

# Time-dependent CP Violation Measurements from Belle

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representing the  
**Belle Collaboration**

Les Rencontres de Physique de la Vallée d'Aoste  
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$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \sim \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

where  $A, \lambda, \rho, \eta$  are Wolfenstein parameters

From unitarity ( $V_{CKM}^* V_{CKM} = 1$ ):

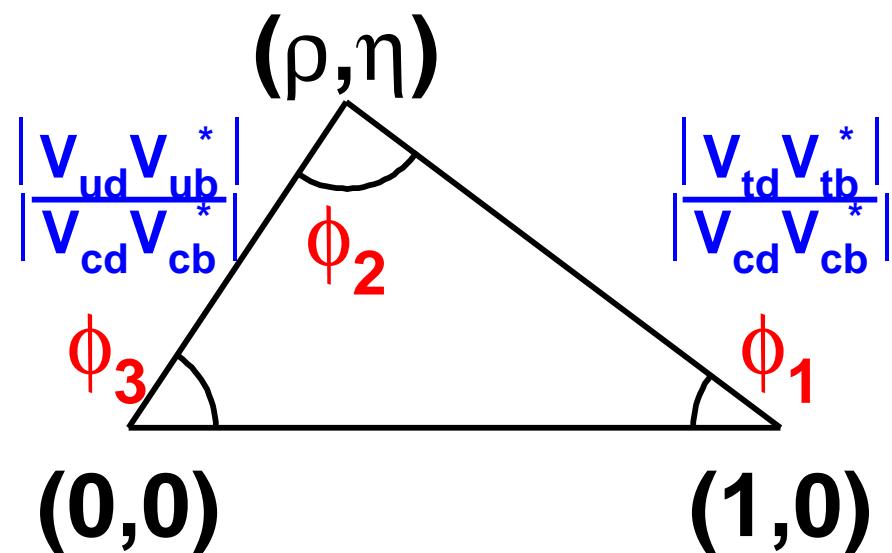
$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

## The Unitarity Triangle

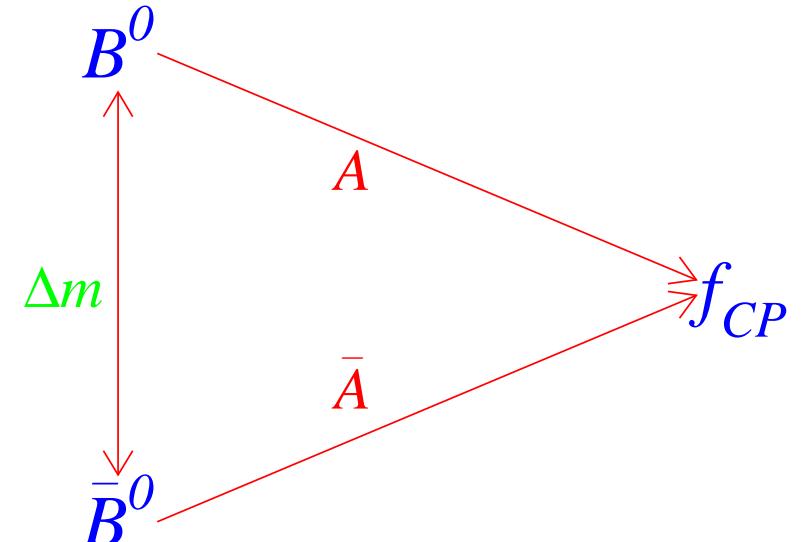
$$\phi_1 \leftrightarrow \beta$$

$$\phi_2 \leftrightarrow \alpha$$

$$\phi_3 \leftrightarrow \gamma$$



- Interference between different paths to a final state  $\Rightarrow$  time-dependent CP violation
- Consider  $B^0/\bar{B}^0$  decaying to a  $CP$  eigenstate
- Define  $\lambda_{CP} = \frac{q\bar{A}}{p\bar{A}}$ 
  - $p, q$  from  $B^0 - \bar{B}^0$  mixing
  - Standard Model :  $\frac{q}{p} \sim e^{-2\phi_1}$
- Simplest scenario:
  - $|\frac{q}{p}| = 1, |\frac{\bar{A}}{A}| = 1 \Rightarrow S_{CP} = \text{Im}(\lambda_{CP})$
- At  $B$  factories, measure  $\Delta t$  from decay time of other  $B$   
 (tagged as  $B^0$  ( $q = +1$ ) or  $\bar{B}^0$  ( $q = -1$ ))



$$P_{CP}^q(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} [1 + q \{S_{CP} \sin(\Delta m \Delta t)\}]$$

# How To Measure Time-Dependent CP Violation

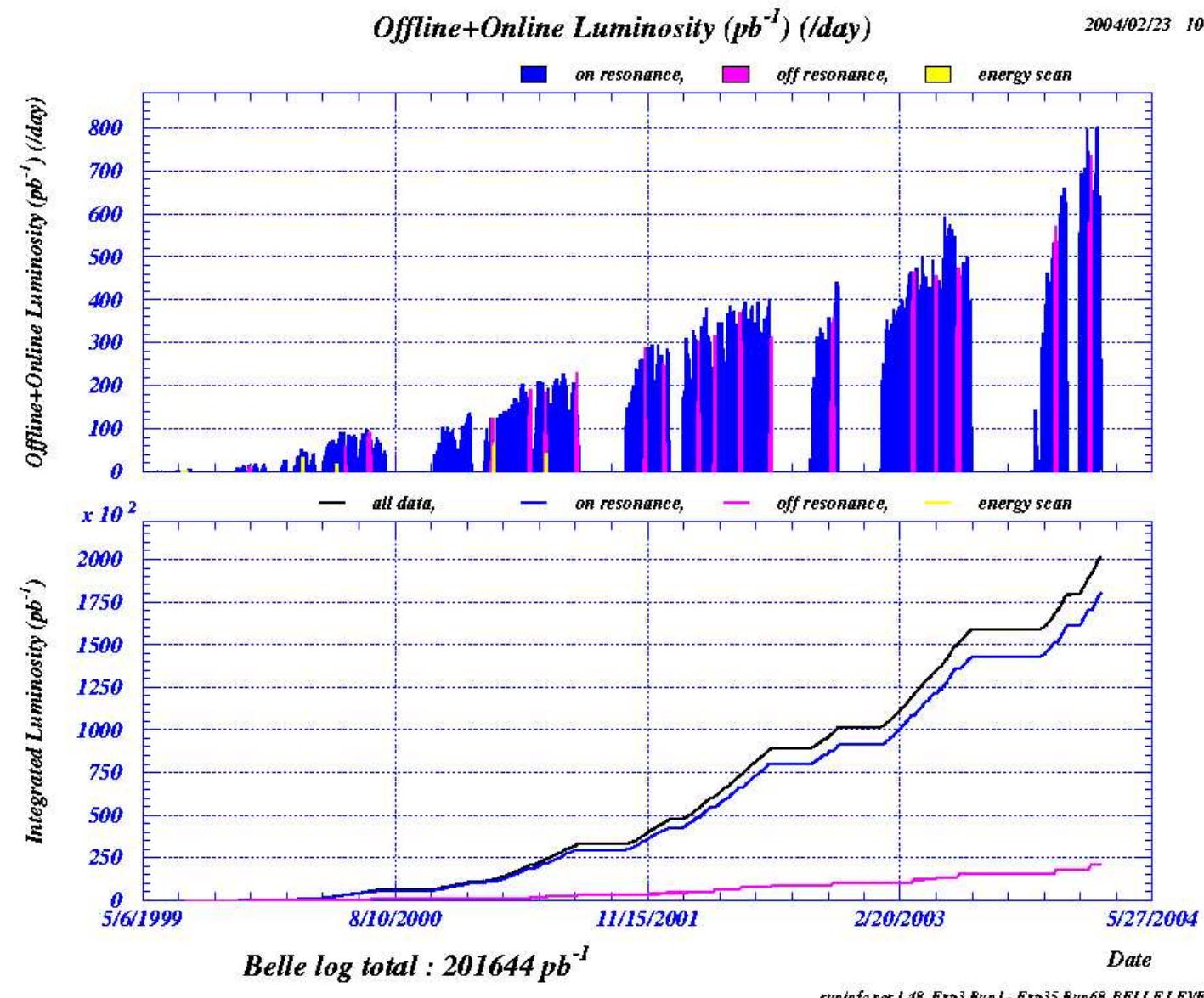


(at an asymmetric energy  $B$  factory)

1. Collect a large sample of  $B - \bar{B}$  decays
2. Identify and select events containing relevant final state
3. Tag the flavour of the other  $B$
4. Measure  $\Delta t$  from  $\Delta z = z_{CP} - z_{\text{tag}} \approx (\beta\gamma)\gamma c \Delta t$
5. Fit the sample

Lots of *Bs*!

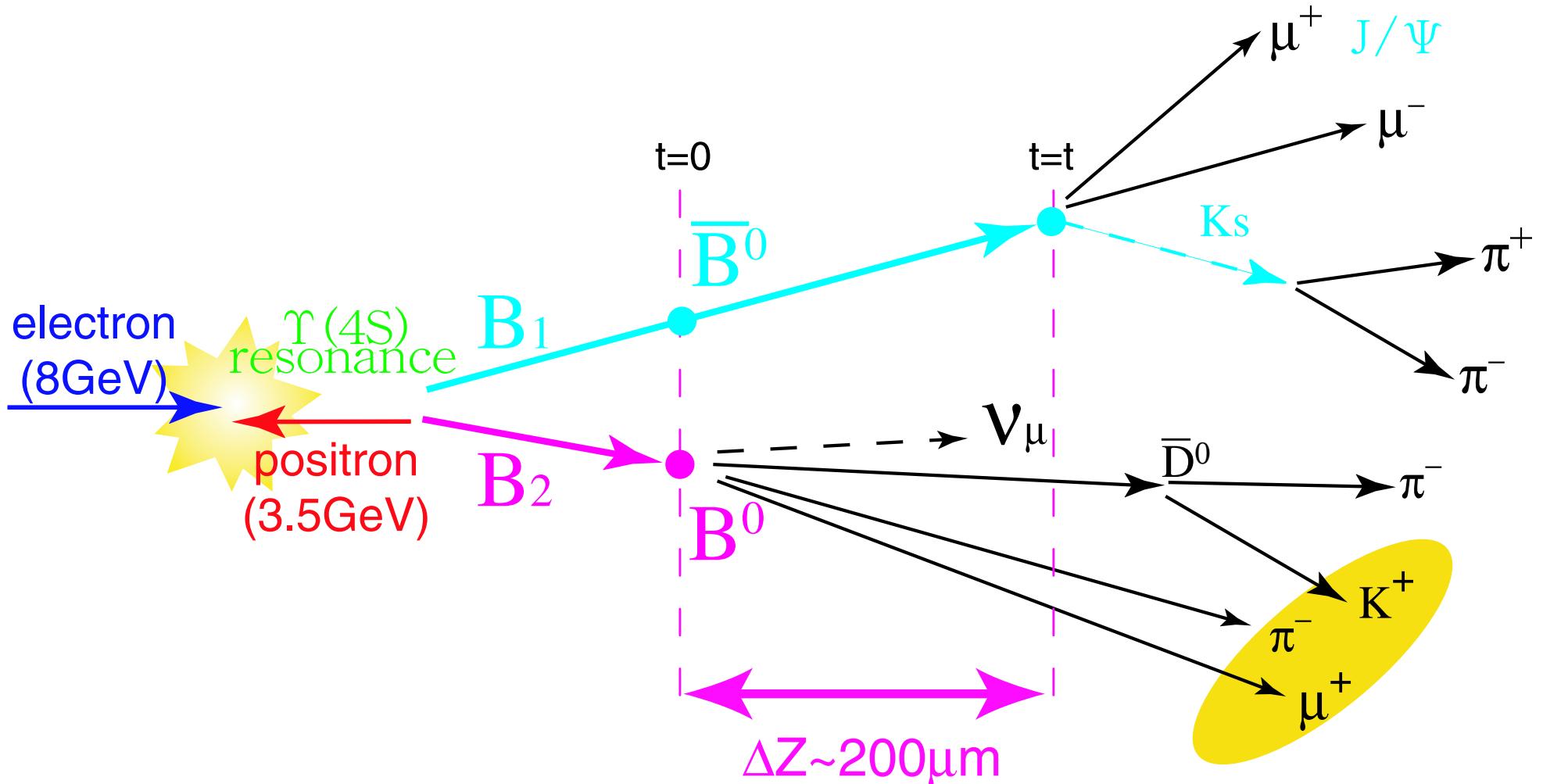
Results presented today use  $140 \text{ fb}^{-1}$  on  $\Upsilon(4S) \cong 150 \times 10^6 B\bar{B}$  pairs

