

# Twenty Years of Bottom Production (and Charm, and Top)

vs. QCD

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A success story, a few glitches left, and some good lessons



# What shall we mean by “success”?

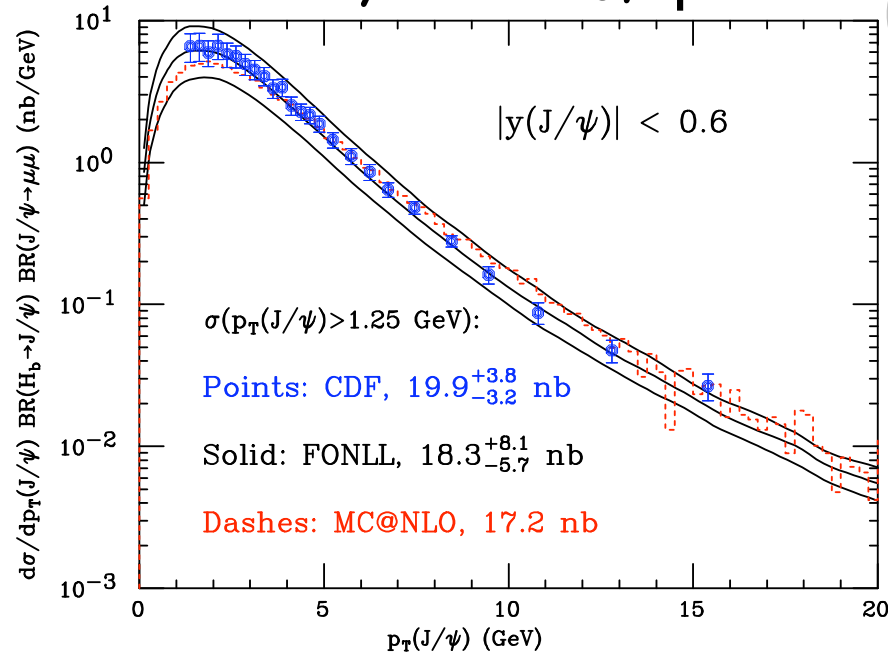
Take massive Next-to-Leading Order perturbative QCD (+ NLL resummation, where needed ) as a reference, and ask for its ability to:

- predict total rates for charm, bottom and top production
- describe differential distributions with the addition of a minimal, self-consistent, and possibly universal set of non-perturbative inputs

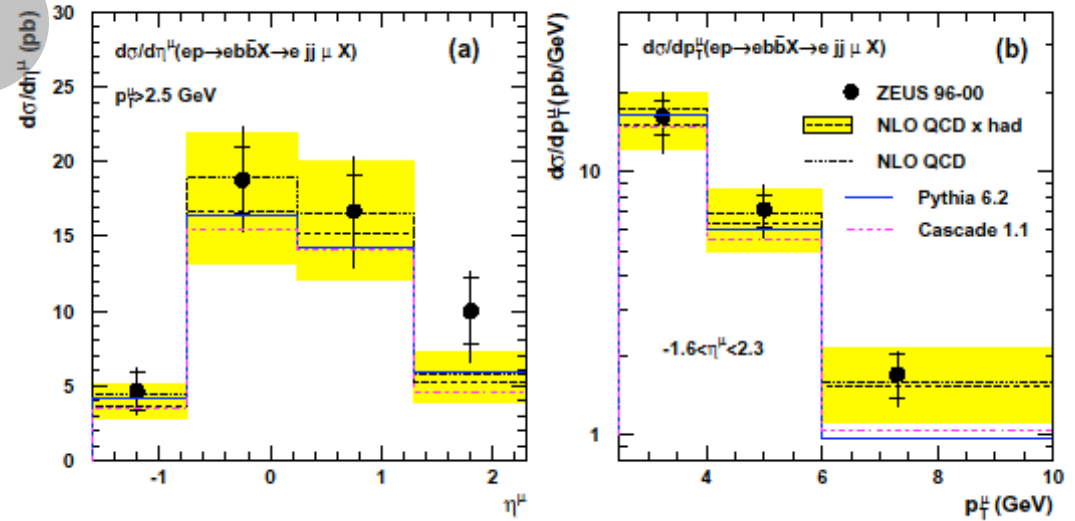
A successful comparison will be an agreement between possibly real measurements (i.e. little or no extrapolations/deconvolutions) and QCD predictions, within both experimental and theoretical uncertainties (ren./fact. scales, quark masses, strong coupling, PDFs and FFs, ....)

# Heavy Quark Production vs. NLO(++) QCD

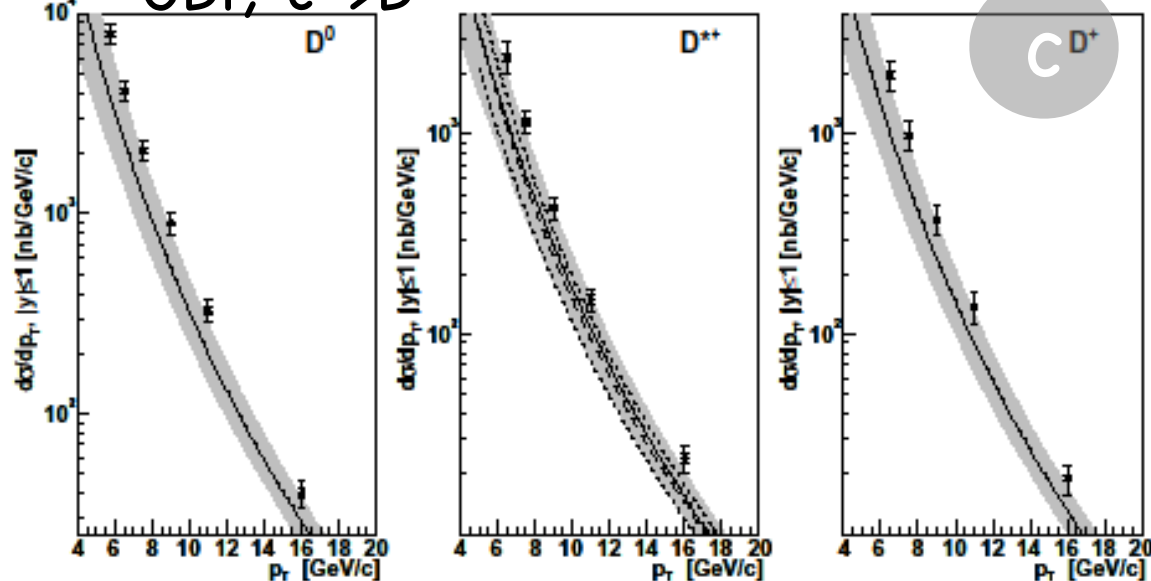
## CDF, $b \rightarrow B \rightarrow J/\psi$



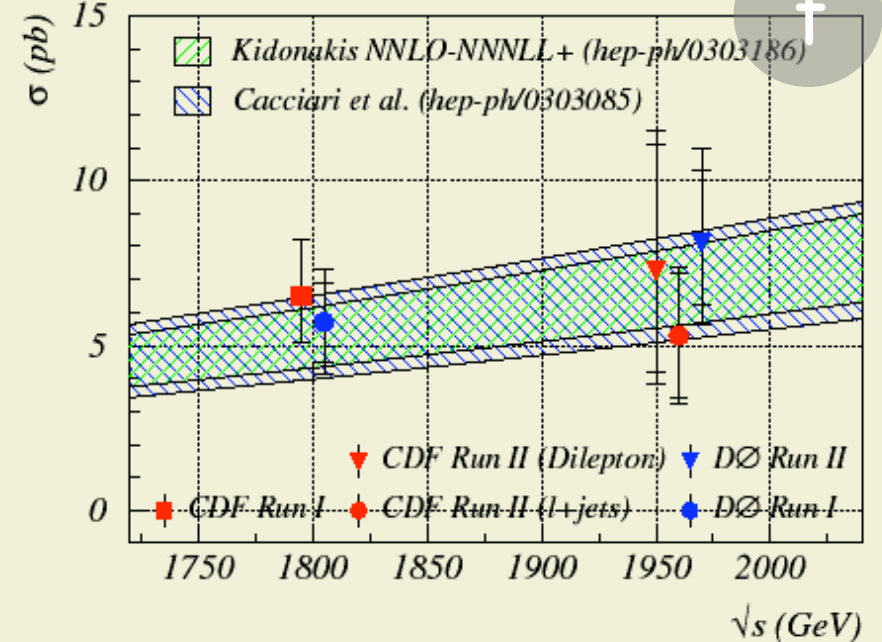
## ZEUS $b \rightarrow B \rightarrow$



## CDF, $c \rightarrow D$



## CDF and DØ Run II Preliminary





These examples qualify for the 'successfulness' test:

- the measurements contain little or no MonteCarlo extrapolation or deconvolution, at least compared to the final expt. error. This should avoid the possibility of biasing an experimental measurement with a theoretical prejudice (e.g. a MC calculation)
- the calculations are all massive and accurate at least to NLO
- the inclusion of non-perturbative information (where needed) has been performed in a minimal and self-consistent way
- the theoretical uncertainties have been explored in a reasonably exhaustive manner

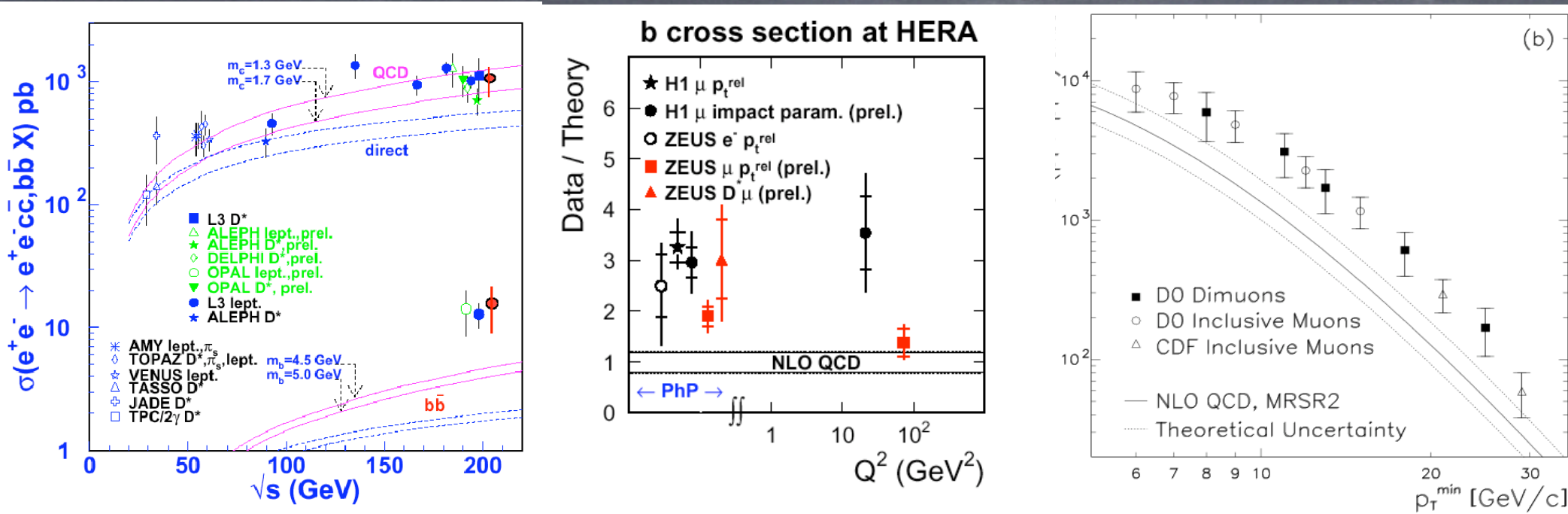
OK, so, the Standard Model is in agreement with the data.....



What's the big deal?!?



