase of the particle's velocity
- An increase of the length of the particle's trajectory

According to the variations of these 2 parameters, the revolution frequency evolves differently

- Below transition energy: The velocity increases faster than the length => The revolution frequency increases
- Above transition energy: It is the opposite case ⇒ The revolution frequency decreases
- At transition energy: The variation of the velocity is compensated by the variation of the trajectory => A variation of energy does not modify the frequency

Transition

- # Lets look at the behaviour of a particle in a constant magnetic field.
- # Low momentum ($\beta << 1, \gamma \Rightarrow 1$)
- # The revolution frequency increases as momentum increases
- # <u>High momentum</u> ($\beta \approx 1, \gamma >> 1$) —
- # The revolution frequency decreases as momentum increases
- # For one particular momentum or energy we have:

$$\frac{1}{\gamma^2} = \alpha_p$$

This particular energy is called the **Transition energy**

A Single particle in a longitudinal electric field (below transition)

Lets see what a low energy particle does with this oscillating voltage in the cavity.



Set the oscillation frequency so that the period is exactly equal to one revolution period of the particle.

Add a second particle to the first one

Lets see what a second low energy particle, which arrives later in the cavity, does with respect to our first particle.





1st revolution period



100st revolution period







500st revolution period







800st revolution period



900st revolution period

Synchrotron Oscillations



900st revolution period

Particle B has made 1 full oscillation around particle A.
The amplitude depends on the initial phase.

Exactly like the pendulum

We call this oscillation:

Synchrotron Oscillation

Rende Steerenberg, 30-Jan-2008

What happens beyond transition?

Until now we have seen how things look like below transition

Higher energy \Rightarrow faster orbit \Rightarrow higher $F_{rev} \Rightarrow$ next time particle will be earlier. Lower energy \Rightarrow slower orbit \Rightarrow lower $F_{rev} \Rightarrow$ next time particle will be later.

What will happen above transition ?

Higher energy \Rightarrow longer orbit \Rightarrow lower $F_{rev} \Rightarrow$ next time particle will be later. \checkmark Lower energy \Rightarrow shorter orbit \Rightarrow higher $F_{rev} \Rightarrow$ next time particle will be earlier.

Rende Steerenberg, 30-Jan-2008 AXEL - 2008

Off momentum particles (above transition)



On momentum particle arrives at $t_0 \rightarrow V = V_0 \rightarrow o.k$. $\Delta p/p > 0$ have a longer path \rightarrow arrive late, e.g. $t_2 \rightarrow V_2 < V_0$ $\Delta p/p < 0$ have a shorter path \rightarrow arrive early, e.g. $t_1 \rightarrow V_1 > V_0$



What are the implication for the RF?

For particles below transition we worked on the <u>rising edge</u> of the sine wave.

For Particles above transition we will work on the <u>falling edge</u> of the sine wave.



Buckets and bunches





Sincrotron acceleration



Bunch

Examples

CERN PS, SPS, SPPbarS, LEP, LHC FERMILAB **TEVATRON** DESY **HERA** SLAC SLC, PEP II



Operation

- 1985 now, FERMILAB, Chicago
- Circumference 4 miles
- Particles
 protons antiprotons
- Beam energy 0.9 TeV → 1 TeV
- Luminosity 10³⁰ - 10³² cm⁻² sec⁻¹
- L_{int} Run Ia+Ib : 110 pb⁻¹
- Experiments CDF, DØ
- Characteristics:
 - `dirty' environment (see LHC later)
 - high interaction rate

FERMILAB'S ACCELERATOR CHAIN

Fermilab from the air







Acceleratori



HERA

- Operation

 1992 now,
 DESY, Hamburg
- Circumference
 6.3 km
- Particles electrons (or positrons) - protons
- Beam energy
 e = 28 GeV , protons = 820 GeV
- Luminosity about 2x10³¹ cm⁻² sec⁻¹
 - L_{int} up to now : about 180 pb⁻¹
- Experiments
 H1, ZEUS, HERA-b, HERMES
- Characteristics:
 - only lepton-hadron collider
 - superconducting magnets for proton ring

HERA - Electron Proton Collider (6.3 km)













- Operation
 1989 2000, CERN, Geneva
- Circumference
 27 km
- Particles
 electrons positrons
- Beam energy 45 GeV → 104.5 GeV
- Luminosity 10³¹ - 10³² cm⁻² sec⁻¹
- L_{int} ⊮1000 pb⁻¹
- Experiments ALEPH, DELPHI, L3, OPAL
- Characteristics:
 - very clean environment
 - very small backgrounds
Collisions at LHC



2835 bunch/beam Proton-Proton 10¹¹ Protons/bunch Beam energy

Luminosity

7 TeV (7x10¹² eV) 10³⁴ cm⁻² s⁻¹

Crossing rate 40 MHz

Collisions rate ≈ 10⁷ - 10⁸Hz

New physics rate \approx .00001 Hz

Event selection: 1 in 10,000,000,000,000

LEP vs LHC: Magnets, a change in technology Bending Field $\rightarrow p(TeV) = 0.3 B(T) R(Km)$ (earth magnetic field is between 24,000 nT and 66,000 nT)