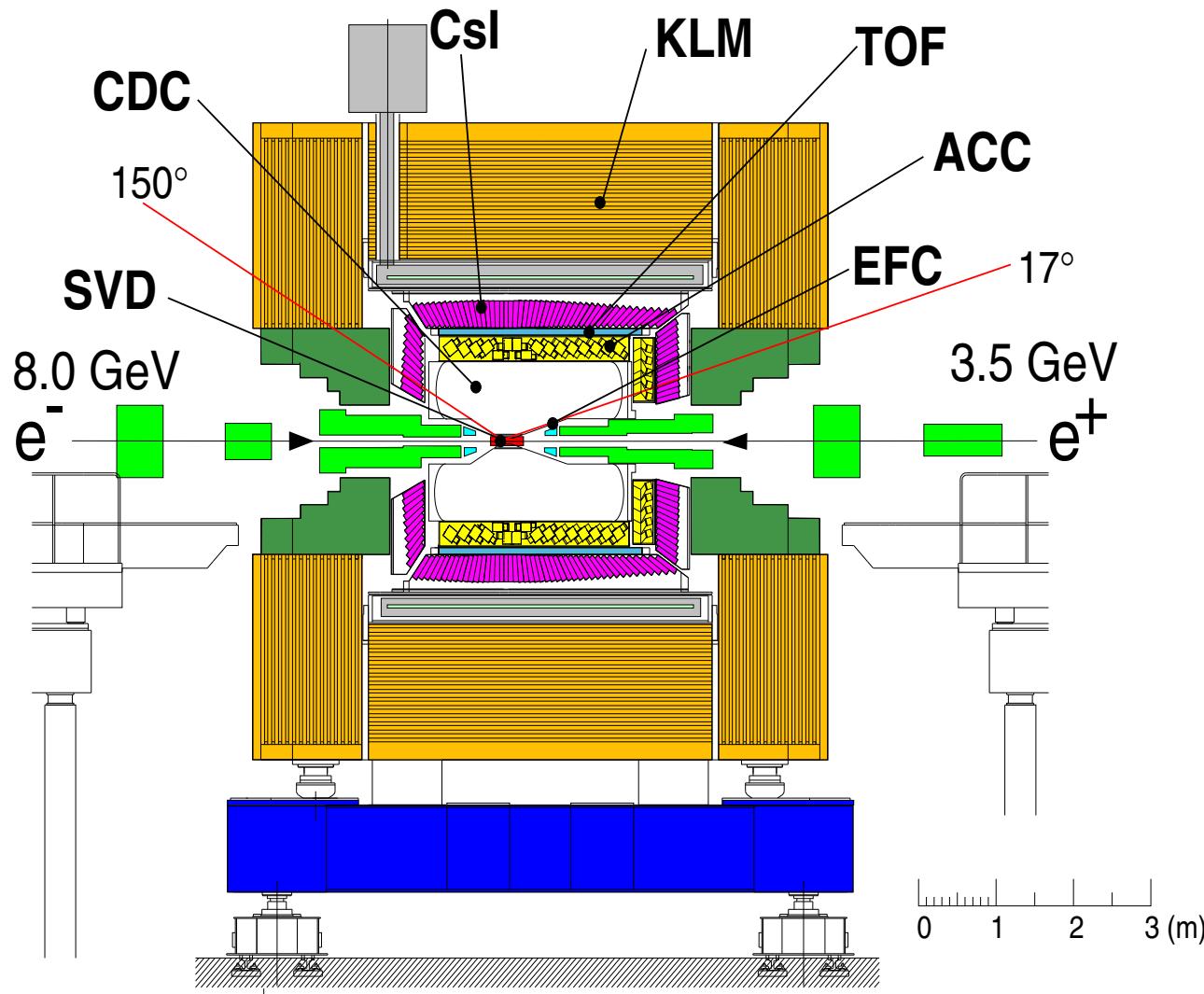


# How To Measure Time-Dependent CP Violation



Illustrated using  $\bar{B}^0 \rightarrow J/\psi K_S$ ,  $B^0 \rightarrow D^{*-} \mu^+ \nu_\mu$





- SVD 3 DSSD layers  
 $\sigma \sim 55 \mu\text{m}$  for  $1 \text{ GeV}/c$  @  $90^\circ$
- CDC 50 layers  
 $\sigma_p/p \sim 0.35\%$  @  $1 \text{ GeV}/c$
- $\sigma_\pi(dE/dx) \sim 7\%$
- TOF  $\sigma_t \sim 95 \text{ ps}$
- ACC ( $n = 1.01 \rightarrow 1.03$ )  
 $K/\pi$  separation up to  $3.5 \text{ GeV}/c$
- CsI  $\sigma_E/E_\gamma \sim 1.8\%$  @  $1 \text{ GeV}$
- KLM 14 RPC layers
- 1.5 T magnetic field

# The Golden Mode(s)

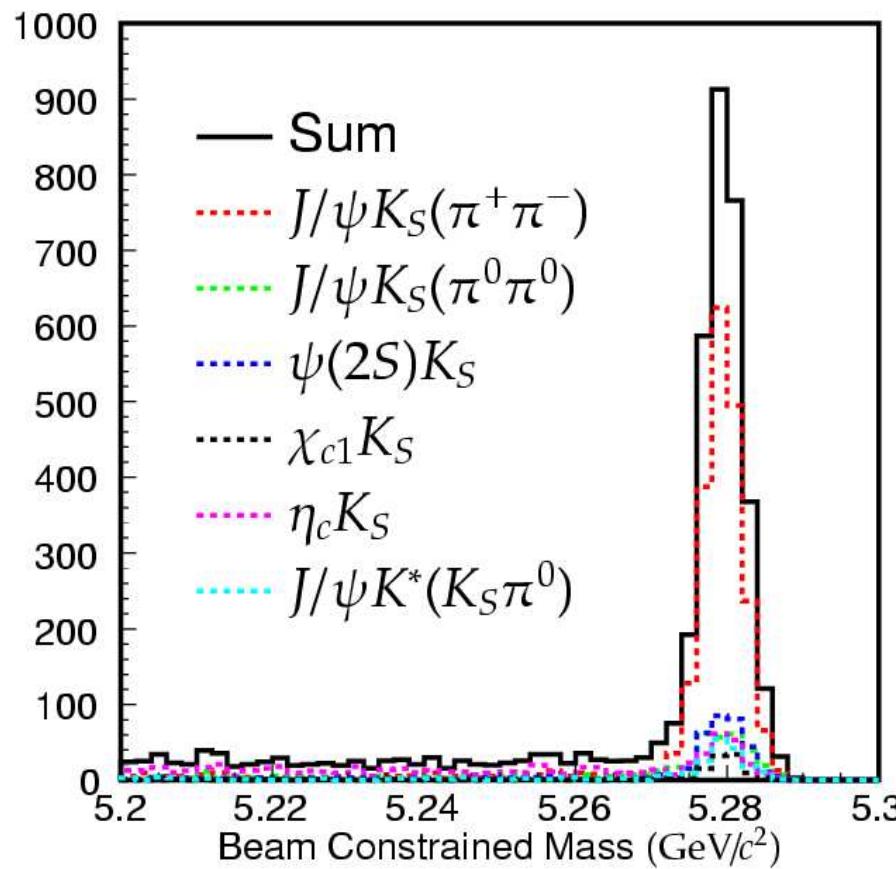


$b \rightarrow c\bar{c}s$  transitions are dominated by a single weak phase

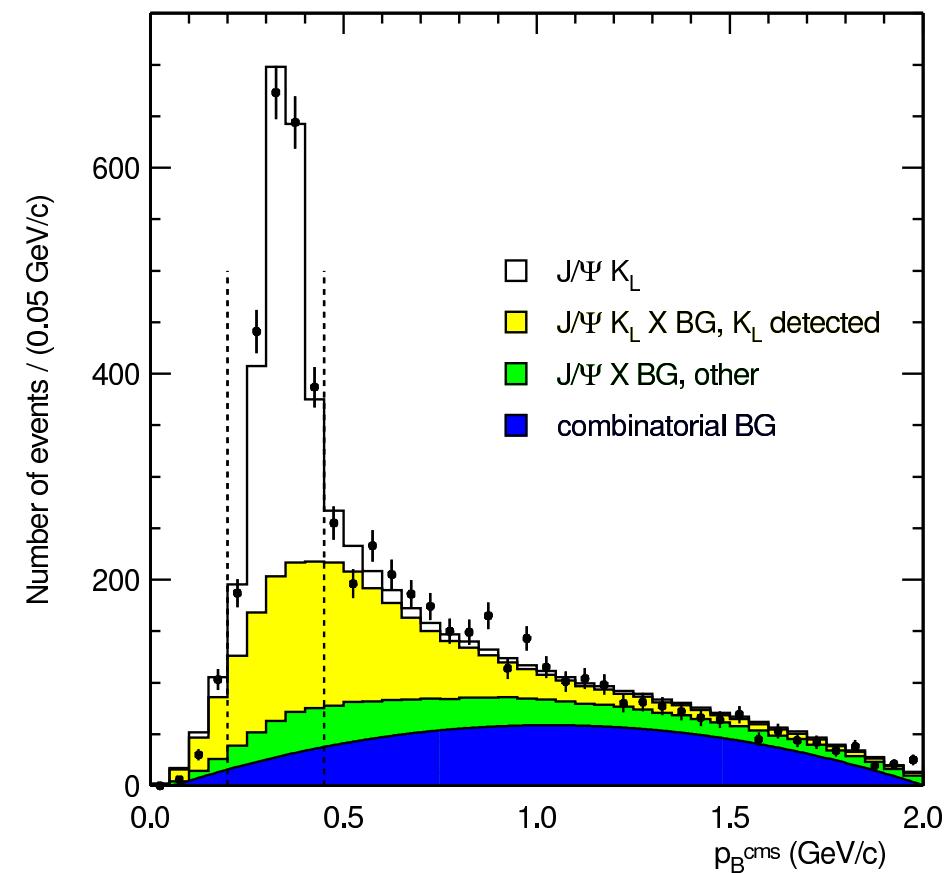
measure  $\sin(2\phi_1)$

$J/\psi K_S$ , etc.

3085 candidates



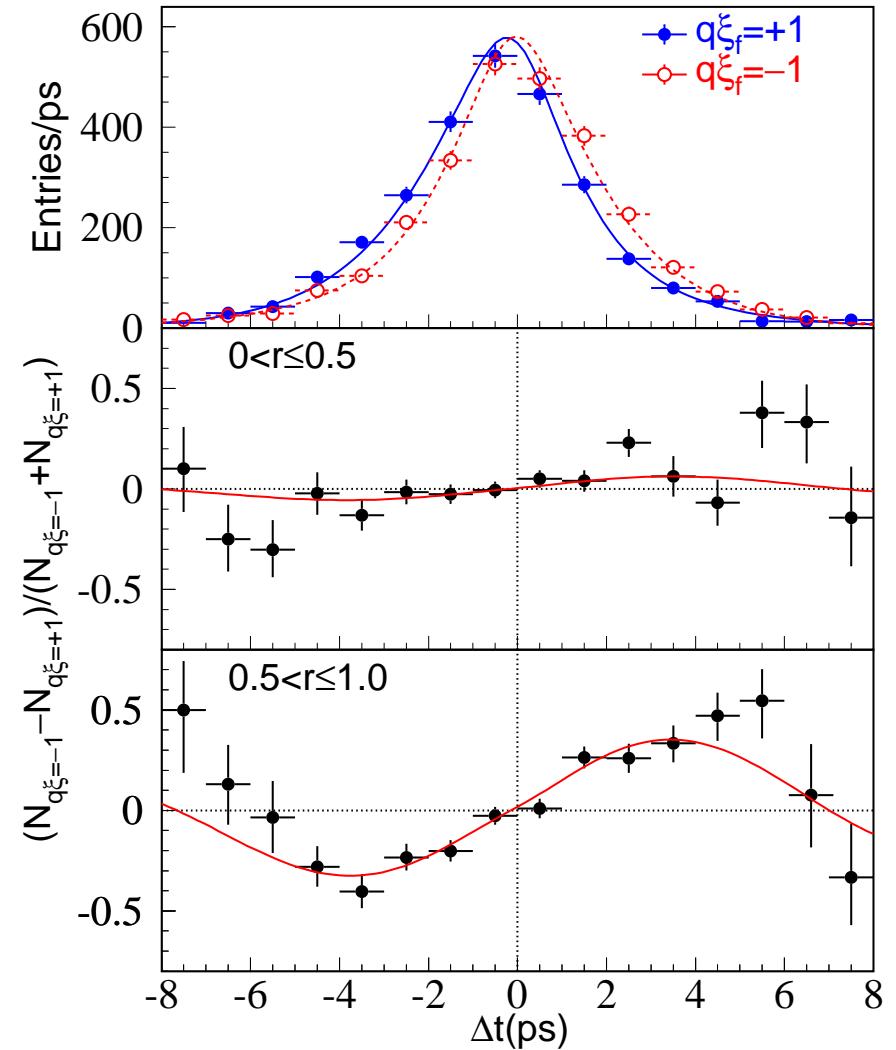
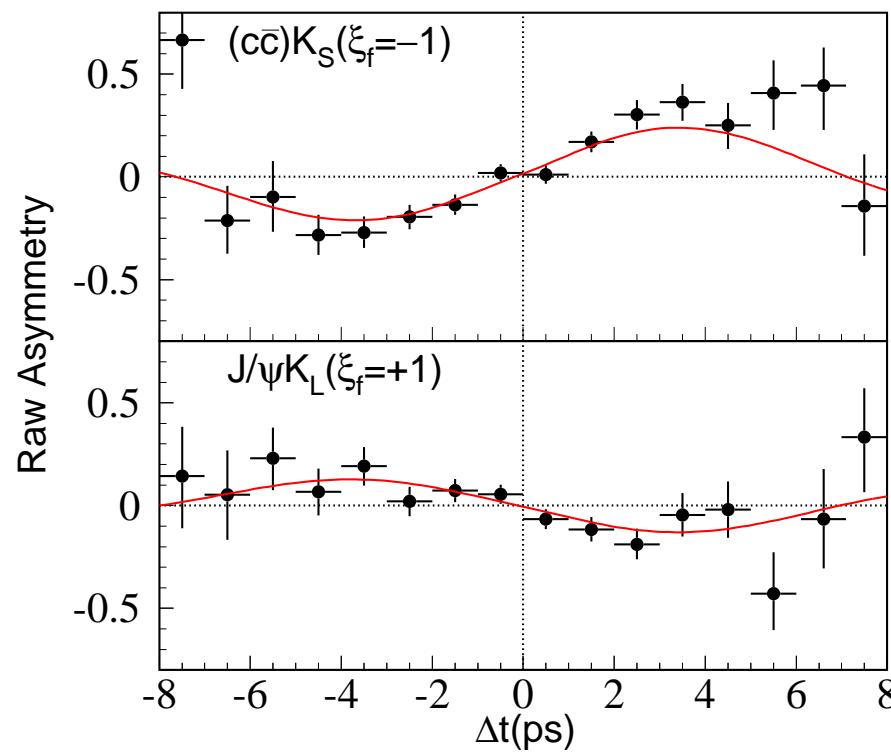
$J/\psi K_L$   
2332 candidates