Until recently, a much bleaker picture was being presented



While for charm (large th. unc.) and for top (large expt. unc.) agreement was found, for bottom production discrepancies of 'a factor of three' or so were typically quoted in  $\gamma\gamma$ ,  $\gamma p$  and  $pp$

Let's look at these comparisons in detail

NB: the hadroproduction part of this talk draws generously from a seminar that M.L. Mangano gave at Fermilab in January. His full talk, with many more details, can be found at <http://cern.ch/~mlm/talks/Bcrossection.pdf>



It's worth remembering that most of the perturbative QCD ingredients have been available for some time now:

## Hadroproduction

Nason, Dawson, Ellis, NP B327 (1989) 49, NP B303 (1988) 607

Beenakker, van Neerven, Meng, Schuler, Smith, NP B351 (1991) 507

## Photoproduction

Nason, Ellis, NP B312 (1989) 551

Smith, van Neerven, NP B374 (1992) 36

## $\Upsilon\Upsilon$

Drees, Kraemer, Zunft, Zerwas, PL B306 (1993) 371

## Collinear resummation

Mele, Nason, NP B361 (1991) 626

MC, Greco, NP B421 (1994) 530

## Threshold resummation

Bonciani, Catani, Mangano, Nason, NP B529 (1998) 424



NLO  
(massive)

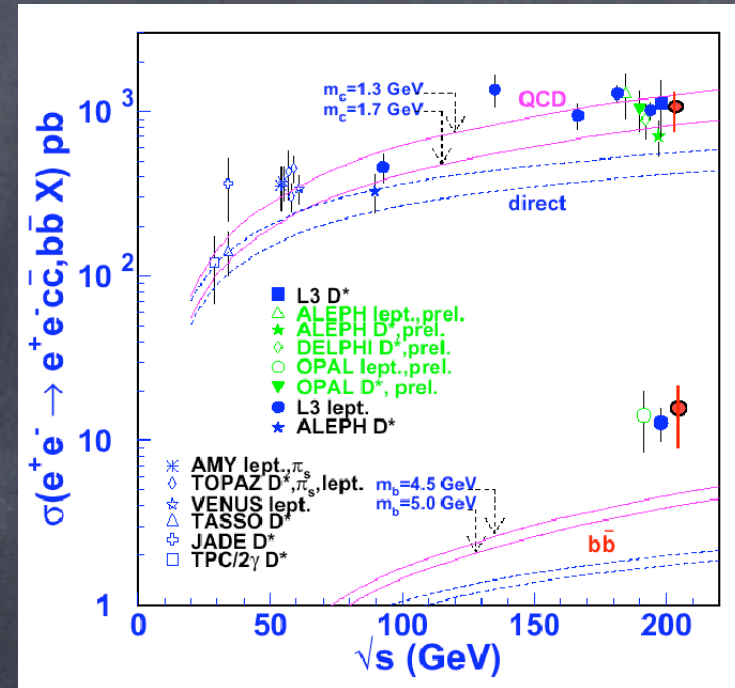


NLL

+ surely many others. Apologies to those I forgot.



# $\mathbb{1} \rightarrow Q\bar{Q}$ @ LEP2



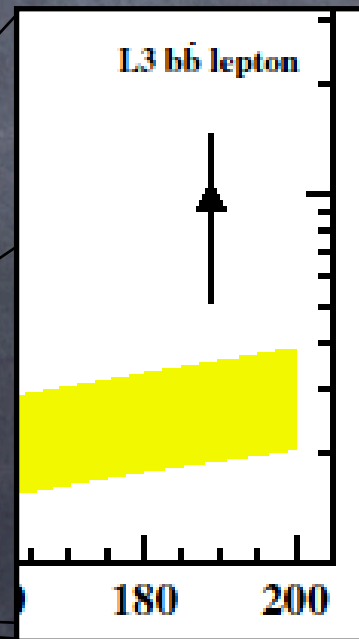
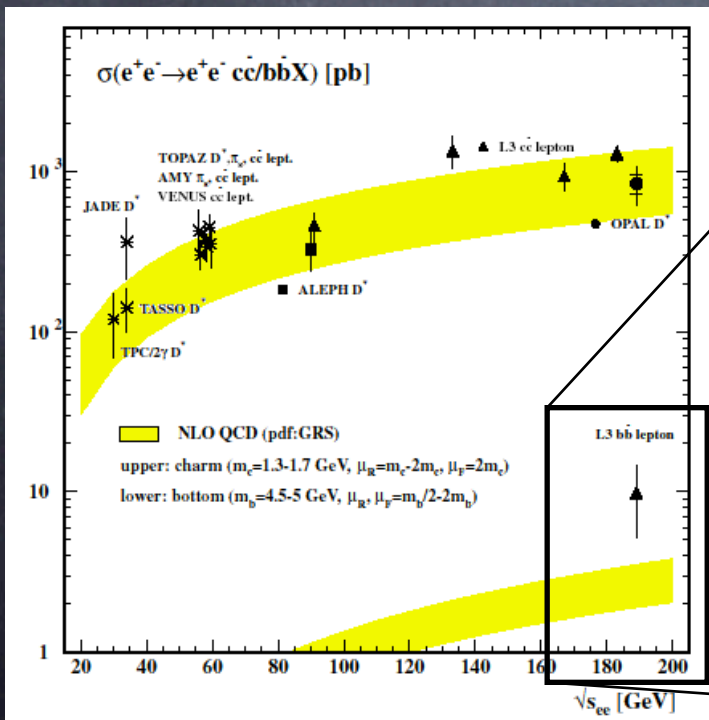
Good agreement  
for charm

Large apparent  
discrepancy  
for bottom

L3, OPAL and DELPHI report  
a factor of three excess  
over NLO QCD predictions

## Latest comprehensive theoretical review

S. Frixione, M. Krämer and E. Laenen  
[J. Phys. G: Nucl. Part. Phys. 26 (2000) 723]



4 pb  
2 pb

Full estimate of  
theoretical uncertainty  
slightly larger than shown on  
experimental plots



Measurements of the cross sections for open charm and beauty production in  $\gamma\gamma$  collisions at  $\sqrt{s} = 189\text{--}202$  GeV

L3 Collaboration

# L3 1999–2001

[Phys. Lett. B503 (2001) 10]

## Abstract:

measured and compared to next-to-leading order perturbative QCD calculations. The cross section of b production is measured in  $\gamma\gamma$  collisions for the first time. It is in excess of the QCD prediction by a factor of three. © 2001 Published by Elsevier

### Expt.

$$\sigma(e^+e^- \rightarrow e^+e^-b\bar{b}X)_{\text{combined}} = 13.1 \pm 2.0(\text{stat}) \pm 2.4(\text{syst}) \text{ pb.}$$

### Theory

open beauty threshold energy is set to 10.6 GeV. For  $\langle\sqrt{s}\rangle = 194$  GeV and a b quark mass of 4.5 GeV, this cross section is 4.4 pb. The  $b\bar{b}$  cross section is

Theoretical uncertainties?

Recent update:

$$\sigma(e^+e^- \rightarrow e^+e^-b\bar{b}X)_{\text{combined}} = 12.8 \pm 1.7(\text{stat}) \pm 2.3(\text{syst}) \text{ pb}$$

## Conclusions:

this cross section is 4.4 pb. The  $b\bar{b}$  cross section is measured in  $\gamma\gamma$  collisions for the first time and is a factor of 3 and about 4 statistical uncertainty standard deviations higher than expected.

All in all, data and theory are fairly compatible at the 3-sigma level. Claiming a “factor of three excess” in the abstract is perhaps a little premature....

*Rumours of my death have been greatly exaggerated. --Mark Twain*



# OPAL 2000 [OPAL-Note PN 455 (2000)]

Expt.

$$\sigma(e^+e^- \rightarrow e^+e^-b\bar{b}) =$$

$$14.2 \pm 2.5 \text{ (stat)} \pm 4.8 \text{ (sys)} \text{ pb.}$$

Theory

massive b quarks [5], with the direct contribution shown separately. The prediction of the NLO calculation for the total cross-section at  $\sqrt{s_{ee}} = 200 \text{ GeV}$  is 3.88 pb and 2.34 pb for a b quark mass of 4.5 GeV and 5.2 GeV, respectively, significantly lower than both measurements. A recent measurement of the open beauty cross-

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## DELPHI 2002

$$\sigma_{b\bar{b}} = 14.9 \pm 3.3 \text{ (stat)} \pm 3.4 \text{ (syst)} \text{ pb} \quad (\text{Muon } p_T\text{-rel.})$$

$$\sigma^{b\bar{b}} = 11.4 \pm 4.5 \text{ pb} \quad (\text{Muon } p_T\text{-rel.} + \text{K-lepton charge corr.})$$

---

Results from L3, DELPHI and OPAL fully compatible.

Unfortunately, only L3 has published its analysis in final form.

NB: all three collaborations used PYTHIA for extracting the b signal (with the same technique) and also for extrapolating from the cuts to the full space.

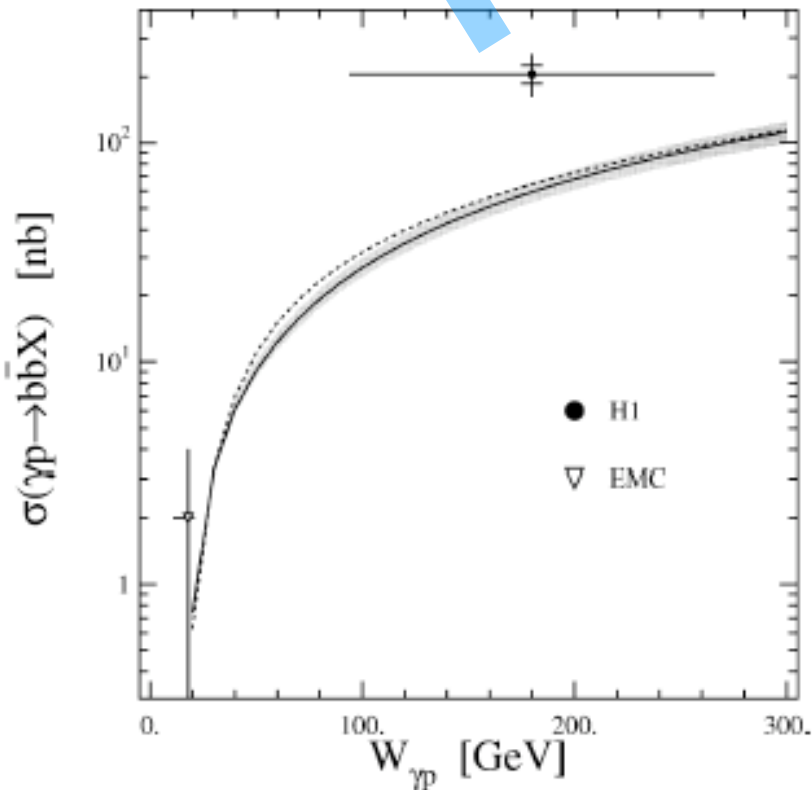
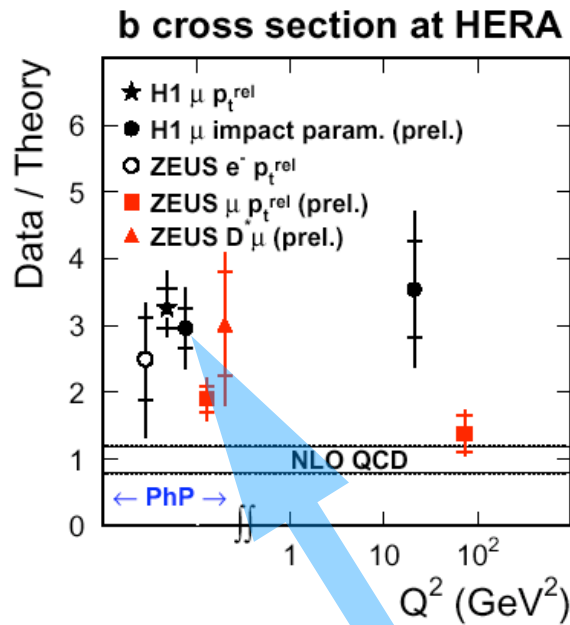
The three measurements are therefore strongly correlated.

Plea: could ALEPH do it? In a different way? Publishing visible cross sections?

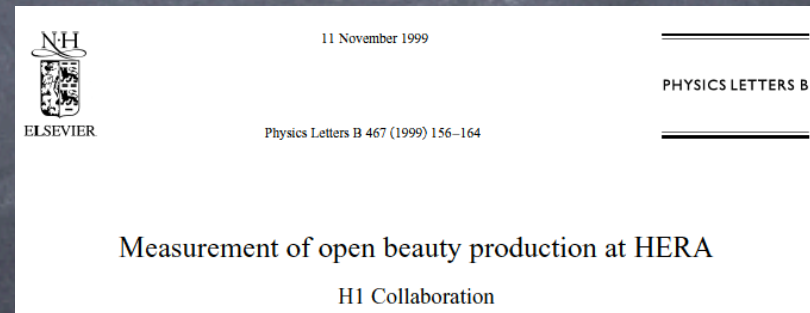


# Bottom Photoproduction

First measurements at HERA apparently showed fairly large discrepancies



H1 1999 [Phys. Lett. B467 (1999) 156]



180 GeV, respectively. The measured cross sections are higher than the expectation based on a NLO QCD calculation.



# ZEUS 2001 [Eur. Phys. J. C18 (2001) 625]

Eur. Phys. J. C 18, 625–637 (2001)  
Digital Object Identifier (DOI) 10.1007/s100520100571

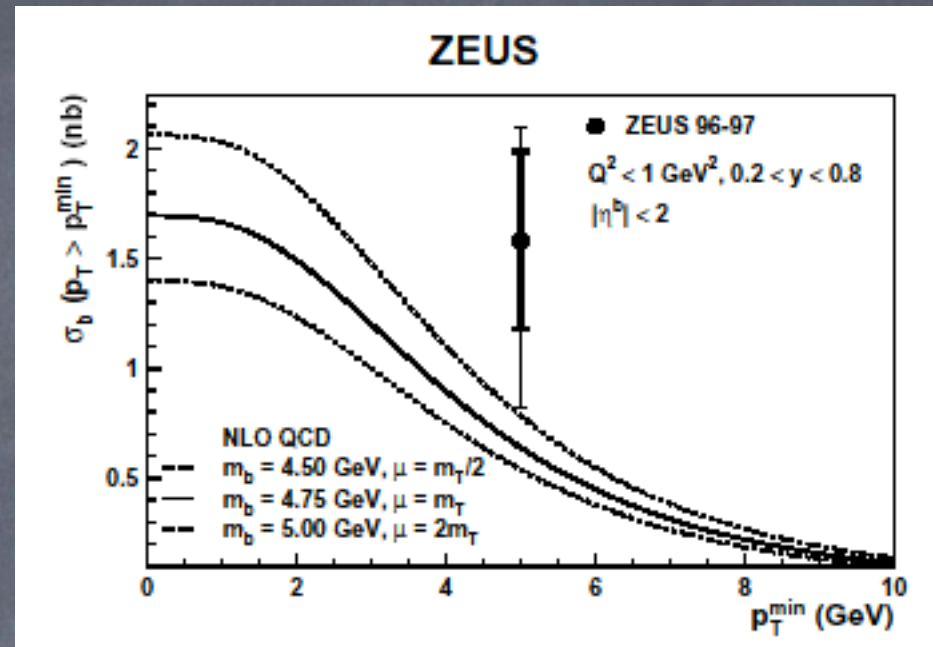
THE EUROPEAN  
PHYSICAL JOURNAL C  
Società Italiana di Fisica  
© Springer-Verlag 2001

## Measurement of open beauty production in photoproduction at HERA

The ZEUS Collaboration

The extrapolated cross section lies somewhat above the central NLO prediction, consistent with the general observation that NLO QCD calculations underestimate beauty production both in hadroproduction [4–6] and photoproduction at HERA [3].