Tunnel R \approx 4.3 Km LHC 7 TeV \rightarrow B \approx 8.3 T \rightarrow <u>Superconducting coils</u> LEP 0.1 TeV \rightarrow B \approx 0.1 T \rightarrow Room temperature coils



Protons can go up in energy more than electrons because they **emit less synchrotron radiation.** Bending (dipoles) and focusing (quadrupoles) strengths require high magnetic fields generated by superconductors

Accelerators and LHC experiments at CERN







The LHC arcs





392 main quadrupoles + 2500 corrector magnets

MCS: Sextupole corrector (b3)

MCDO: Assembly of spool correctors consists of an octupole insert MCO (b4) and a decapole magnet MCD (b5)

MQT: Trim quarupole corrector MS: arc sextupole corrector

MQS: skew quad lattice corrector

MCBH: Horizontal dipole corrector

MCBV: Vertical dipole corrector

MO: Lattice octupole



RF - tunnel view







Bottle of Hydrogen, to start with!





The real bottle is inside the cage





Linac2: some pictures







Downstream of Linac2, the proton beams will only encounter **circular accelerators** (and transfer lines)





CERN Control Centre - Layout





MORE SLIDES

Synchrotron radiation

Radiation emitted by charged particles accelerated longitudinally and/or transversally

Power radiated per particle goes like:

 $\mathbf{0}$ $\mathbf{\nabla}^4$

4th power of the energy (2nd power)⁻¹ of the bending radius (4th power)⁻¹ of the particle mass

Energy lost per turn per particle due to synchrotron radiation:

- e- W(MeV) = 8.85 x 10^{-5} x E⁴(GeV)/ ρ^2 (km) ≈ 2 GeV (LEP)
- $P = W(keV) = 7.8 \times 10^{-3} \times E^4(TeV)/\rho^2(km) \approx 6 \text{ keV}$ (LHC)

We must protect the LHC coils even if energy per turn is so low



Power lost per m in dipole: <u>0.206 W</u> Total radiated power per ring: <u>3.6 kW</u>





Inside one cell







LHC design parameters



Nominal LHC parameters				
Beam injection energy (TeV)	0.45			
Beam energy (TeV)	7.0			
Number of particles per bunch	1.15 x 10 ¹¹			
Number of bunches per beam	2808			
Max stored beam energy (MJ)	362			
Norm transverse emittance (µm rad)	3.75			
Colliding beam size (µm)	16			
Bunch length at 7 TeV (cm)	7.55			











Relative beam sizes around IP1 (Atlas) in collision







Delivered beam current: Beam energy: Repetition rate: Radio-frequency system:

~150mA 90 keV (source) \rightarrow 750 keV (RFQ) \rightarrow 50 MeV 1 Hz 202 MHz



PS Booster







Sketch of the PS Booster with: - Distribution of Linac beam into 4 rings - Recombination prior to transfer

- Constructed in the 70ies to increase the intensity into the PS
- Made of four stacked rings
- Acceleration to E_{kin}=1.4 GeV
- Intensities > 10¹³ protons per ring obtained (i.e., four times design!!)
- Several types of beams with different characteristics
- → Physics beams for ISOLDE
- → Beams for AD/PS/SPS physics



Proton Synchrotron





from Thursday 03 December 2009 at 14:00 to Friday 04 December 2009 at 17:00 (Europe/Zurich) at CERN (500-1-001 - Main Auditorium)







Nominal LHC beams at the SPS





Da -1.70e+04 0.00 dy 2132.53

Injectors have been since long ready for the nominal LHC...

91







Courtesy of J. Uythoven









500 0mW/dw = 930 655. HILMAG-11000 N1-D-A5 500 0mW/dw = 720 524.

HIX2.MIN PREPULSE.

Out/div

HI2INJ-BEAM-AS 10.0mV/cM S0.218 m/

NO 11108

2 07 + L III2.014G-CIIRRENT-A-A5 5 00.0197/018 -1.2017

Extensively tested during TI2/8 commissioning and sector tests:

- synchronization of kickers with extracted beam
- steering of the transfer lines
- protection settings
- injection quality checks

ŵ

OASIS VIEWER

R, 10

Beam1

DHC: UK

File General Scopel Scopel Scopel Help

🔤 🔚 🛯 🖉 🖉 🖉 🖉 🌑

Beam₂



Injection elements





TED TI2 position:	BEAM	TDI P2 gaps/mm	up: 9.05	down: 9.04
TED TI8 position:	BEAM	TDI P8 gaps/mm	up: 8.32	down: 8.36



Beam dump (IP6)





Interaction region layout







With more than 154 bunches, we need a crossing angle to avoid parasitic collisions outside the IP.
Beams are separated in the other plane during injection and ramp

$$\mathcal{L} = \frac{N^2 n_b f_{\text{rev}}}{4\pi\sigma_x \sigma_y} F$$

$$F = \frac{1}{\sqrt{1 + \left(\frac{\theta_c \sigma_z}{2\sigma^*}\right)^2}}$$

Luminosity: the beam size

We need a small beam in the collision point





S. Redaelli, LPCC lectures, 07/09-04-2010



Beam envelope