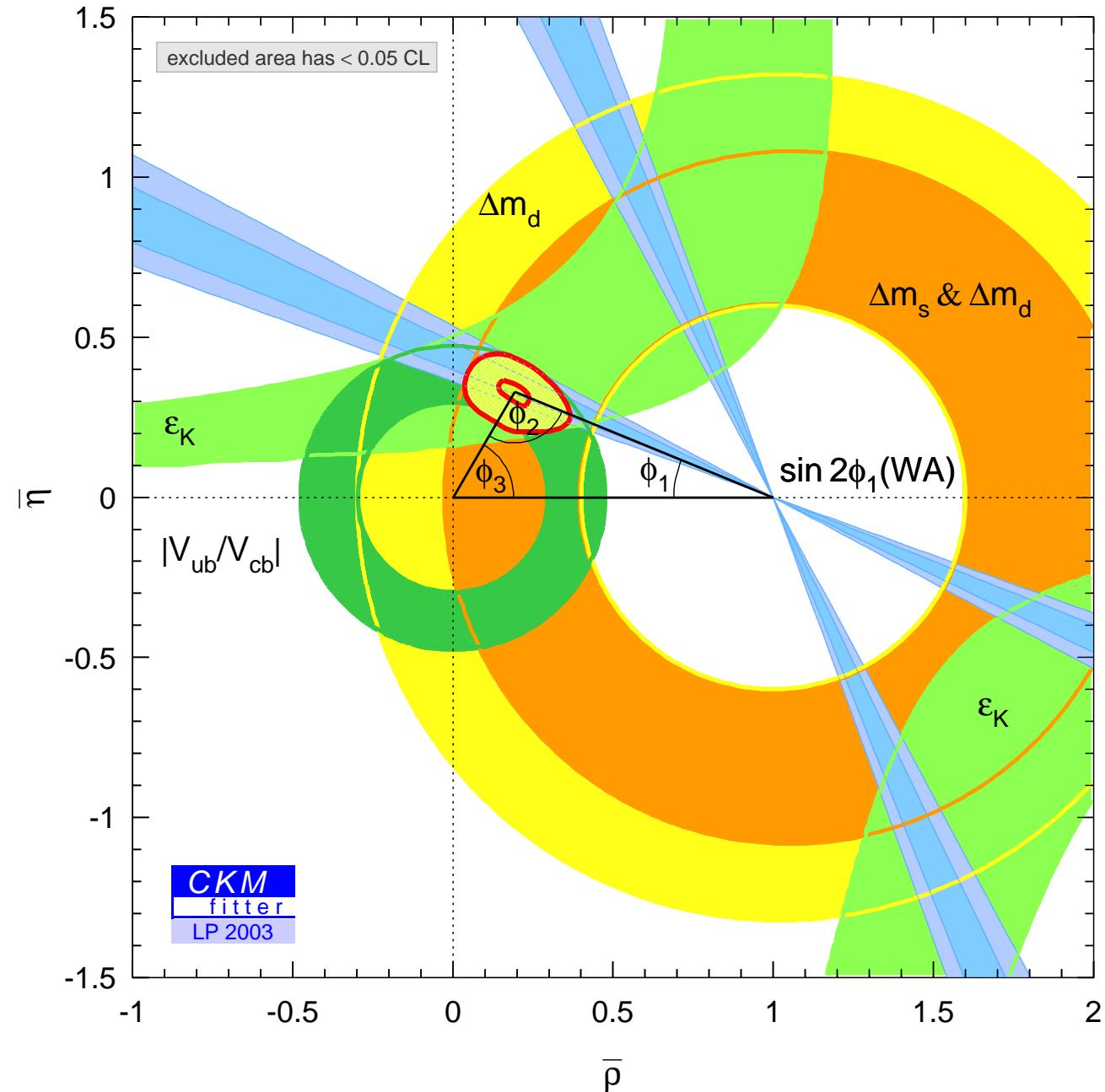
- Flavour tagging
  - Use flavour specific, inclusive properties of decay products
  - Include correlations in a multi-dimensional likelihood
  - Assign  $q = \pm 1$  &  $r \in 0, 1$
  - Divide data in categories:  $6$  of  $r \times 2$  of  $q$
- Vertexing
  - Require SVD hits to obtain precise vertex
  - Use run-dependent interaction point profile
- Fitting
  - Use unbinned maximum likelihood fits
  - Wrong tag fraction for each  $q,r$  bin
  - Event-by-event signal probability based on  $\Delta E, M_{bc}$
  - Event-by-event resolution function based on vertex errors

PRELIMINARY

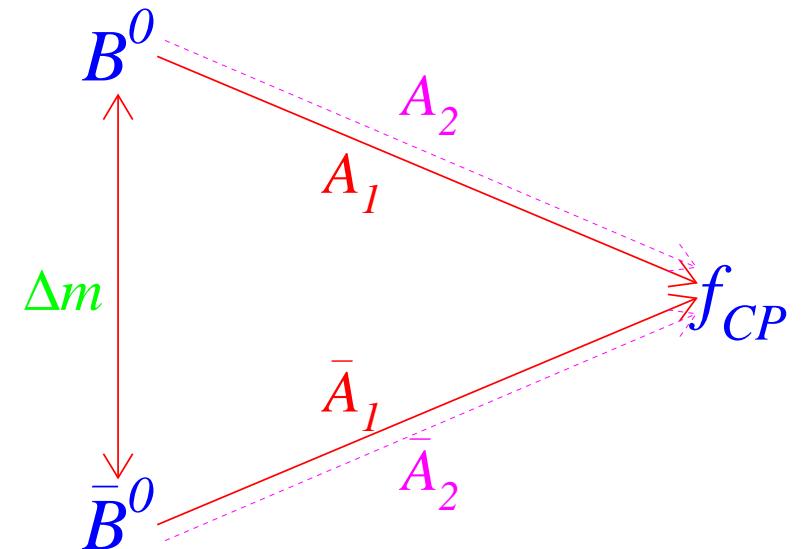
$$\sin(2\phi_1) = 0.733 \pm 0.057 \pm 0.028$$



## $\rho - \eta$ Constraint

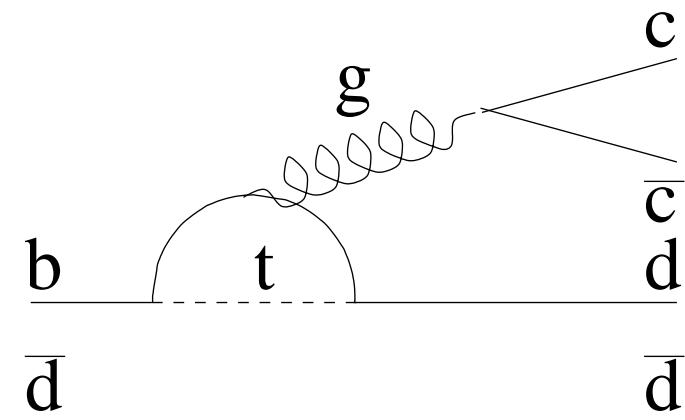
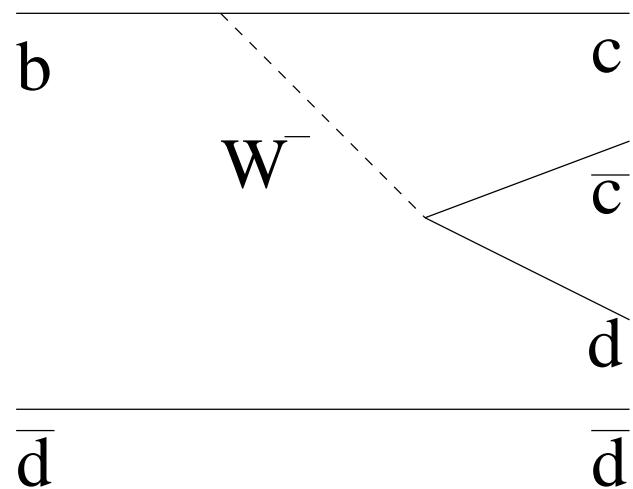


- If more than weak phase contributes,  $A = A_1 + A_2, \bar{A} = \bar{A}_1 + \bar{A}_2 \Rightarrow \left| \frac{\bar{A}}{A} \right| \neq 1$
- Remember  $\lambda_{CP} = \frac{q \bar{A}}{p A}$
- $S_{CP} = \frac{2 \text{Im}(\lambda_{CP})}{|\lambda_{CP}|^2 + 1}, \quad A_{CP} = \frac{|\lambda_{CP}|^2 - 1}{|\lambda_{CP}|^2 + 1}$
- If  $\left| \frac{q}{p} \right| = 1, A_{CP} = \frac{\Gamma_{\bar{B}^0 \rightarrow f_{CP}} - \Gamma_{B^0 \rightarrow f_{CP}}}{\Gamma_{\bar{B}^0 \rightarrow f_{CP}} + \Gamma_{B^0 \rightarrow f_{CP}}} \equiv \text{time-integrated (direct) CP asymmetry}$



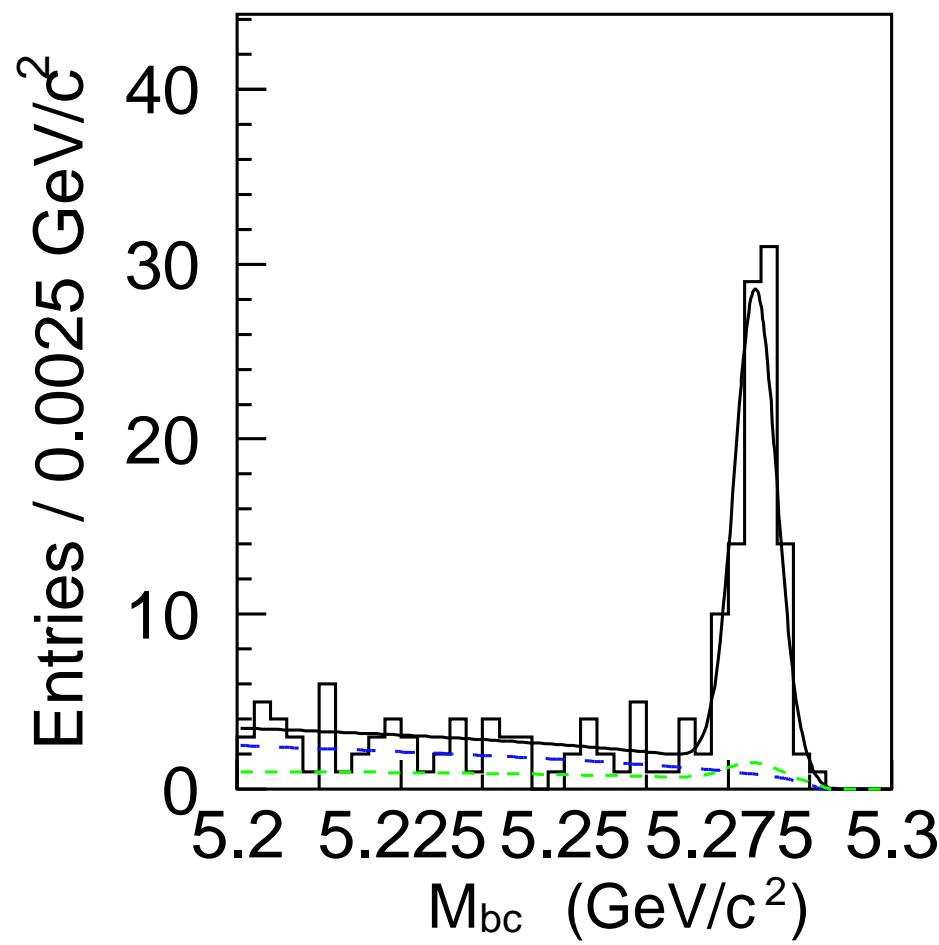
$$P_{CP}^q(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} [1 + q \{ S_{CP} \sin(\Delta m \Delta t) + A_{CP} \cos(\Delta m \Delta t) \}]$$