H1 1999



# ZEUS 2003 [hep-ex/0312057]

## Introduction

ZEUS 2001

Beauty production cross section has been measured in  $p\bar{p}$  collisions at the ISR [2],  $Spp\bar{S}$  and Tevatron colliders [4], in  $\gamma\gamma$  interactions at LEP [5] and in fixed-target  $\pi N$  [6] and  $pN$  [7] experiments. Apart from the  $Spp\bar{S}$  data and the fixed-target experiments, the results were significantly above the NLO QCD prediction. The H1 measurement in  $ep$  interactions at HERA [8] found a cross section significantly larger than the prediction. The previous ZEUS measurement [9] was above, but consistent with, the prediction.

## Conclusions

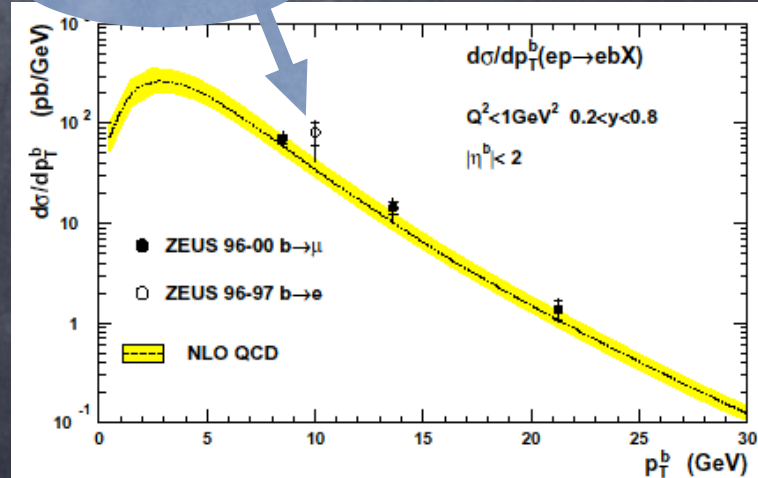
The large excess of the first measurement of beauty photoproduction over NLO QCD, reported by the H1 collaboration [8], is not confirmed. The present result is consistent with the previous ZEUS measurement using semi-leptonic B decays into electrons [9]. Beauty photoproduction in  $ep$  collisions is reasonably well described both by NLO QCD and by a MC model that includes a substantial flavour excitation component.

DESY-03-212  
December 2003

Beauty photoproduction measured using decays into muons in dijet events in  $ep$  collisions at  $\sqrt{s} = 318 \text{ GeV}$

ZEUS 2001

ZEUS Collaboration





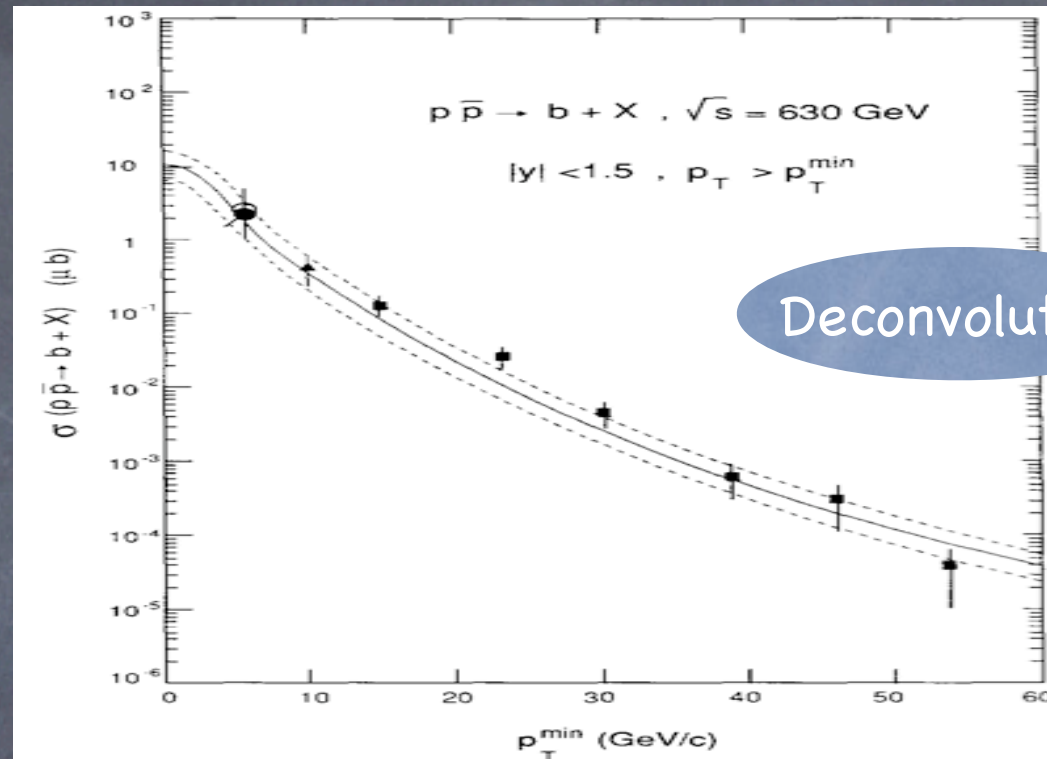
# Bottom production in $p\bar{p}$ collisions

UA1 1988-1991

UA1, PL B213 (1988) 405

UA1, PL B256 (1991) 121

UA1/QCD  $\sim 1$



CDF 1992

PRL 68 (1992) 3403

$$\sigma(\bar{p}p \rightarrow B^- X; P_T > 9.0 \text{ GeV}/c, |y| < 1.0)$$

$$= 2.8 \pm 0.9(\text{stat}) \pm 1.1(\text{syst}) \mu\text{b}.$$

Deconvoluted!

$$\sigma(pp \rightarrow bX; P_T > 11.5 \text{ GeV}, |y| < 1):$$

$$\text{CDF} = 6.1 \pm 1.9 \pm 2.4 \text{ b}$$

$$\text{theory} = 1.1 \pm 0.5 \text{ b}$$

tion. Our measurement is approximately 1.6 standard deviations above the theoretical calculation.



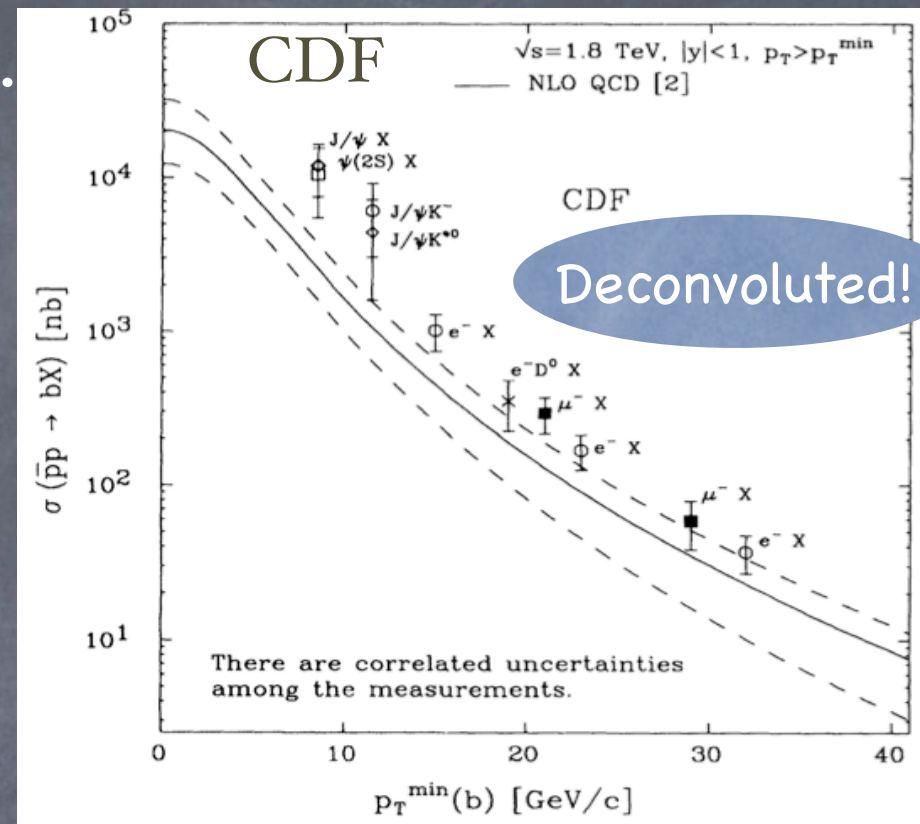
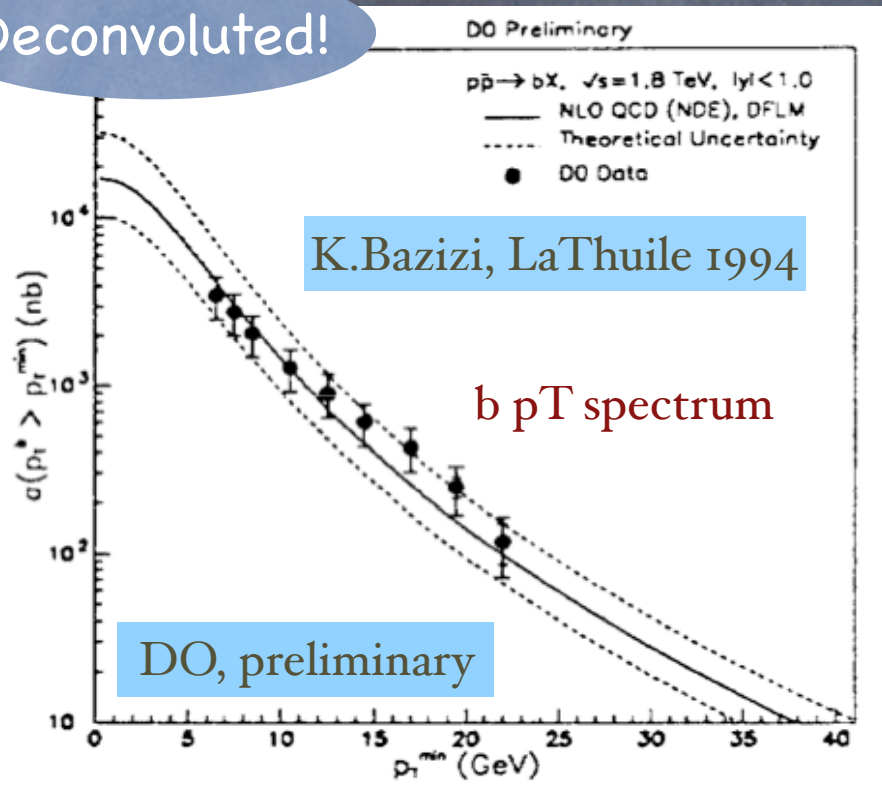
The 'usual' plot enters the stage....

## CDF 1993

PRL 71 (1993) 500, PRL 71 (1993) 2396

agreement within the experimental errors. This result supports the conclusion of previous CDF analyses that the next-to-leading order QCD calculation tends to underestimate the inclusive  $b$ -quark cross section.

Deconvoluted!



D0 finds however no excess at this stage: consistent with QCD, barely consistent with CDF



“Real” observables are also measured:

CDF 1995

PRL 75 (1995) 1451

B mesons, NOT deconvoluted  
to b quark level

However, how is the theoretical  
predictions for B mesons calculated?