Contributions from tree and penguin amplitudes



Penguin contains  $V_{td} \rightsquigarrow$  different phase

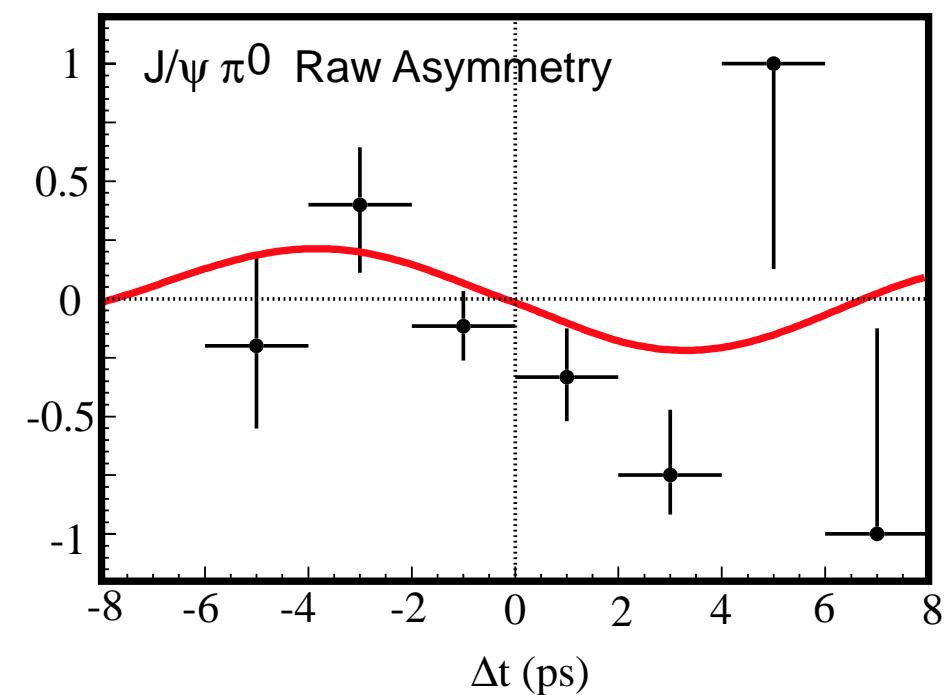
103 candidate events



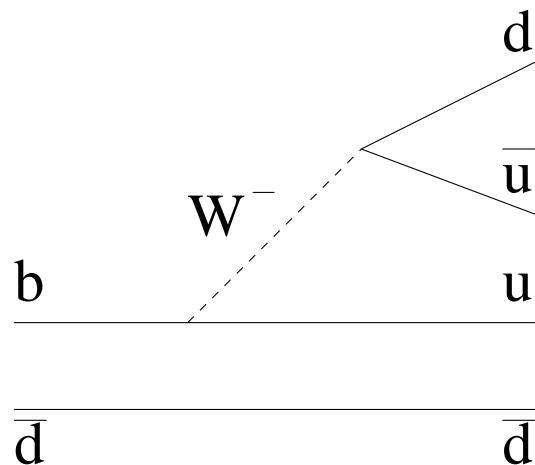
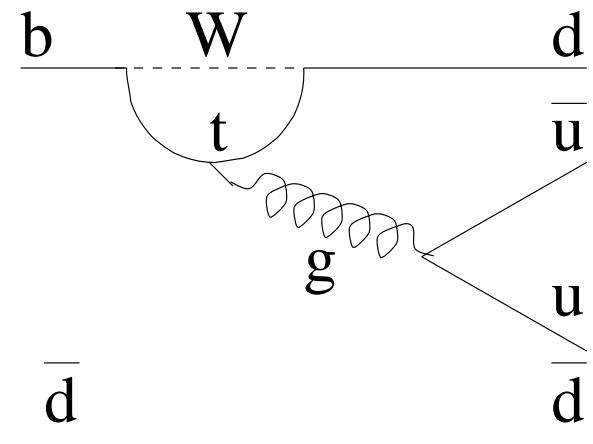
PRELIMINARY

$$S_{J/\psi\pi^0} = -0.72 \pm 0.42 \pm 0.08$$

$$A_{J/\psi\pi^0} = -0.01 \pm 0.29 \pm 0.07$$



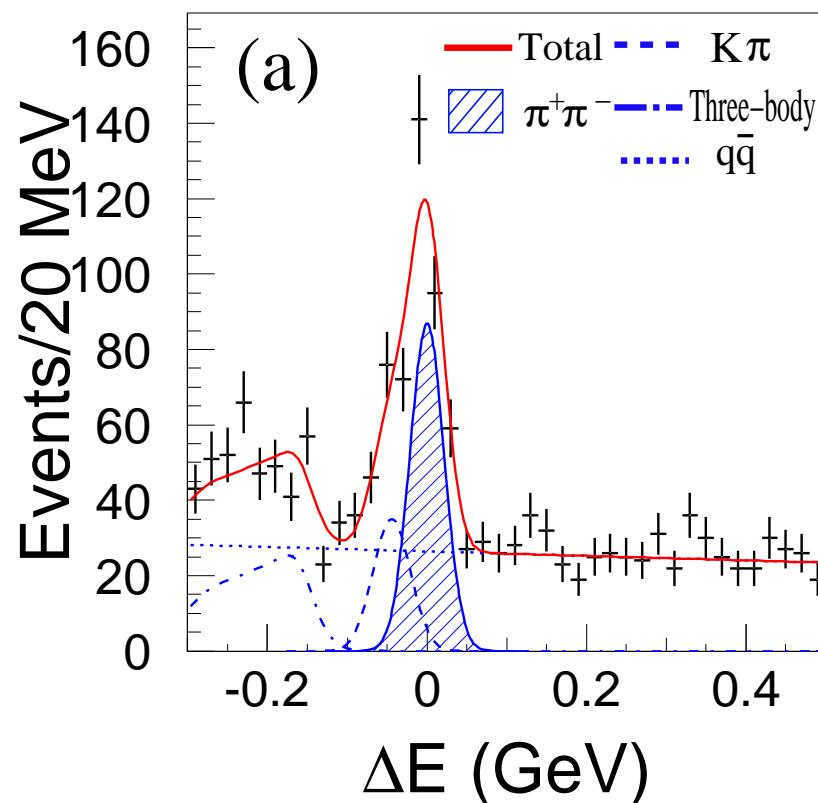
## Contributions from tree and penguin amplitudes

tree contains  $V_{ub}$ penguin contains  $V_{td}$ 

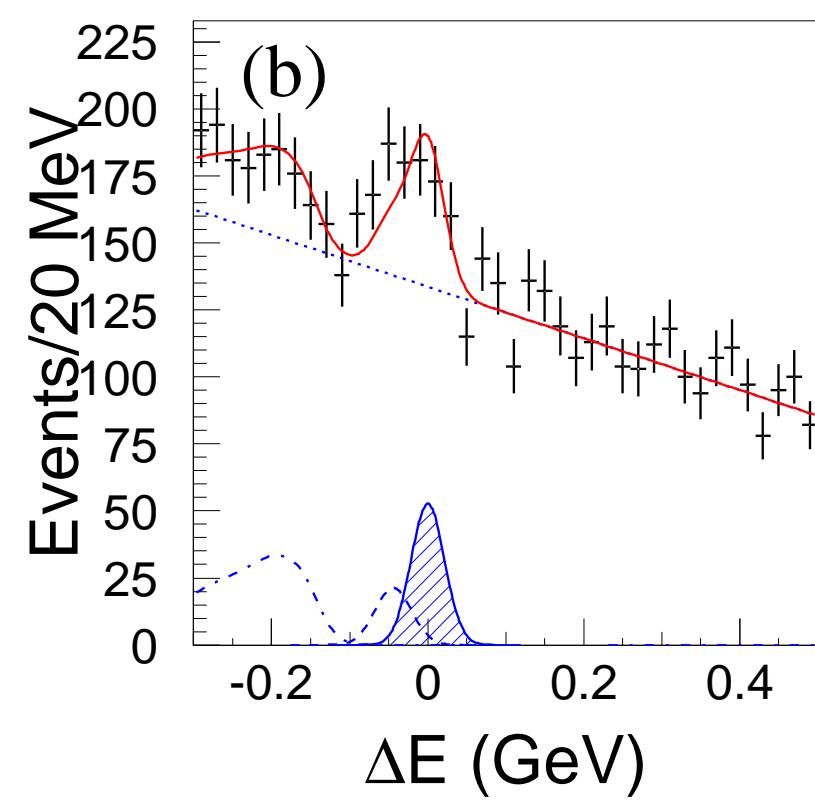
- Small branching fraction ( $\sim 4 \times 10^{-6}$ )
- Large background from  $e^+ e^- \rightarrow q\bar{q}$  ( $q = u, d, s, c$ )
- Background from  $B \rightarrow K^+ \pi^-$

Categorize candidates based on level of  $q\bar{q}$  background

High quality



Low quality

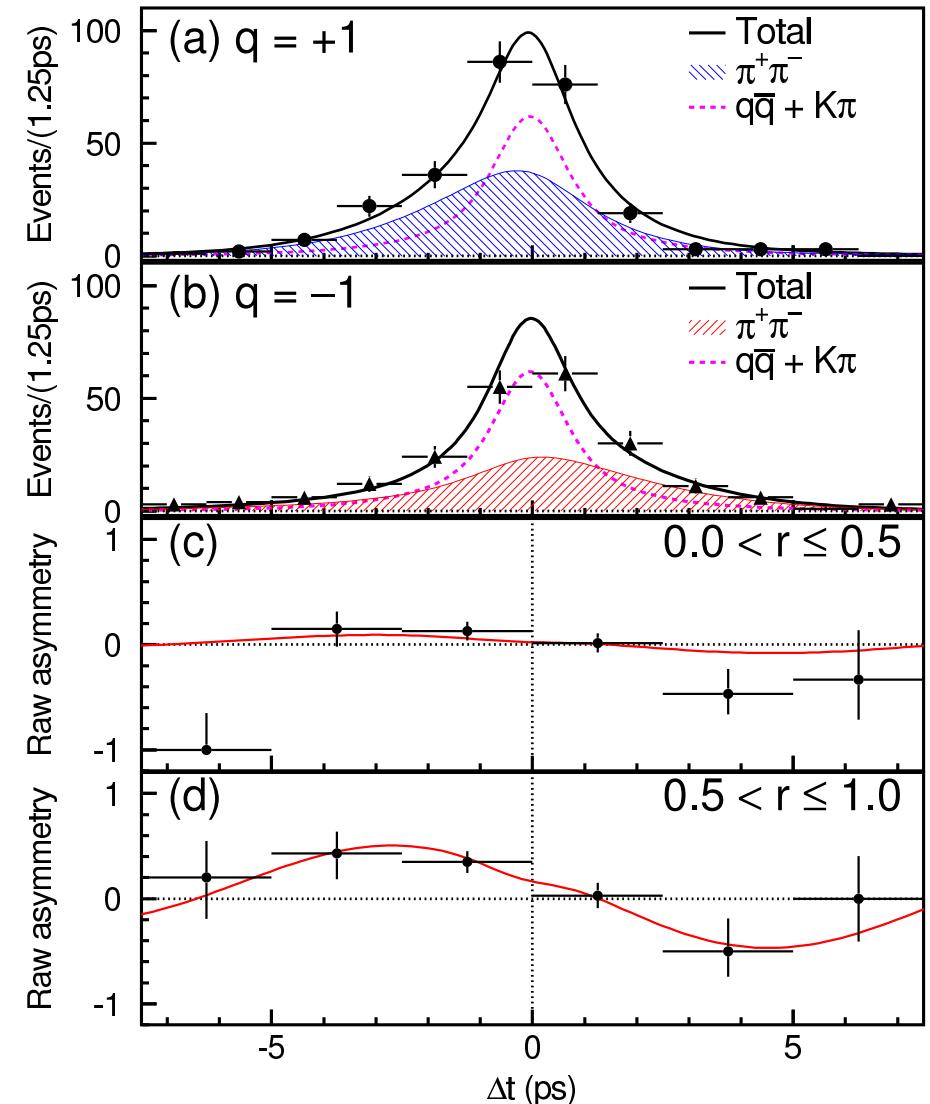


- 1529 candidates
- $372 \pm 32 \pi^+ \pi^-$  signal events

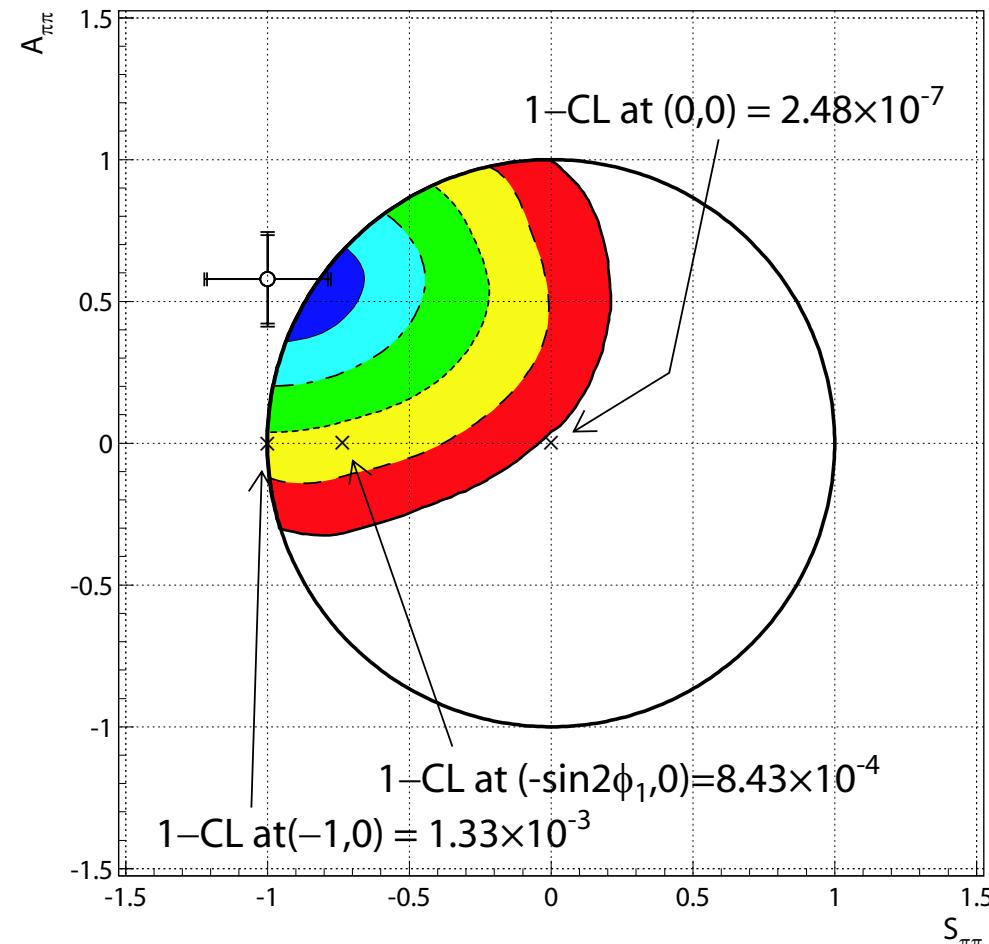
$$S_{\pi^+ \pi^-} = -1.00 \pm 0.21 \pm 0.07$$

$$A_{\pi^+ \pi^-} = +0.58 \pm 0.15 \pm 0.07$$

- Many cross-checks performed
  - $K\pi$  control sample
  - $q\bar{q}$  control sample
  - Various substitution samples
  - Toy Monte Carlo studies
  - Binned fit