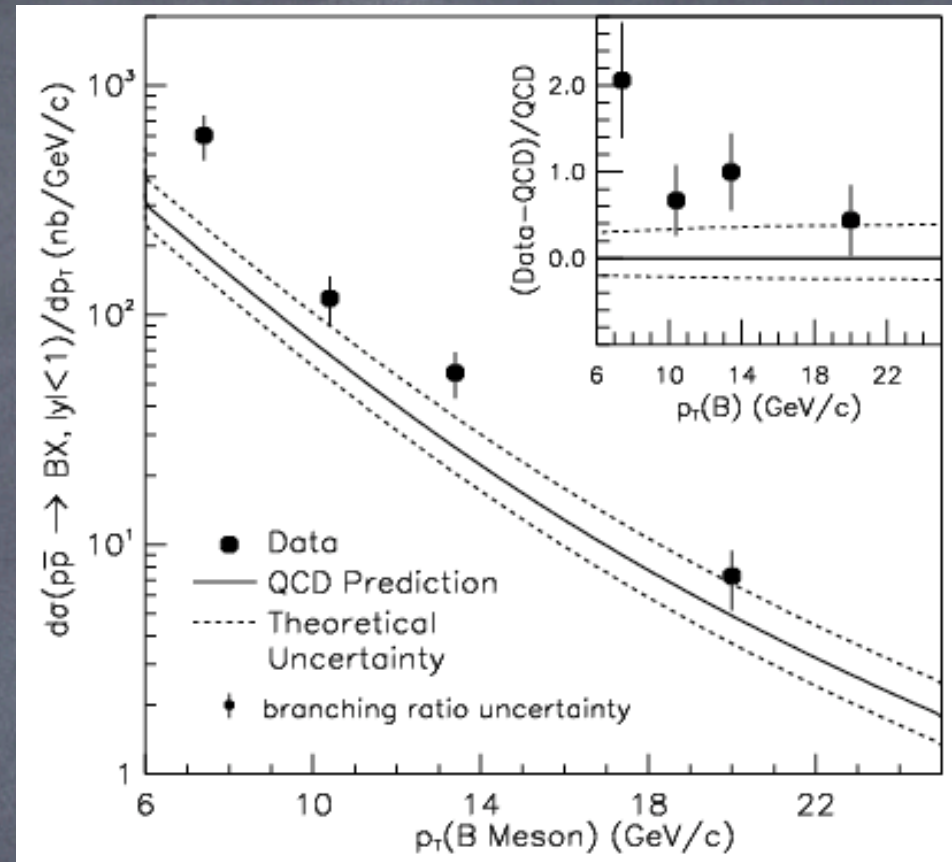


Fig. 2. To determine the level of agreement between the data and the theoretical prediction, the predicted cross section is fitted to the measurements, holding the shape constant and varying the magnitude. The fit yields an overall scale factor of  $1.9 \pm 0.2 \pm 0.2$ , with a confidence level of 20%. In conclusion, we find that the shape of the  $B$  meson differential cross section presented here is adequately described by next-to-leading order QCD, while the absolute rate is at the limits of that predicted by typical variations in the theoretical parameters. It will be interesting

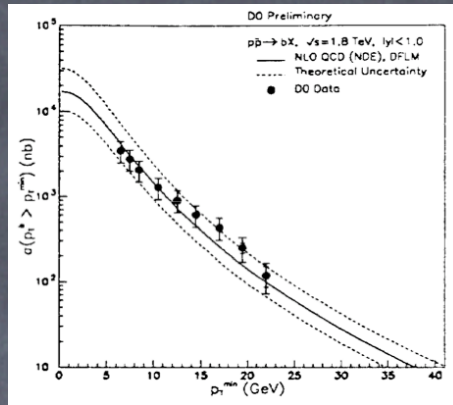
The possible 'disagreement' between  
data and theory is quantified for  
the first time



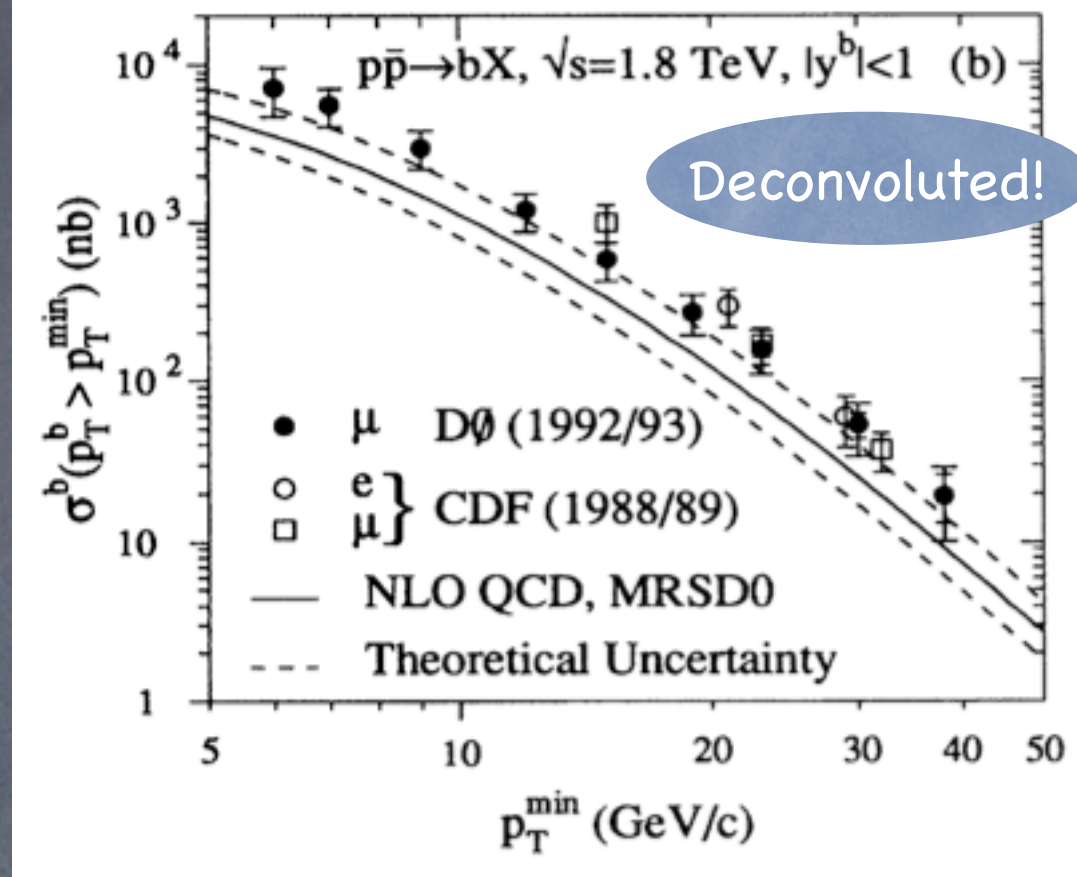
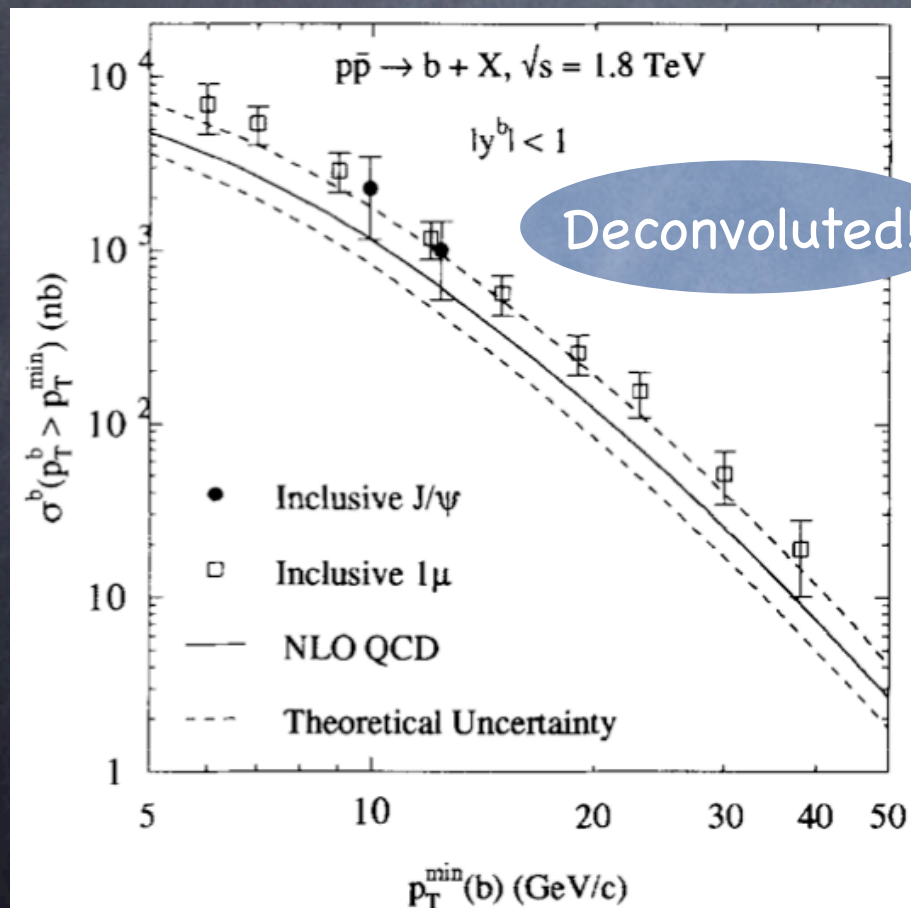
# D0 1995-1996

PRL 74 (1995) 3548

PL B370 (1996) 239



The final D0 data become more CDF-like. However, they are still compatible with NLO QCD



Conclusions:

tion. Our measurement indicates that, within theoretical uncertainties, the NLO QCD description [1] of heavy flavor production in  $p\bar{p}$  at  $\sqrt{s} = 1.8 \text{ TeV}$  is adequate for the kinematic range  $|y^b| < 1.0$  and  $p_T^b > 6 \text{ GeV}/c$ .



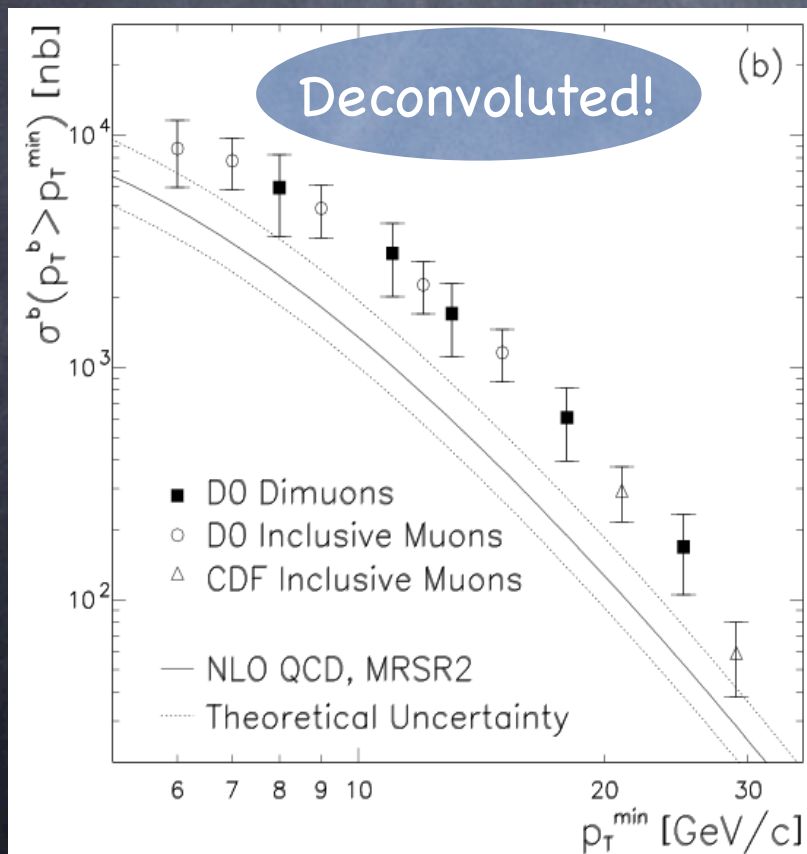
A few years later, the data (or the attitude?) change....

Despite the conclusions of the previous paper ("adequate description"), the previously measured  $b$  cross section is now considered "systematically larger" in the Introduction:

DO 1999–2000

PL B487 (2000) 264

Measurements of the  $b$  quark production cross section and  $b\bar{b}$  correlations in  $p\bar{p}$  collisions provide an important test of perturbative quantum chromodynamics (QCD) at next-to-leading order (NLO). The measured  $b$  quark production cross section at  $\sqrt{s} = 1.8$  TeV [1–4] is systematically larger than the central values of the NLO QCD predictions [5,6].



This, of course, helps accepting the conclusion that the new data show now a considerable excess:

## Conclusions

as described above and is dominated by the variation of the scales. The ratio of the data to the central NLO QCD prediction is approximately three over the entire  $p_T^{\min}$  range covered.

approximately three over

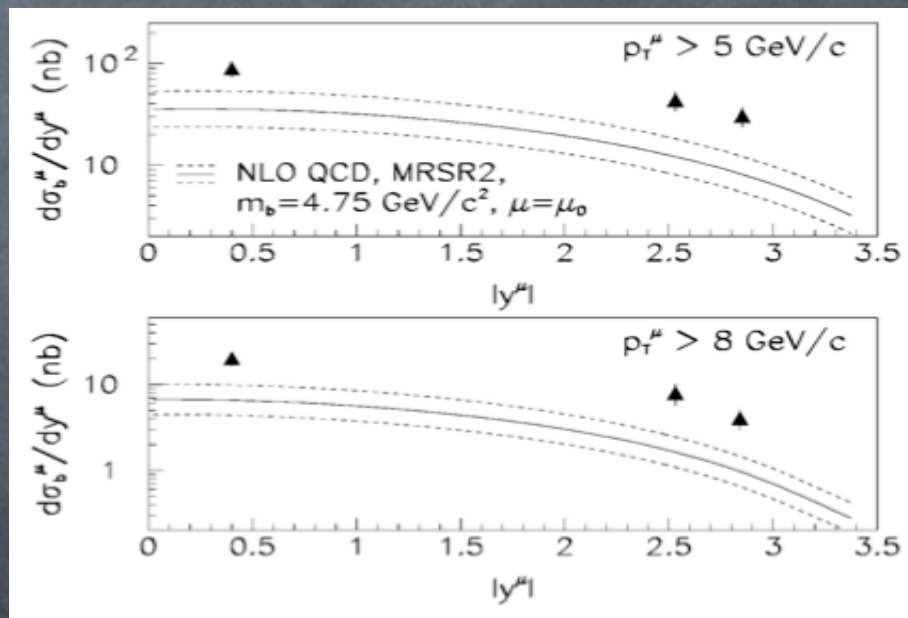
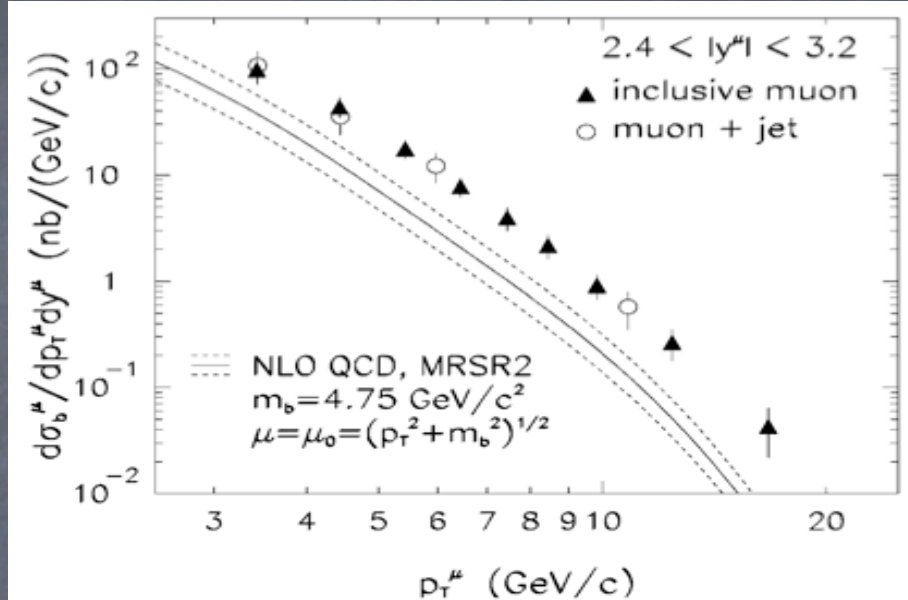


# Forward muons from b decay

Not quite: TH  
systematics not included

TABLE II. The cross section of muons from  $b$ -quark decay compared to NLO QCD. Errors are statistical and systematic added in quadrature.

$p_T^\mu > 5 \text{ GeV}/c$				
Rapidity	$\langle y \rangle$	Measured Theory		Ratio
		$\sigma_b^\mu \text{ (nb)}$	$\sigma_b^\mu \text{ (nb)}$	
0.00–0.80	0.40	$89 \pm 16$	36	$2.5 \pm 0.4$
2.40–2.65	2.53	$43.5 \pm 9.4$	12	$3.6 \pm 0.8$
2.65–3.20	2.85	$30.5 \pm 6.6$	8.4	$3.6 \pm 0.8$
$p_T^\mu > 8 \text{ GeV}/c$				
Rapidity	$\langle y \rangle$	Measured Theory		Ratio
		$\sigma_b^\mu \text{ (nb)}$	$\sigma_b^\mu \text{ (nb)}$	
0.00–0.80	0.40	$20.1 \pm 3.7$	6.6	$3.0 \pm 0.6$
2.40–2.65	2.53	$7.9 \pm 2.2$	1.6	$4.8 \pm 1.3$
2.65–3.20	2.84	$4.1 \pm 1.1$	0.99	$4.0 \pm 1.1$



## Abstract & Conclusions:

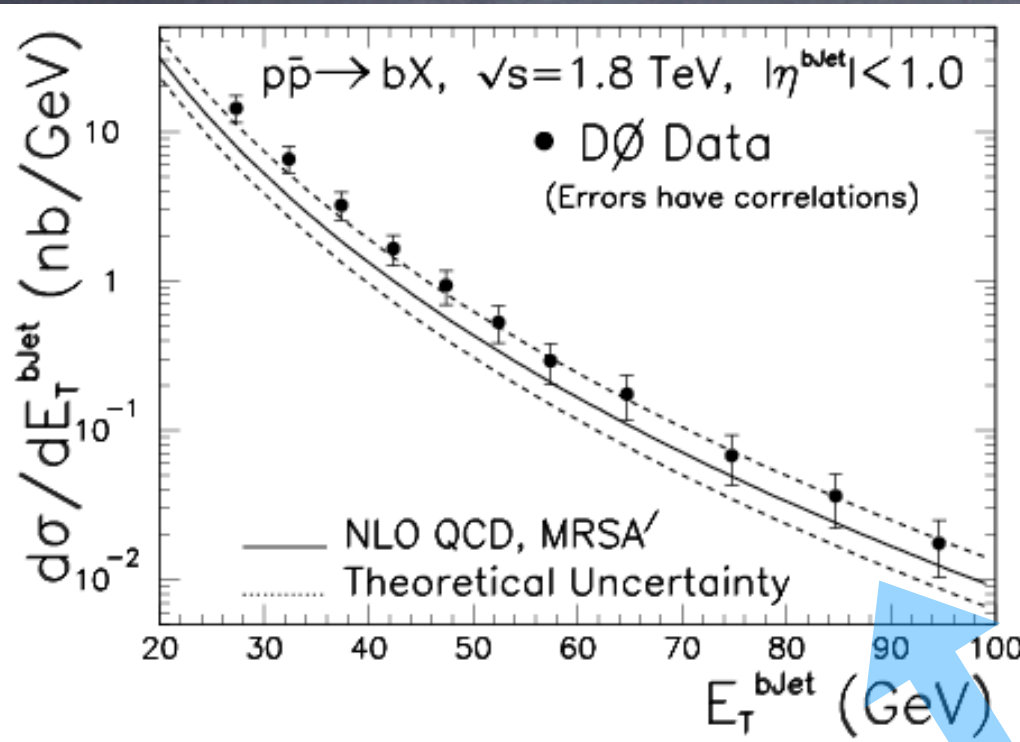
analysis were collected by the D0 experiment at the Fermilab Tevatron. We find that next-to-leading-order QCD calculations underestimate  $b$ -quark production by a factor of 4 in the forward rapidity region.



# D0 2000

PRL 85 (2000) 5068

Most recent D0 results:  
b-jets and large  $p_T$  b-quarks



b-jets are observable quantities:  
no need for a deconvolution

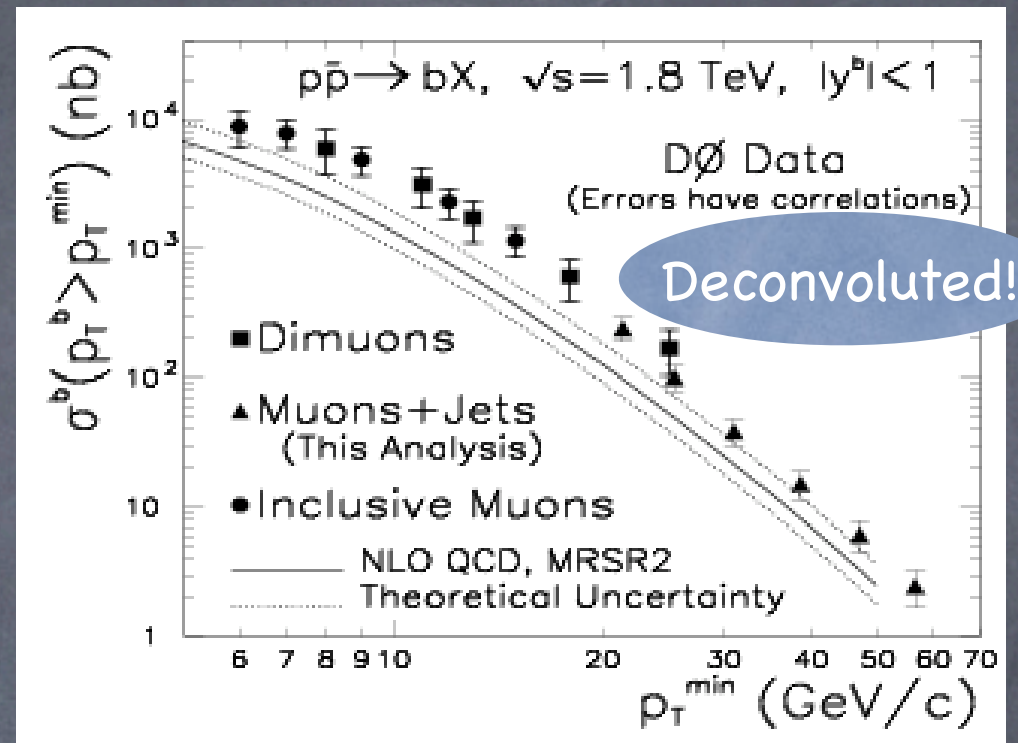


Figure 2 displays the same general pattern of past  $b$  production measurements [4–11], with data lying above the central values of the prediction, but comparatively less so in the present case, where general agreement between measurement and the upper band of the theoretical uncertainty is observed.

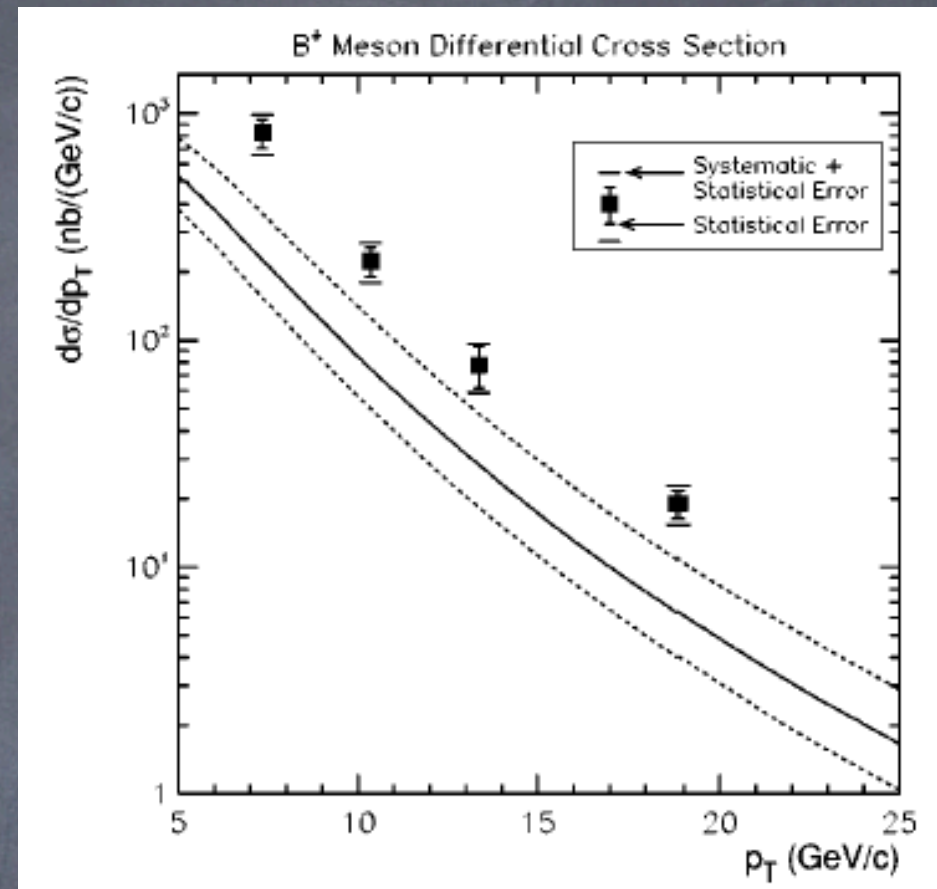
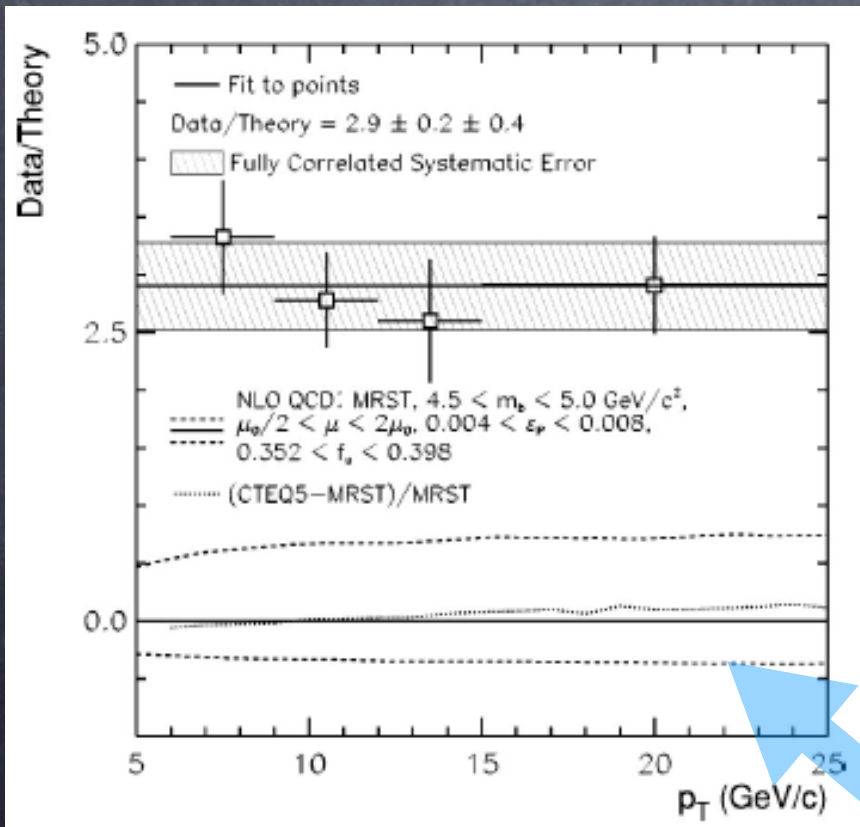