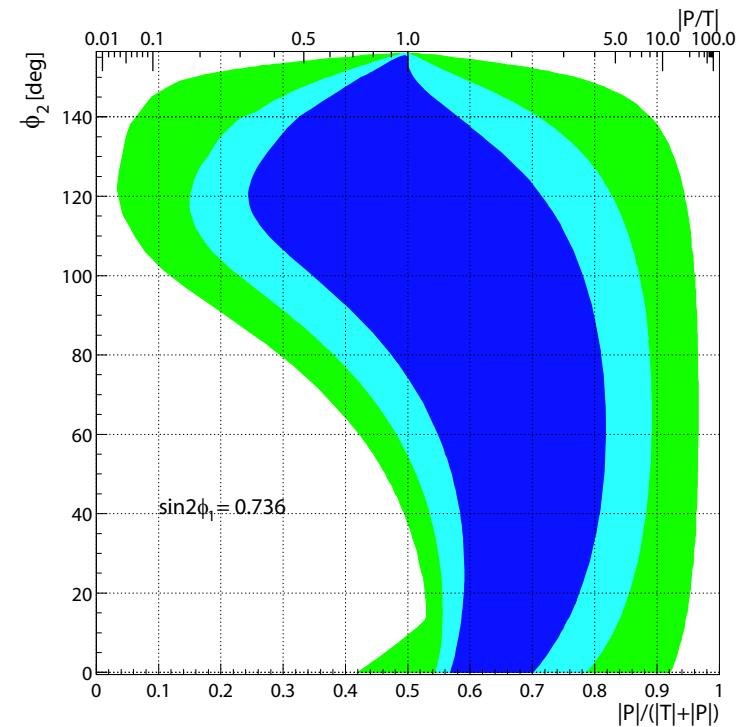
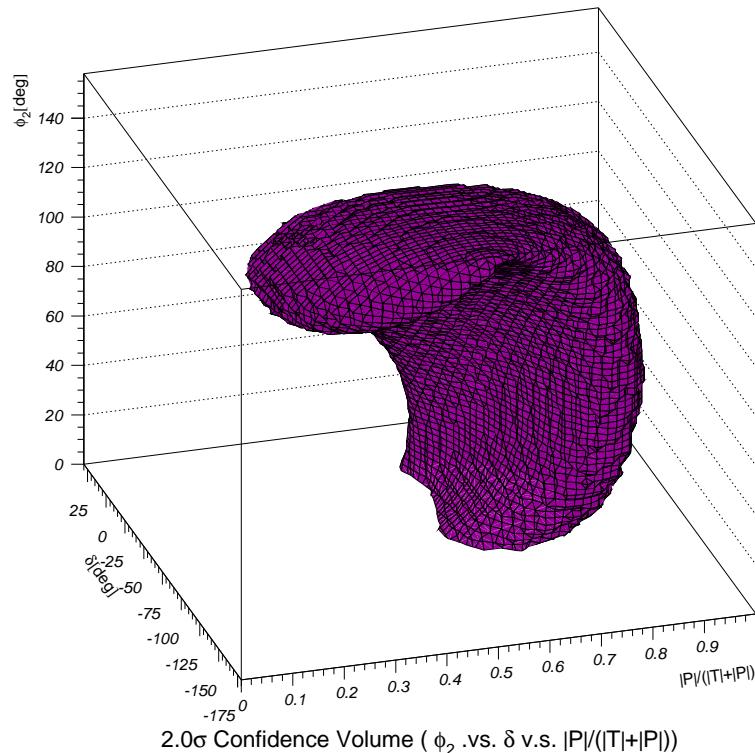
## Feldman-Cousins Analysis

OBSERVATION OF CP VIOLATION $5.2\sigma$ EVIDENCE FOR DIRECT CP VIOLATION $3.2\sigma$

# Constraint on $\phi_2$



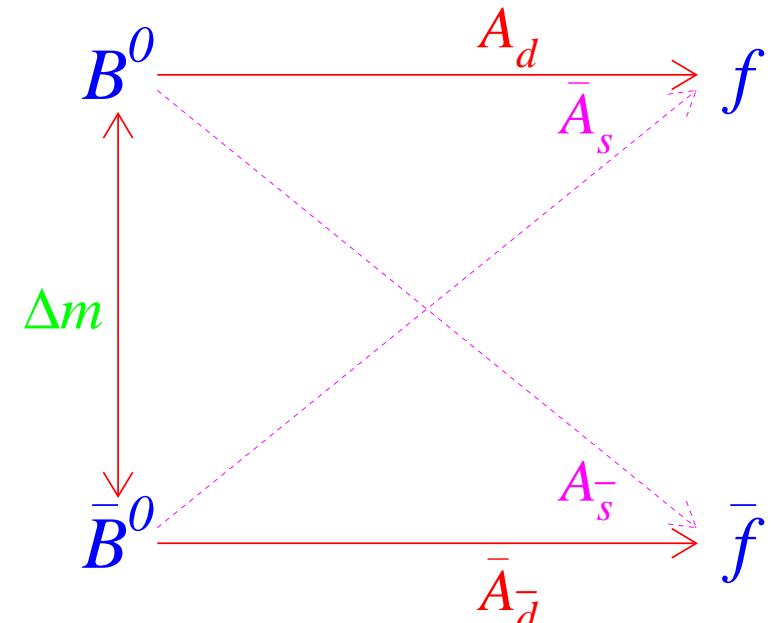
- $S_{\pi^+\pi^-}$  &  $A_{\pi^+\pi^-}$  can be written as functions of  $\phi_1$ ,  $\phi_2$ ,  $P/T$  &  $\delta$   
 M. Gronau & J.L. Rosner, PRD **65**, 093012 (2002)
- Using measured  $\phi_1$ , translate constraint on  $S_{\pi^+\pi^-}$  &  $A_{\pi^+\pi^-}$   
 $\rightarrow$  confidence volume in  $(\phi_2, P/T, \delta)$  space



95.5% confidence level limits:

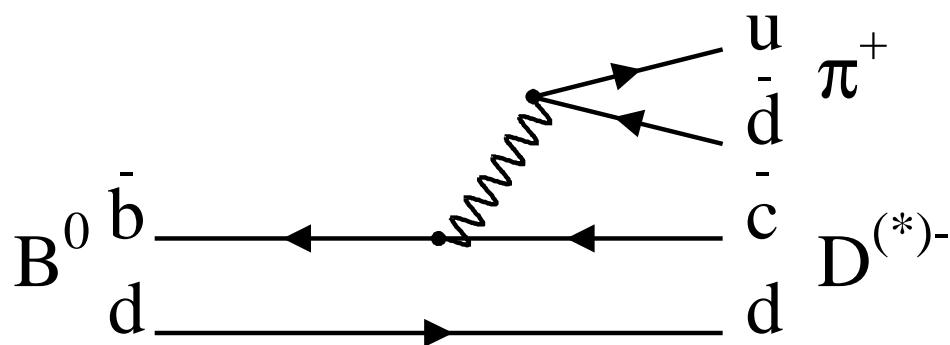
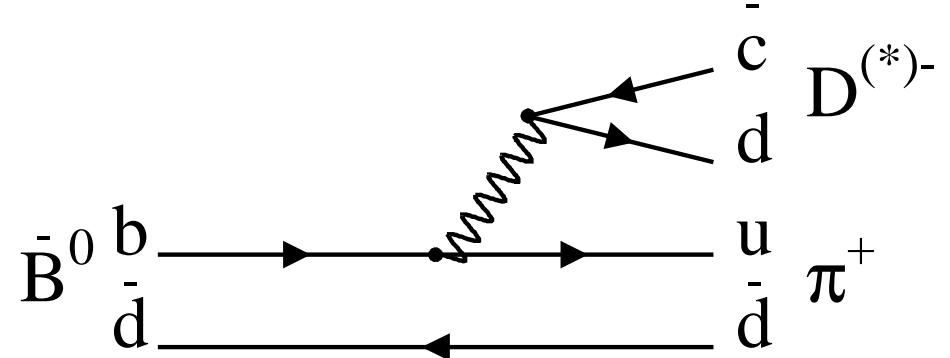
- ★  $P/T > 0.17$  (any  $\phi_2, \delta$ )
- ★  $90^\circ \leq \phi_2 \leq 146^\circ$  ( $P/T \leq 0.45$ , any  $\delta$ )

- Consider now  $B^0/\bar{B}^0$  decaying to a non- $CP$  eigenstate
- dominant** and **suppressed** contributions
- Define  $\rho = \frac{q}{p} \frac{\bar{A}_s}{A_d}$ ,  $\bar{\rho} = \frac{p}{q} \frac{A_s}{\bar{A}_{\bar{d}}}$
- Simple scenario:
  - $|q| = 1$ ,  $|\bar{\rho}| = 1$ ,  $|\rho| \ll 1$



$$P_f^q(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} [1 - q (\cos(\Delta m \Delta t) + 2 \Im(\rho) \sin(\Delta m \Delta t))]$$

$$P_{\bar{f}}^q(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} [1 + q (\cos(\Delta m \Delta t) + 2 \Im(\bar{\rho}) \sin(\Delta m \Delta t))]$$

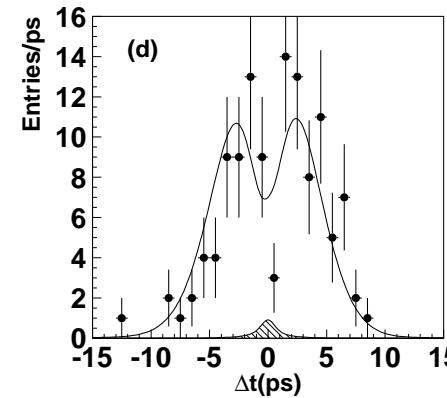
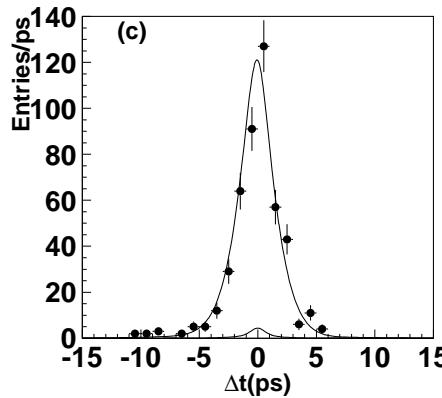
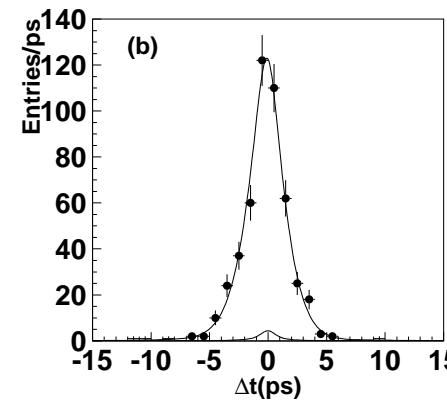
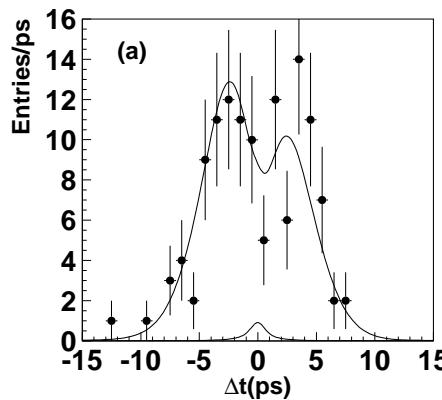
dominant  $\sim V_{cb}V_{ud}$ suppressed  $\sim V_{ub}V_{cd}$ Can naively predict  $\left| \frac{A_s}{A_d} \right| \sim 0.02$ Weak phase difference is  $2\phi_1 + \phi_3$