# CDF 1998–2002

PRL 85 (2002) 5068

Last CDF Run I result:  
B mesons, superseding 1995 result

Data/Theory ratio



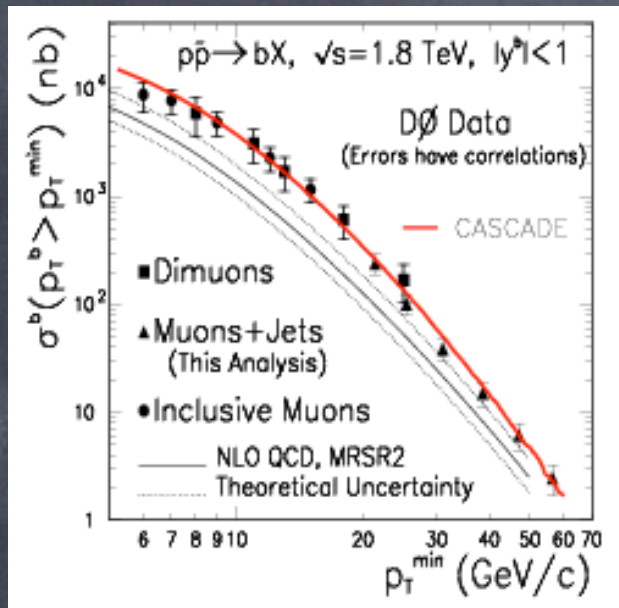
ainties. The differential cross section is measured to be  $2.9 \pm 0.2$  (stat $\oplus$ syst $_{p_T}$ )  $\pm 0.4$  (syst $_{fc}$ ) times higher than the NLO QCD predictions with agreement in shape. The first

However, once more, the theoretical uncertainty is not included in the error on the ratio

BTW: being the data points a ratio, shouldn't this band better be around 1 and not 0 !?!



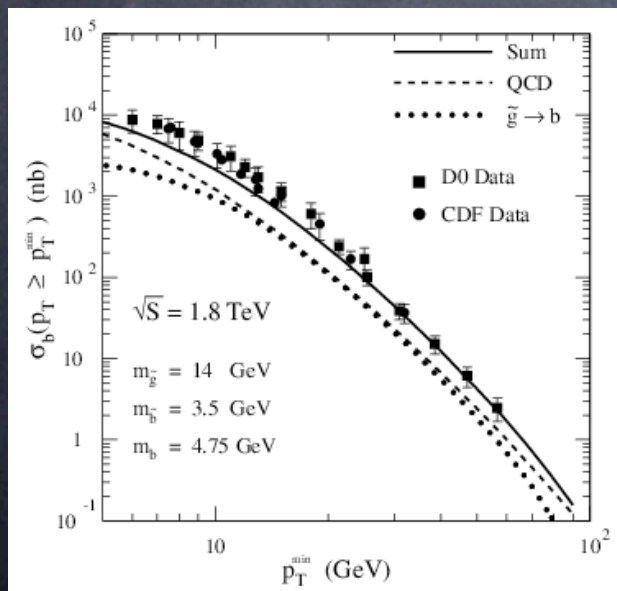
By the years 2001–2002, lots of discrepant data.  
Proposed explanations range from the semi-conventional....



H. Jung, CASCADE, [Phys. Rev. D65 (2002) 034015]

MC implementation of small- $x$  dynamics, following CCFM  
Main criticism: lack of control of NLO effects

....to the very exotic ones:



Berger, Harris, Kaplan, Sullivan, Tait, Wagner  
PRL 86 (2001) 4231

standard model (MSSM) [3]. We postulate the existence of a relatively light gluino  $\tilde{g}$  (mass  $\simeq 12\text{--}16$  GeV) that decays into a bottom quark and a light bottom squark  $\tilde{b}$  (mass  $\simeq 2\text{--}5.5$  GeV). The  $\tilde{g}$  and the  $\tilde{b}$  are the spin-1/2 and spin-0 supersymmetric partners of the gluon ( $g$ ) and bottom quark ( $b$ ). In our scenario the  $\tilde{b}$  is either long-lived or decays hadronically. We obtain good agreement with hadron collider rates of bottom-quark production. Several



# Theoretical ingredients of a VCE

## (Very Conventional Explanation)

The prediction for the distribution of a 'real particle' ( $J/\psi$  or muon) can be obtained by convoluting:

- 1) the NLO (+ NLL = FONLL) calculation for  $b$  quarks
- 2) the fragmentation of the  $b$  quark into a  $B$  meson,  $f(b \rightarrow B)$
- 3) the decay of the  $B$  meson into the  $J/\psi$  or the muon

$$\frac{d\sigma(B)}{dp_T} = \frac{d\sigma(b)}{d\hat{p}_T} \otimes f(b \rightarrow B) \otimes g(B \rightarrow J/\psi)$$

For  $f(b \rightarrow B)$  the Peterson et al. form with  $\epsilon_b = 0.006$  is used in most experimental papers, following a determination by Chrin made in 1987 (sic) using charm data,  $\epsilon_b = m_c / m_b \epsilon_c$  rescaling, and LO Montecarlo calculations

Not being the  $b$  quark a physical particle,  $f(b \rightarrow B)$  cannot be a physical observable: its details depend on the perturbative calculation it is interfaced with. A single fragmentation function cannot do for all calculations



Around 1997 [MC, M. Greco, PRD 55 (1997) 7134, M.L. Mangano, lectures on HQ production, hep-ph/9711337] we started arguing that systematics related to fragmentation risked being underestimated, and called for a stricter consistency between HQ FF determination from  $e^+e^-$  data and their use elsewhere:

For one thing,  $\epsilon_b$  fitted within a NLO description is smaller than the usual 0.006 value. Hence, a harder Peterson will give a larger cross section in the  $p_T > m_b$  region

It was also noted that, due to the steeply falling spectrum of the partonic cross section, the transverse momentum distribution in hadronic collisions is sensitive to large moments of the FF, while it is the second moment,  $\langle z \rangle$ , which is mainly determined from  $e^+e^-$  data

$$\text{Assuming } \frac{d\sigma}{d\hat{p}_T} \sim \frac{1}{\hat{p}_T^N} \quad \text{we get} \quad \frac{d\sigma}{dp_T} \sim \int \frac{dz}{z} \left(\frac{z}{\hat{p}_T}\right)^N f(z) = f_N \frac{d\sigma}{d\hat{p}_T}$$

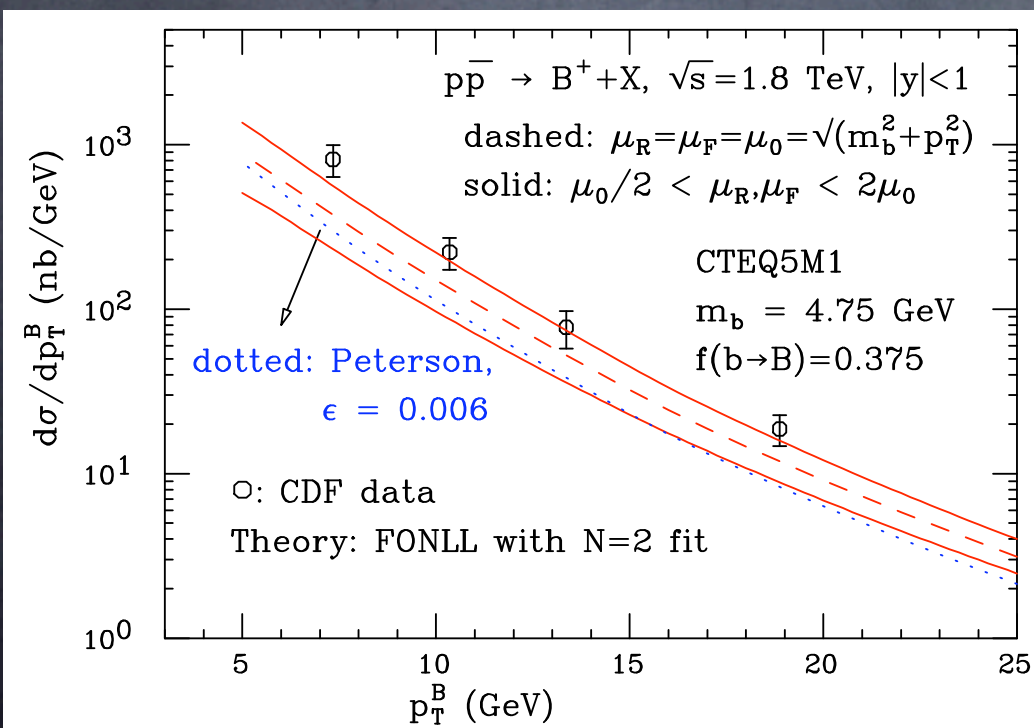
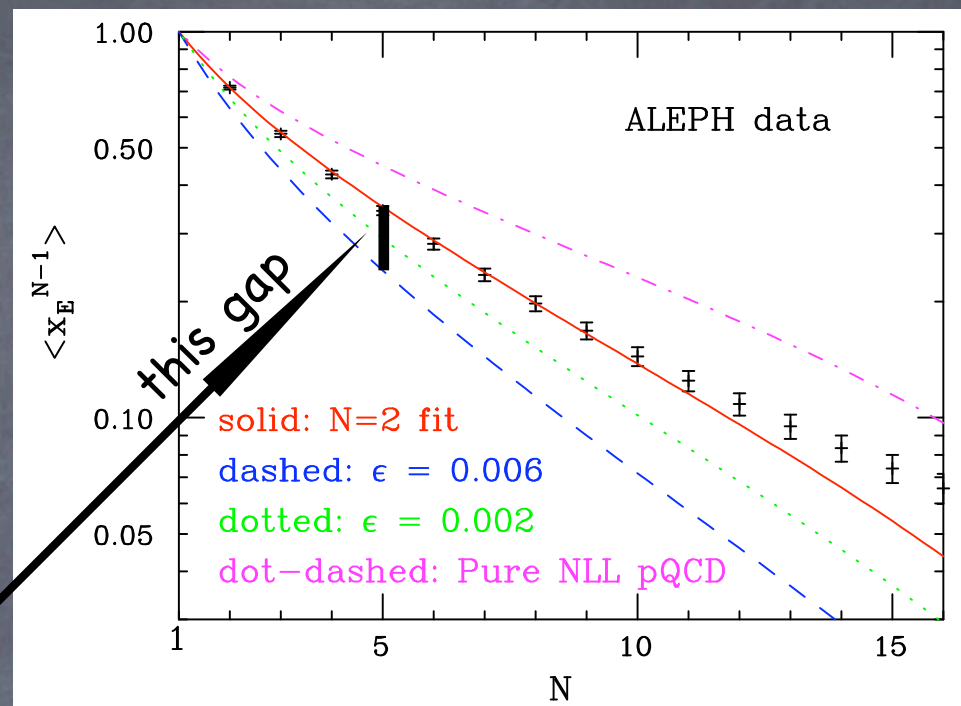
In proton-(anti)proton collisions  $N$  is of order 5. Therefore, a proper extraction of moments around this one from  $e^+e^-$  collisions is more important than a good description of the spectrum



From the year ~ 2000 accurate enough data on B fragmentation were finally available from LEP, allowing good fits up to  $N=10$  or so.

NB. NLL resummed pQCD calculation needed [B. Mele and P. Nason, Nucl. Phys. B361 (1991) 626]

Note that Peterson with  $\epsilon_b = 0.006$  underestimates the moments around  $N=5$ . Its use will consequently underestimate the B cross section

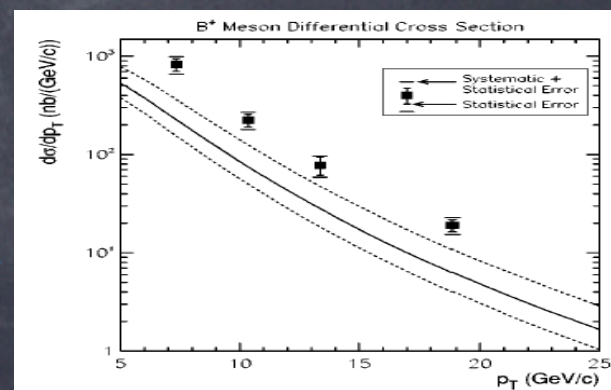


With these ingredients, a much better description of the B meson CDF data can be given:

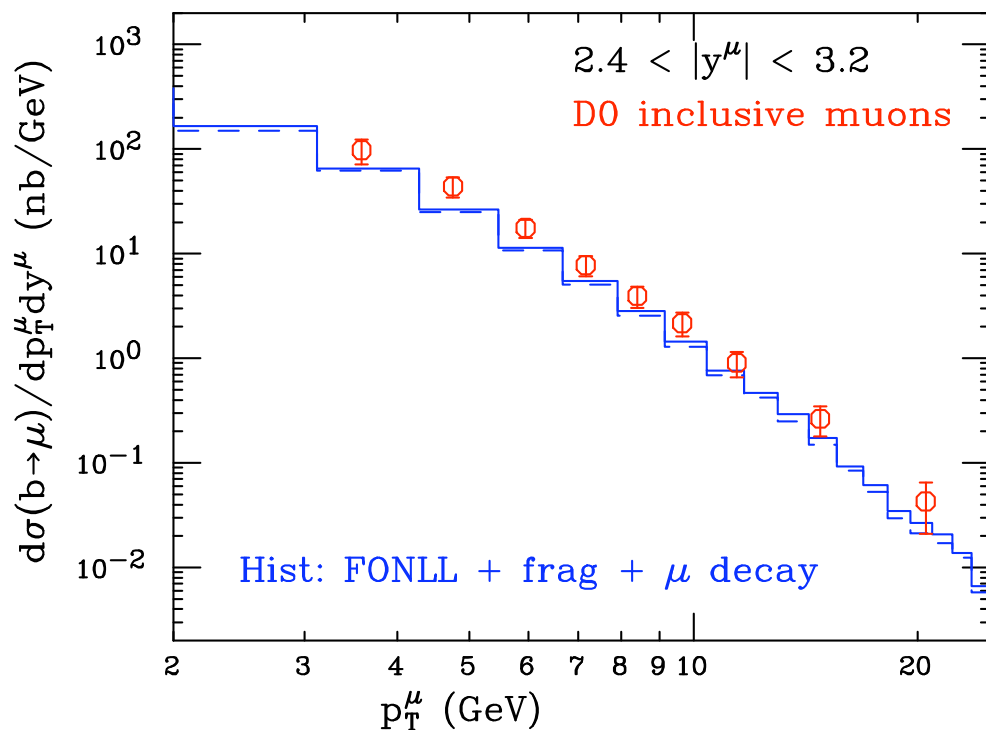
$$\text{Data/Theory} = 1.7 \pm 0.5 \text{ (expt.)} \pm 0.5 \text{ (th.)}$$

i.e. no significant discrepancy

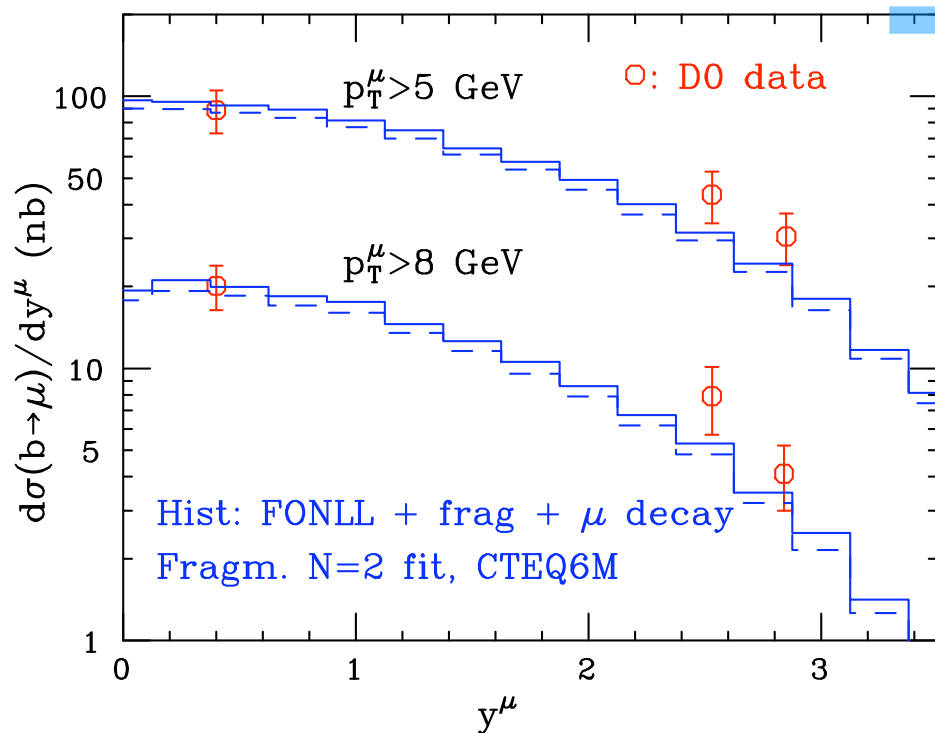
compare



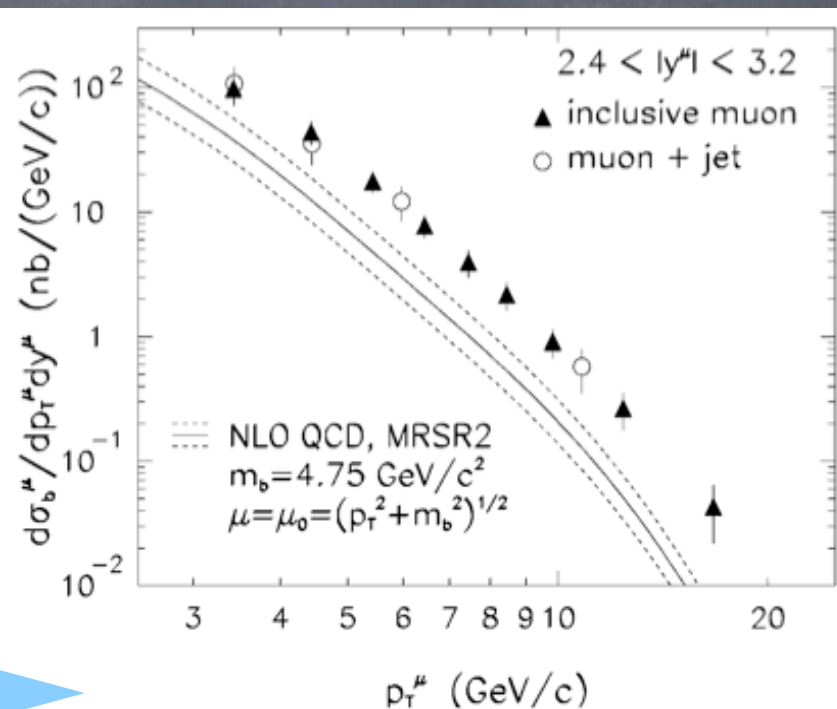
PRELIMINARY



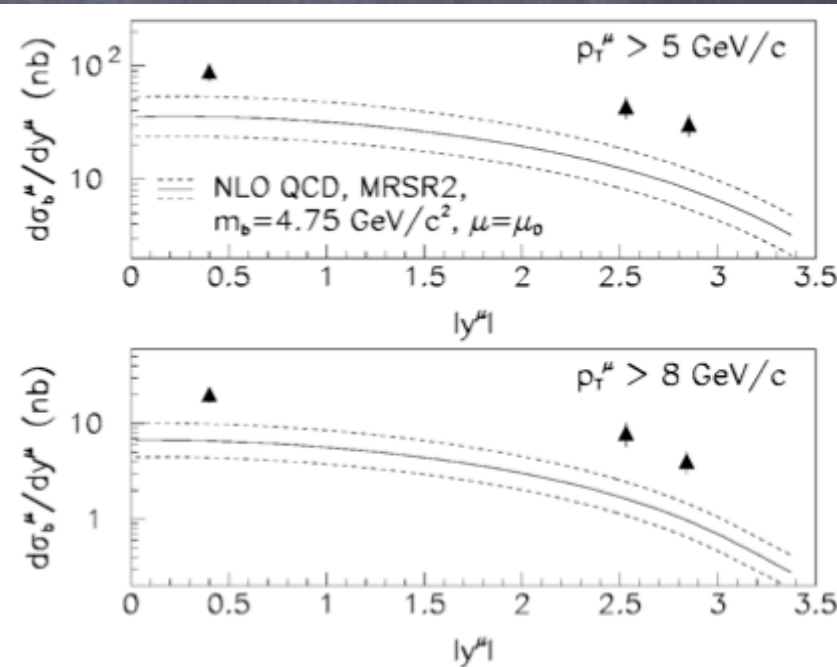
PRELIMINARY



D0 'forward muons from b' data are also now better described

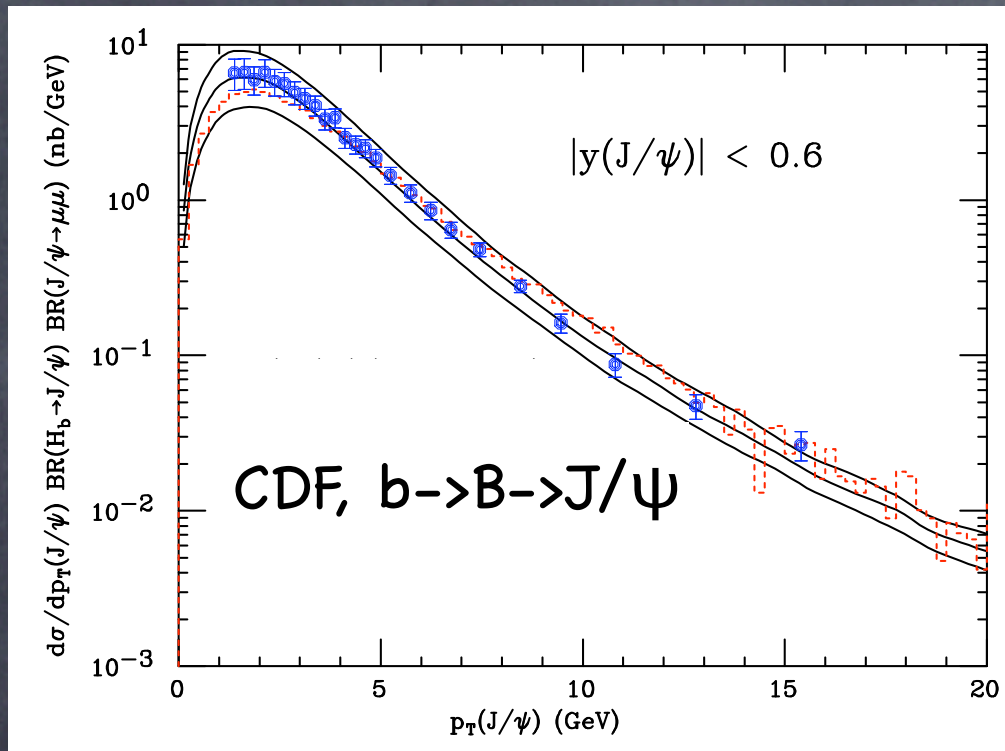


compare





# 2003: CDF Run II preliminary data at 1.96 TeV



MC, Frixione, Mangano, Nason, Ridolfi, hep-ph/0312132

$$\sigma(pp \rightarrow H_b \rightarrow \psi; P_{T\psi} > 1.25, |y| < 0.6)$$

$$\sigma_{J/\psi}^{\text{CDF}} = 19.9^{+3.8}_{-3.2 \text{ stat+syst}} \text{ nb}$$

$$\sigma_{J/\psi}^{\text{FONLL}} = 19.0^{+8.4}_{-6.0} \text{ nb}$$

$$\sigma(pp \rightarrow H_b X; P_T > 0, |y| < 0.6) \times B(H_b \rightarrow \psi)$$

$$\sigma_{H_b}^{\text{CDF}} = 24.5^{+4.7}_{-3.9 \text{ stat+syst}} \text{ nb}$$

$$\sigma_{H_b}^{\text{FONLL}} = 22.9^{+9.5}_{-6.8} \text{ nb}$$

$$\sigma(pp \rightarrow bX; P_T > 0, |y| < 1)$$

$$\sigma_b^{\text{CDF}}(|y| < 1) = 29.4^{+6.2}_{-5.4 \text{ stat+syst}} \mu\text{b}$$

$$\sigma_b^{\text{NLO}}(|y| < 1) = 23.6^{+11.9}_{-7.6} \mu\text{b}$$

Theory-Data agreement now almost embarrassing. Fully compatible within errors.