For  $B \rightarrow D^{(*)}\pi$

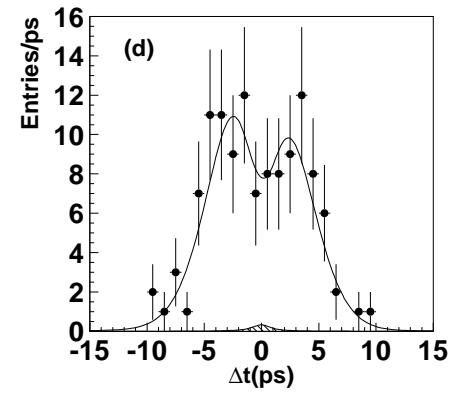
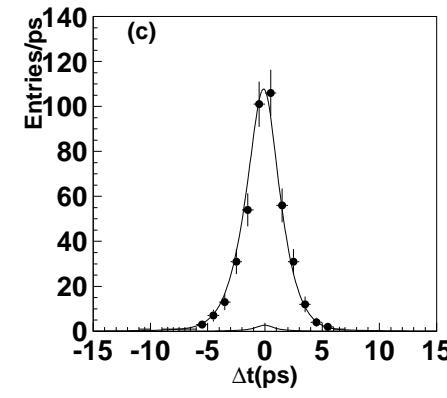
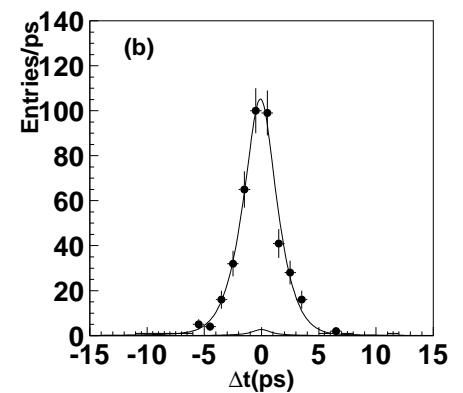
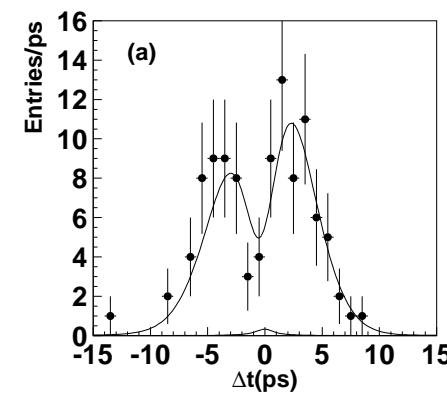
$$\Im(\rho) = (-1)^{L+1} R_{D^{(*)}\pi} \sin(2\phi_1 + \phi_3 - \delta_{D^{(*)}\pi})$$

$$\Im(\bar{\rho}) = (-1)^L R_{D^{(*)}\pi} \sin(2\phi_1 + \phi_3 + \delta_{D^{(*)}\pi})$$

$D\pi$  - 12,027 candidates



$D^*\pi$  - 10,622 candidates



Data: best quality flavour tagging; Curves: Fit result for entire data

$$2 R_{D^*\pi} \sin(2\phi_1 + \phi_3 + \delta_{D^*\pi}) = 0.109 \pm 0.057 \pm 0.019$$

$$2 R_{D^*\pi} \sin(2\phi_1 + \phi_3 - \delta_{D^*\pi}) = 0.011 \pm 0.057 \pm 0.019$$

$$2 R_{D\pi} \sin(2\phi_1 + \phi_3 + \delta_{D\pi}) = 0.087 \pm 0.054 \pm 0.018$$

$$2 R_{D\pi} \sin(2\phi_1 + \phi_3 - \delta_{D\pi}) = 0.037 \pm 0.052 \pm 0.018$$

Assume that  $\delta_{D^{(*)}\pi} = 0$  or  $\pi$ :

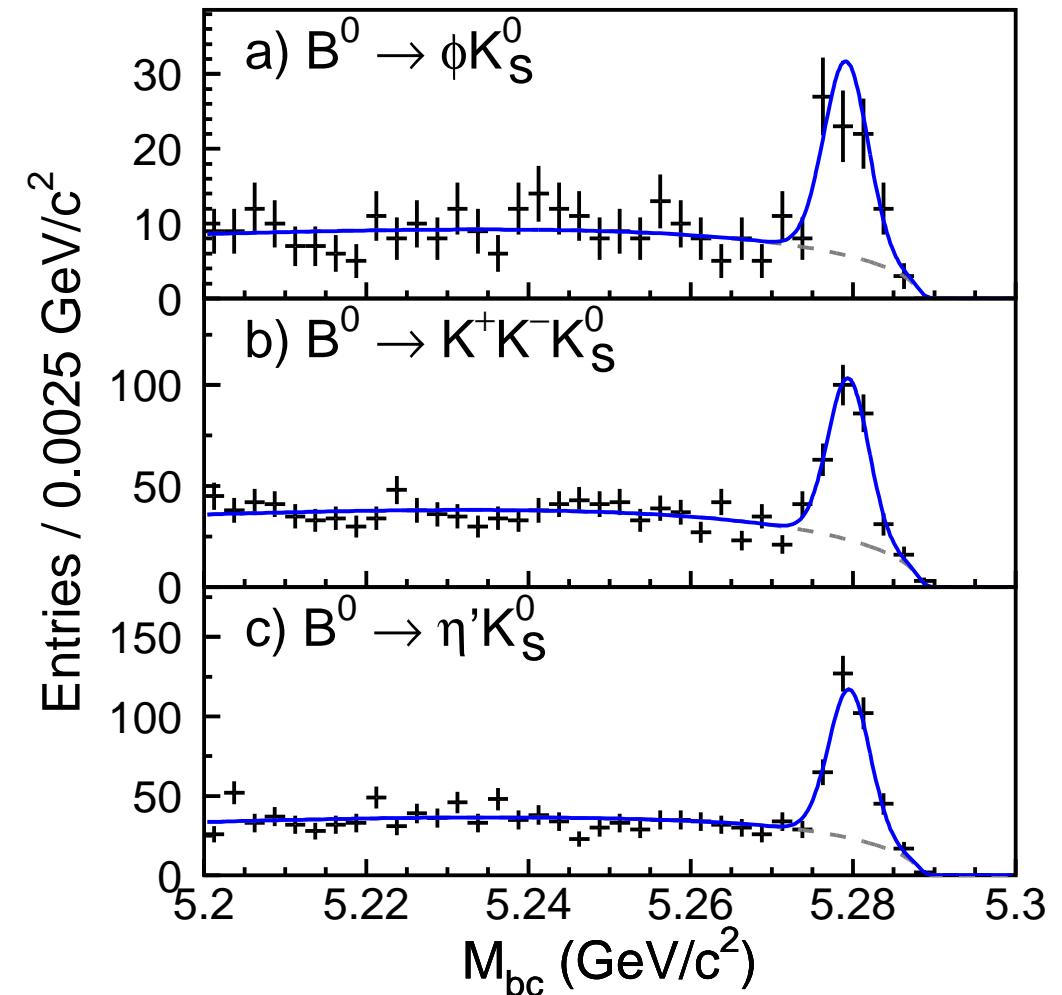
$$|2 R_{D^*\pi} \sin(2\phi_1 + \phi_3)| = 0.060 \pm 0.040 \pm 0.019$$

$$|2 R_{D\pi} \sin(2\phi_1 + \phi_3)| = 0.061 \pm 0.037 \pm 0.018$$

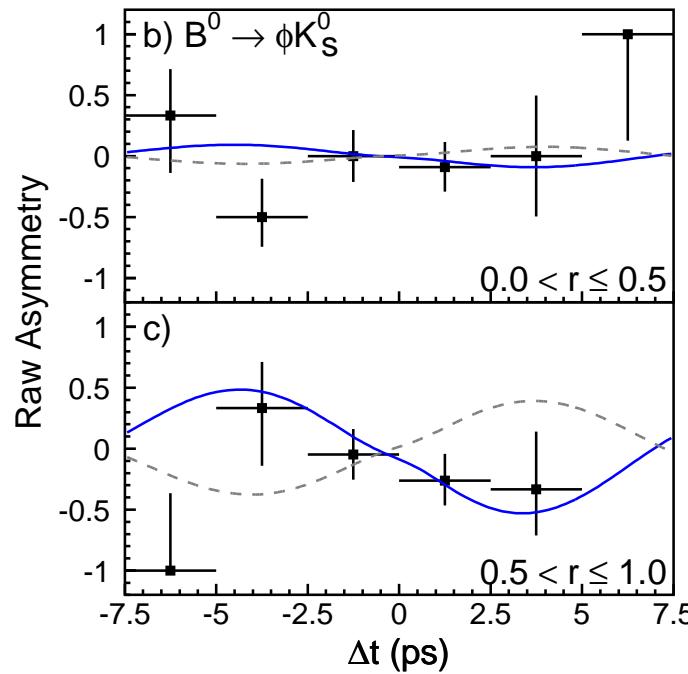
Much more data required to constrain  $\sin(2\phi_1 + \phi_3)$

- $b \rightarrow sq\bar{q}$  contains same weak phase as  $b \rightarrow c\bar{c}s$   
 $\hookrightarrow -\xi_{sq\bar{q}} S_{sq\bar{q}}$  should also measure  $\sin(2\phi_1)$
- $S_{sq\bar{q}} \neq S_{c\bar{c}s}$  can be caused by new physics in  $b \rightarrow s$  penguin

- $B \rightarrow \phi K_S$ :  $CP$  odd  
 106 candidates
- $B \rightarrow K^+ K^- K_S$ :  $CP$  even  
 361 candidates  
 $(\phi$  contribution is vetoed)
- $B \rightarrow \eta' K_S$ :  $CP$  odd  
 421 candidates



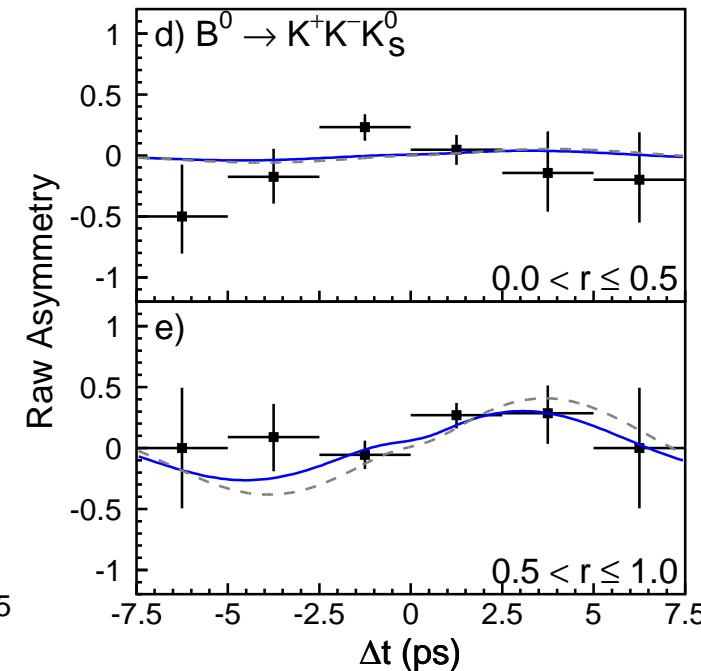
$B \rightarrow \phi K_S$



$$S_{\phi K_S} = -0.96 \pm 0.50^{+0.09}_{-0.11}$$

$$A_{\phi K_S} = -0.15 \pm 0.29 \pm 0.07$$

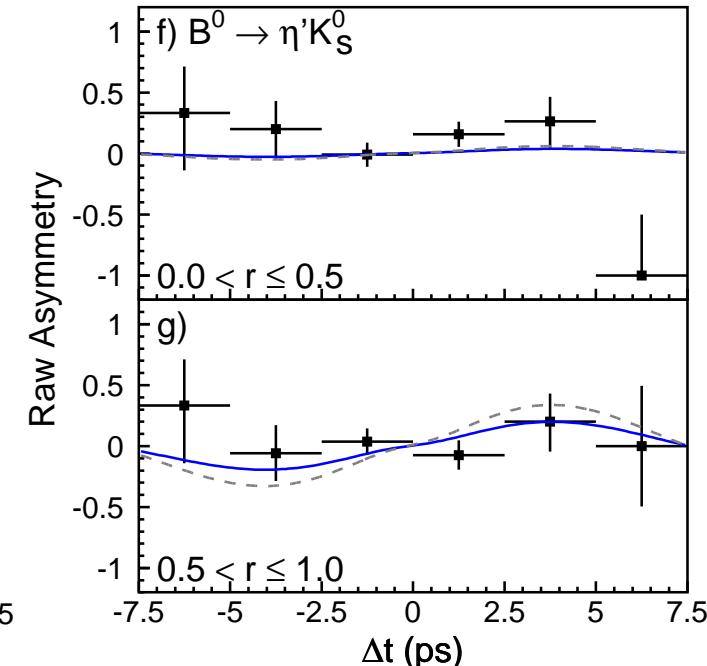
$B \rightarrow K^+ K^- K_S$



$$-S_{K^+ K^- K_S} = +0.51 \pm 0.26 \pm 0.05^{+0.18}_{-0.00}$$

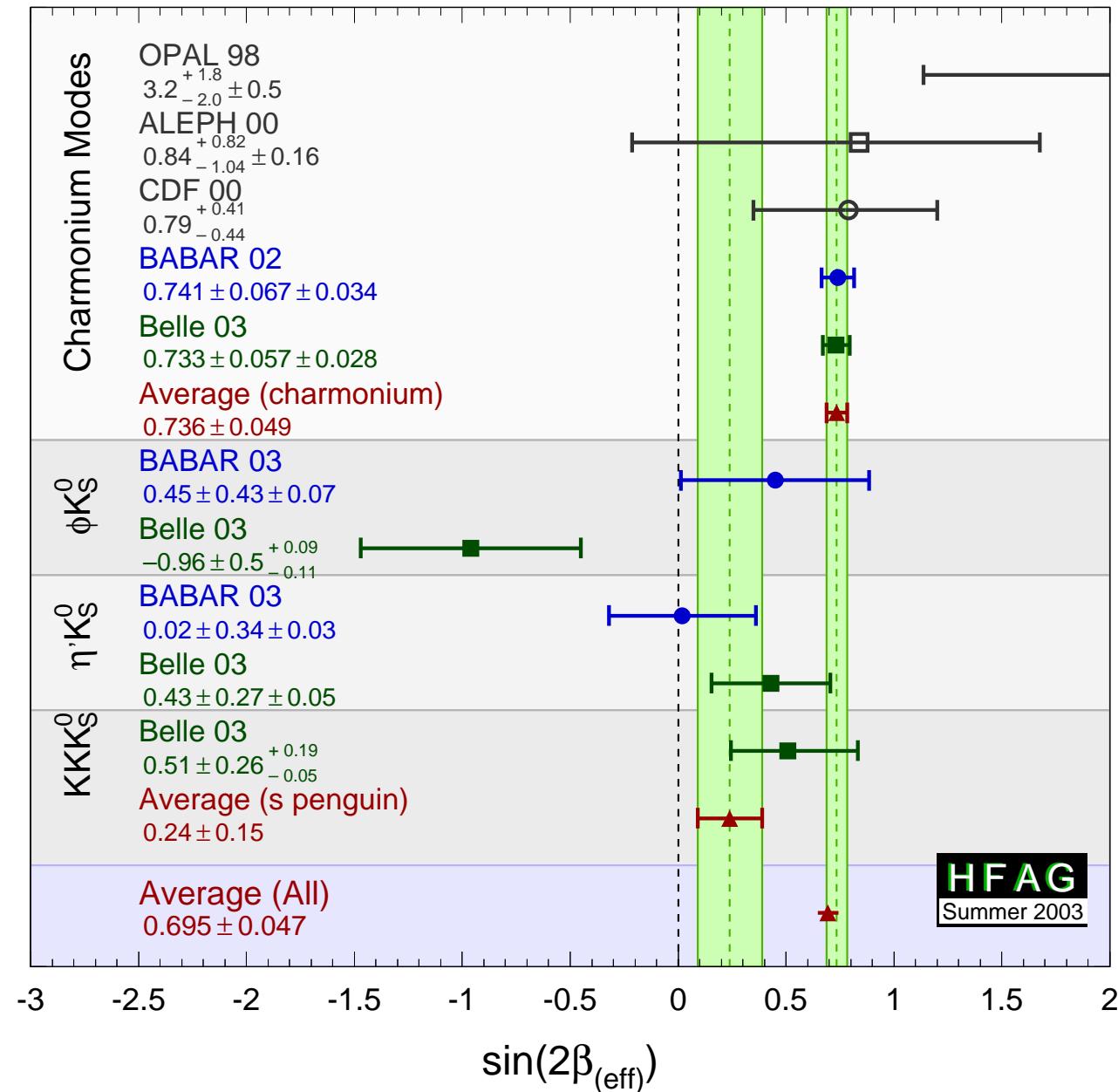
$$A_{K^+ K^- K_S} = -0.17 \pm 0.16 \pm 0.04$$

$B \rightarrow \eta' K_S$



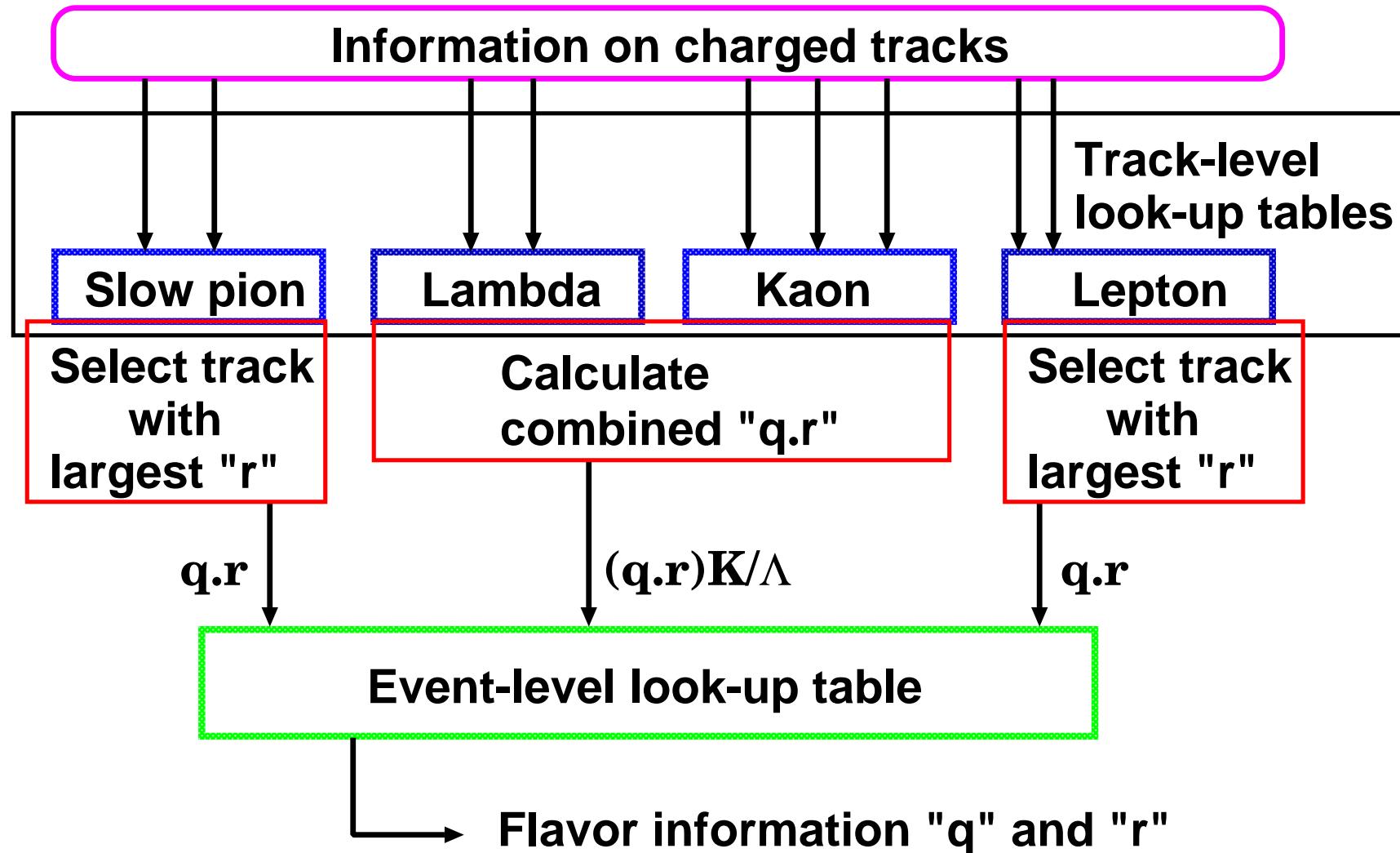
$$S_{\eta' K_S} = +0.43 \pm 0.27 \pm 0.05$$

$$A_{\eta' K_S} = -0.01 \pm 0.16 \pm 0.04$$



- $\sin(2\phi_1)$  is the most constraining  $CP$  violation measurement
- $CP$  violation in  $B \rightarrow \pi^+ \pi^-$  has been observed
- Evidence for direct  $CP$  violation in  $B$  decays
- Evidence for new physics in  $B \rightarrow \phi K_S$
- Much more luminosity has been, is being, and will be accumulated  
⇒ new and improved measurements are coming soon

# BACKUP SLIDES



Mixing asymmetry:

$$\frac{OF - SF}{OF + SF} \propto (1 - 2w) \cos(\Delta m \Delta t)$$

TABLE I: The event fractions  $\epsilon_l$ , wrong-tag fractions  $w_l$ , wrong-tag fraction differences  $\Delta w_l$ , and average effective tagging efficiencies  $\epsilon_{\text{eff}}^l = \epsilon_l(1 - 2w_l)^2$  for each  $r$  interval. The errors include both statistical and systematic uncertainties. The event fractions are obtained from the  $J/\psi K_S^0$  simulation.

| $l$ | $r$ interval  | $\epsilon_l$ | $w_l$             | $\Delta w_l$       | $\epsilon_{\text{eff}}^l$ |
|-----|---------------|--------------|-------------------|--------------------|---------------------------|
| 1   | 0.000 – 0.250 | 0.398        | $0.464 \pm 0.006$ | $-0.011 \pm 0.006$ | $0.002 \pm 0.001$         |
| 2   | 0.250 – 0.500 | 0.146        | $0.331 \pm 0.008$ | $+0.004 \pm 0.010$ | $0.017 \pm 0.002$         |
| 3   | 0.500 – 0.625 | 0.104        | $0.231 \pm 0.009$ | $-0.011 \pm 0.010$ | $0.030 \pm 0.002$         |
| 4   | 0.625 – 0.750 | 0.122        | $0.163 \pm 0.008$ | $-0.007 \pm 0.009$ | $0.055 \pm 0.003$         |
| 5   | 0.750 – 0.875 | 0.094        | $0.109 \pm 0.007$ | $+0.016 \pm 0.009$ | $0.057 \pm 0.002$         |
| 6   | 0.875 – 1.000 | 0.136        | $0.020 \pm 0.005$ | $+0.003 \pm 0.006$ | $0.126 \pm 0.003$         |

Effective tagging efficiency  $\approx 28.7\%$

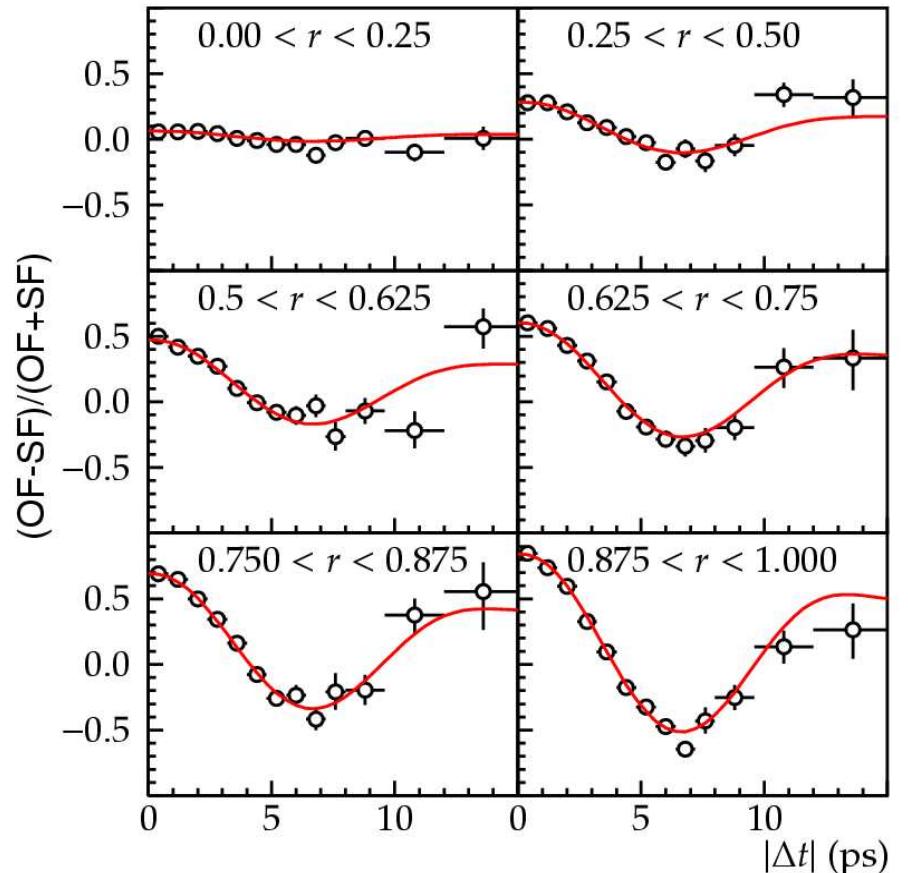


TABLE II: The numbers of reconstructed  $B \rightarrow f_{CP}$  candidates after flavor tagging and vertex reconstruction,  $N_{\text{ev}}$ , and the estimated signal purity,  $p$ , in the signal region for each  $f_{CP}$  mode.  $J/\psi$  mesons are reconstructed in  $J/\psi \rightarrow \mu^+ \mu^-$  or  $e^+ e^-$  decays. Candidate  $K_S^0$  mesons are reconstructed in  $K_S^0 \rightarrow \pi^+ \pi^-$  decays unless otherwise written explicitly.