Central values move slightly apart as we go to more 'artificial' cross sections.  
Indication of uncertainties and systematics related to deconvolution procedures.



# So, what happened?

How did we go from 'factor of three' excesses to full agreement?

A combination of various factors:

- the real distance between data and theory was actually never this large, once ALL uncertainties were taken into account
- new measurements without corrections to unphysical particles (ZEUS, CDF) may have minimized the risk of biasing the data
- both the data and the theory have moved, often within the errors (which might have been larger than previously thought)
- new experimental input (and better use of some of them, e.g. bottom FF) allowed producing more reliable theoretical predictions

Examples ->

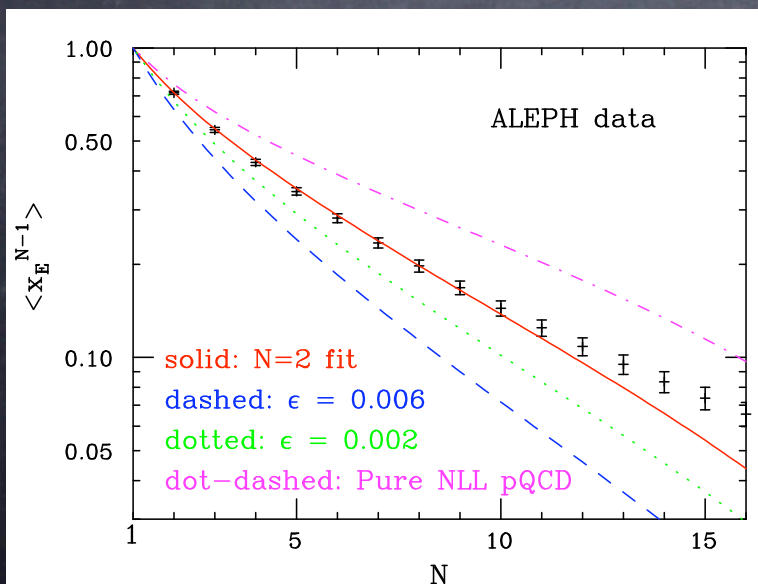
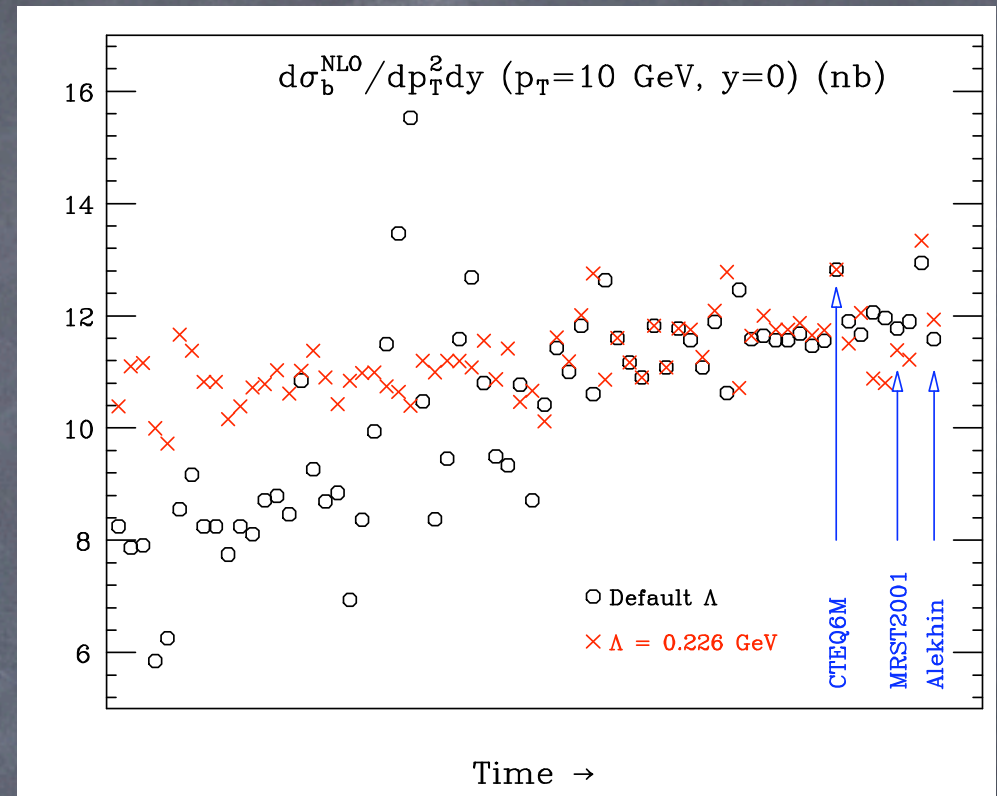


# PDFs

Exercise: calculate the b hadroproduction cross section with every PDF set which has ever been published

RESULT: even a factor of two from early sets to modern ones.

NB. a very large part of this discrepancy is due to the evolution of the value for  $\alpha_s$



# FFs

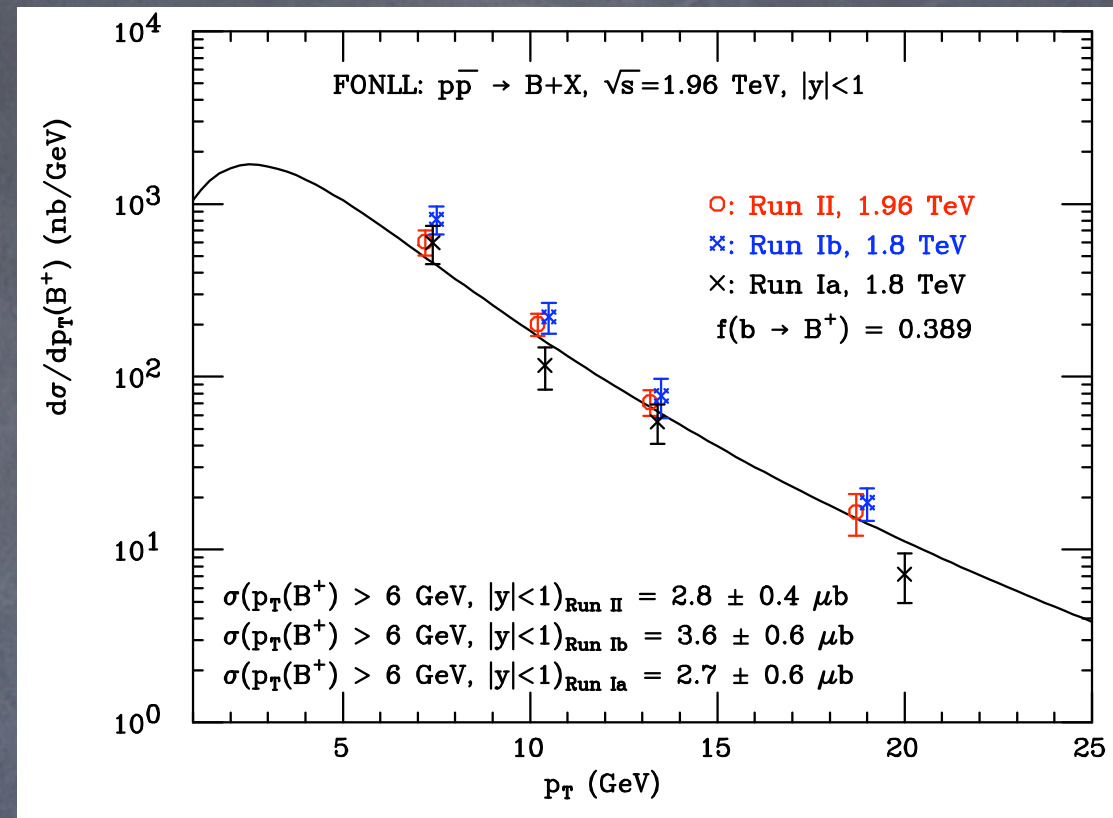
Switching from the usual Peterson with  $\epsilon_b = 0.006$  to a FF fitted in moment space increases the large- $p_T$  cross section by 40%.

This is the single most significant increase, and the one not simply due to improved experimental input.

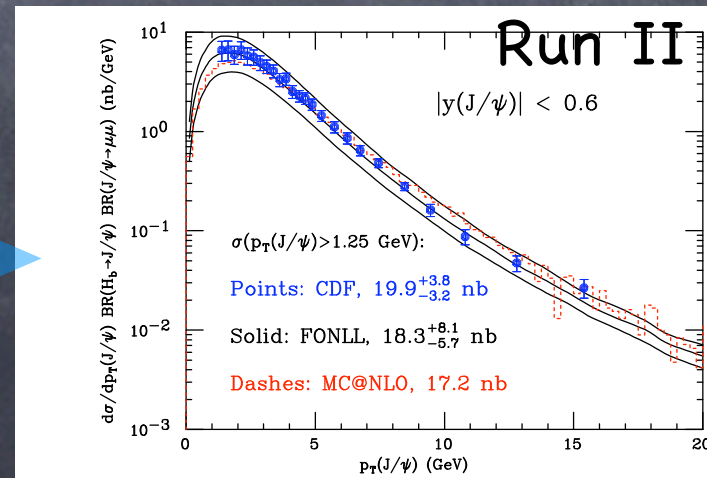
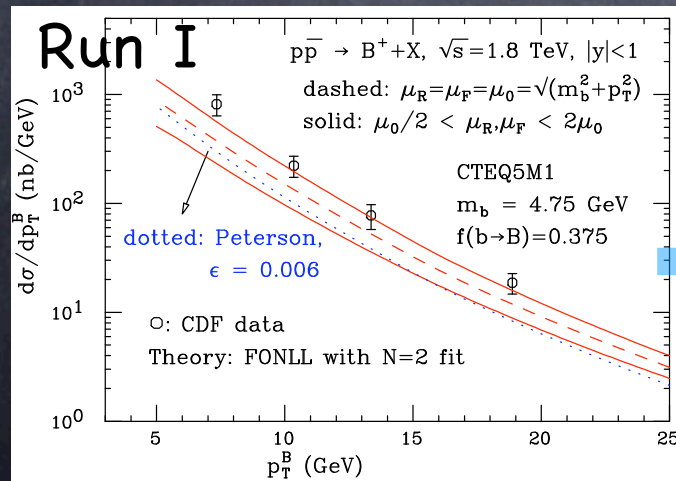
# Data

If the input from PDFs and the measurements and extraction of HQ FFs pushed the theory up, the data 'helped' coming down a little:

Compare Run II data to Run I ones:  
should be 10% higher, they are  
instead about 25% lower



This is the main reason why the same calculation which predicted a CENTRAL VALUE a factor of 1.7 lower than the CENTRAL VALUE of the data, is now in perfect agreement with Run II data



A further 15-20% is given  
by updates in the PDFs  
(CTEQ5M1 → CTEQ6M)



# Summarizing....

- the description of  $b$  production cross section by pQCD is not as bad as it appeared. Actually, it's pretty good.
- in part, the changes are due to theoretical improvements and to legitimate movements of experimental data/inputs within errors
- in part, the discrepancy was never as large and significant as said/written. Plotting 1-sigma errors only and discussing central value ratios forgetting errors altogether might lead to a distorted perception of reality

"Only astronomers use 1-sigma errors" (Licia Verde, yesterday's talk)  
Well.....

When a particle physicist has to be reminded by a cosmologist how to properly treat errors, you know that something is wrong...



# Conclusions

- NLO (+NLL) QCD does a good job in predicting real and unbiased observables. Part of the success is due to the possibility of controlling the whole chain from parton to hadron, carefully matching perturbative and non-perturbative contributions. Experiments should avoid publishing only deconvoluted/extrapolated quantities, which might include strong biases from MC
- New physics is not needed to explain most of the recent bottom production data, but there is still some room for it within the uncertainties
- Higher order calculations (years away anyway) or further resummations should not change the picture, but may help in reducing the theoretical uncertainties (e.g. small- $x$  effects for total  $b$  cross section at the Tevatron)