| Mode                                | $\xi_f$ | $N_{\text{ev}}$ | $p$               |
|-------------------------------------|---------|-----------------|-------------------|
| $J/\psi K_S^0$                      | -1      | 1997            | $0.976 \pm 0.001$ |
| $J/\psi K_S^0(\pi^0 \pi^0)$         | -1      | 288             | $0.82 \pm 0.02$   |
| $\psi(2S)(\ell^+ \ell^-)K_S^0$      | -1      | 145             | $0.93 \pm 0.01$   |
| $\psi(2S)(J/\psi \pi^+ \pi^-)K_S^0$ | -1      | 163             | $0.88 \pm 0.01$   |
| $\chi_{c1}(J/\psi \gamma)K_S^0$     | -1      | 101             | $0.92 \pm 0.01$   |
| $\eta_c(K_S^0 K^- \pi^+)K_S^0$      | -1      | 123             | $0.72 \pm 0.03$   |
| $\eta_c(K^+ K^- \pi^0)K_S^0$        | -1      | 74              | $0.70 \pm 0.04$   |
| $\eta_c(p\bar{p})K_S^0$             | -1      | 20              | $0.91 \pm 0.02$   |
| All with $\xi_f = -1$               | -1      | 2911            | $0.933 \pm 0.002$ |
| $J/\psi K^{*0}(K_S^0 \pi^0)$        | +1(81%) | 174             | $0.93 \pm 0.01$   |
| $J/\psi K_L^0$                      | +1      | 2332            | $0.60 \pm 0.03$   |

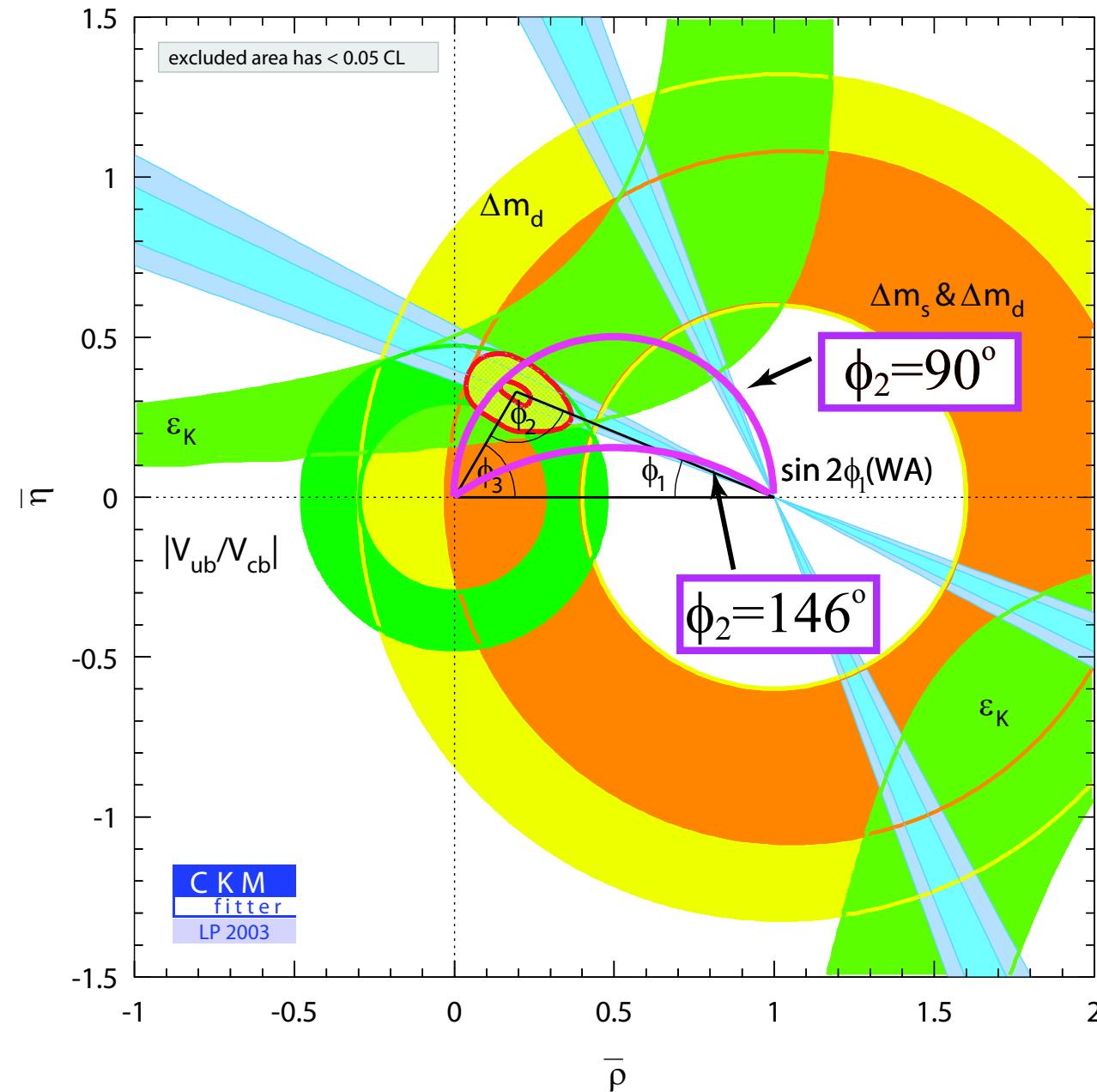
# sin( $2\phi_1$ ) Sub-samples



TABLE III: The numbers of candidate events,  $N_{\text{ev}}$ , and values of  $\sin 2\phi_1$  for various subsamples (statistical errors only).

| Sample                                           | $N_{\text{ev}}$ | $\sin 2\phi_1$    |
|--------------------------------------------------|-----------------|-------------------|
| $J/\psi K_S^0(\pi^+\pi^-)$                       | 1997            | $0.67 \pm 0.08$   |
| $J/\psi K_S^0(\pi^0\pi^0)$                       | 288             | $0.72 \pm 0.20$   |
| $\psi(2S)K_S^0$                                  | 308             | $0.89 \pm 0.20$   |
| $\chi_{c1}K_S^0$                                 | 101             | $1.54 \pm 0.49$   |
| $\eta_c K_S^0$                                   | 217             | $1.32 \pm 0.29$   |
| All with $\xi_f = -1$                            | 2911            | $0.73 \pm 0.06$   |
| $J/\psi K_L^0$                                   | 2332            | $0.80 \pm 0.13$   |
| $J/\psi K^{*0}(K_S^0\pi^0)$                      | 174             | $0.10 \pm 0.45$   |
| $f_{\text{tag}} = B^0$ ( $q = +1$ )              | 2717            | $0.72 \pm 0.09$   |
| $f_{\text{tag}} = \overline{B}{}^0$ ( $q = -1$ ) | 2700            | $0.74 \pm 0.08$   |
| $0 < r \leq 0.5$                                 | 2985            | $0.95 \pm 0.26$   |
| $0.5 < r \leq 0.75$                              | 1224            | $0.68 \pm 0.11$   |
| $0.75 < r \leq 1$                                | 1208            | $0.74 \pm 0.07$   |
| data set I ( $78 \text{ fb}^{-1}$ )              | 3013            | $0.73 \pm 0.07$   |
| data set II ( $62 \text{ fb}^{-1}$ )             | 2404            | $0.74 \pm 0.09$   |
| All                                              | 5417            | $0.733 \pm 0.057$ |

# $\rho - \eta$ Constraint With $\pi^+\pi^-$ Result



| Systematic Uncertainties        | A            | S            |
|---------------------------------|--------------|--------------|
| Wrong tag fraction              | 0.009        | 0.009        |
| Physics ( $B$ , $m_d$ , $A_k$ ) | 0.024        | 0.007        |
| Resolution function             | 0.010        | 0.020        |
| Background shape                | 0.014        | 0.021        |
| Background fractions            | 0.028        | 0.025        |
| Fit bias                        | 0.018        | 0.023        |
| Vertexing                       | 0.039        | 0.045        |
| Tag side interference           | 0.027        | 0.011        |
| Total                           | <b>0.066</b> | <b>0.066</b> |

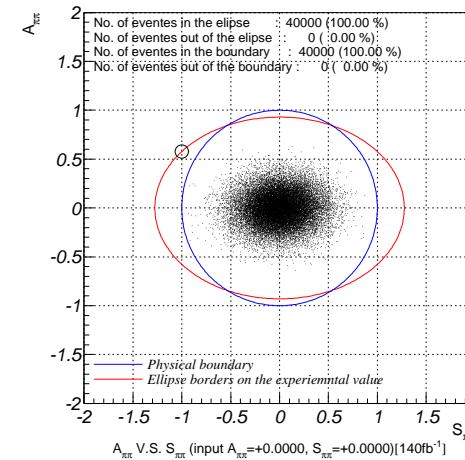
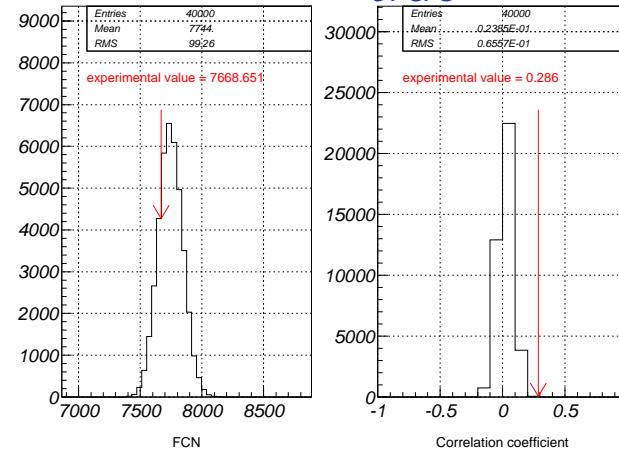
Systematic error < Statistical error

# $\pi^+\pi^-$ Monte Carlo Pseudo-Experiments

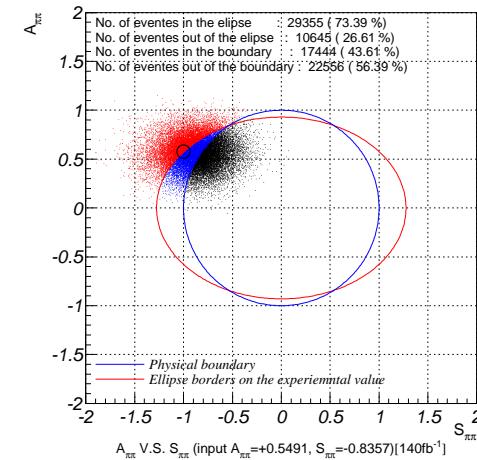
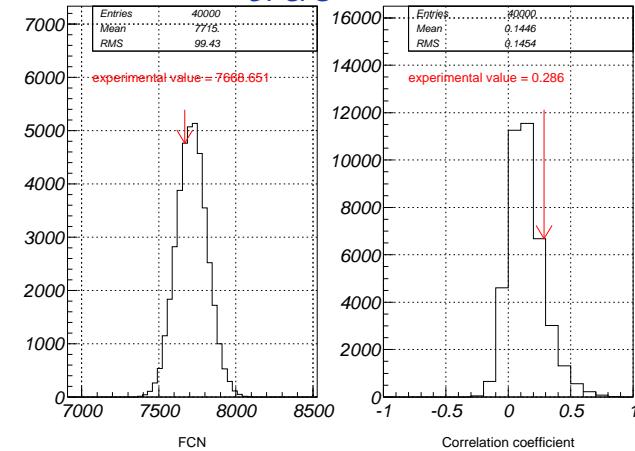


$10^7$  pseudo-experiments generated with:

$$(S_{\pi^+\pi^-}, A_{\pi^+\pi^-})_{\text{true}} = (0, 0)$$



$$(S_{\pi^+\pi^-}, A_{\pi^+\pi^-})_{\text{true}} = (+0.55, -0.83)$$



$P(\text{Belle result}) < 10^{-7}$

$P(\text{Belle result}) \sim 27\%$

- CP of K<sup>+</sup>K<sup>-</sup>K<sub>S</sub> depends on angular momentum of K<sup>+</sup>K<sup>-</sup>
  - spin-0  $\Rightarrow$  CP = +1 eg. f<sub>0</sub>K<sub>S</sub>
  - spin-1  $\Rightarrow$  CP = -1 eg.  $\phi$ K<sub>S</sub>
- Determine CP = +1 fraction ( $\alpha^2$ ) using isospin relation between three kaon final states

$$\frac{1}{\tau_{B^0}} \mathcal{B}(B^0 \rightarrow K^+ K^- K^0) = \frac{1}{\tau_{B^+}} \mathcal{B}(B^+ \rightarrow K^0 \bar{K}^0 K^+)$$

$$K^0 \bar{K}^0 K^+ = \alpha (K_S K_S K^+ + K_L K_L K^+) + \beta K_S K_L K^+$$

$$\mathcal{B}(B^+ \rightarrow K_S K_S K^+) = \mathcal{B}(B^+ \rightarrow K_L K_L K^+)$$

$$\alpha^2 = 2 \times \frac{\mathcal{B}(B^+ \rightarrow K_S K_S K^+)}{\mathcal{B}(B^0 \rightarrow K^+ K^- K^0)} \times \frac{\tau_{B^0}}{\tau_{B^+}}$$

- Measure  $\alpha^2 = 1.03 \pm 0.15 \pm 0.05$

