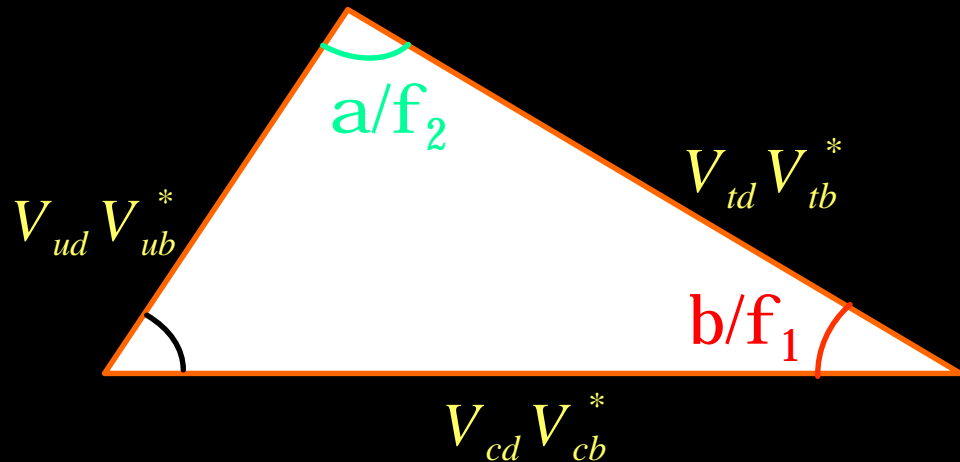


a and b at the *B* factories

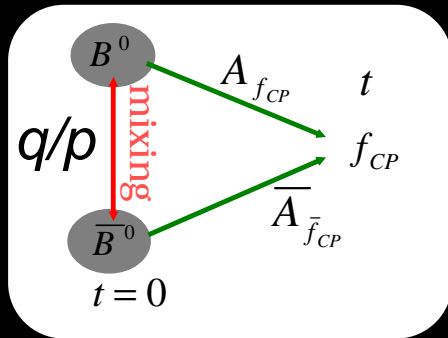
XX Rencontres de physique de la
Vallée d'Aoste - 9 Mar 2006

Giuseppe Finocchiaro
Laboratori Nazionali di Frascati



Preamble: time dependent measurements at the B factories

CPV can arise from interference between two paths, e.g. decay with and without mixing



Independent of phase convention

$$I_{f_{CP}} = \frac{q}{p} \cdot \frac{\bar{A}_{f_{CP}}}{A_{f_{CP}}} \leftarrow \text{amplitude ratio}$$

mixing

Time-dependent CP asymmetry:

$$A_{CP}(t) \equiv \frac{N(\bar{B}_{phys}^0(\Delta t) \rightarrow f_{CP}) - N(B_{phys}^0(\Delta t) \rightarrow f_{CP})}{N(\bar{B}_{phys}^0(\Delta t) \rightarrow f_{CP}) + N(B_{phys}^0(\Delta t) \rightarrow f_{CP})}$$

$$= S_{f_{CP}} \sin(\Delta m \Delta t) - C_{f_{CP}} \cos(\Delta m \Delta t)$$

$$S_{f_{CP}} = \frac{-2 \operatorname{Im} I_{f_{CP}}}{1 + |I_{f_{CP}}|^2}$$

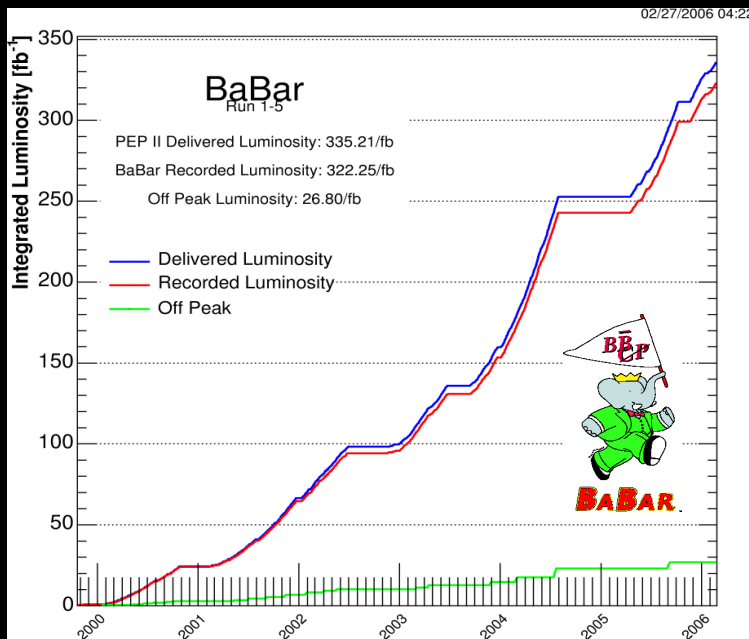
$$C_{f_{CP}} = \frac{1 - |I_{f_{CP}}|^2}{1 + |I_{f_{CP}}|^2}$$

Main ingredients:

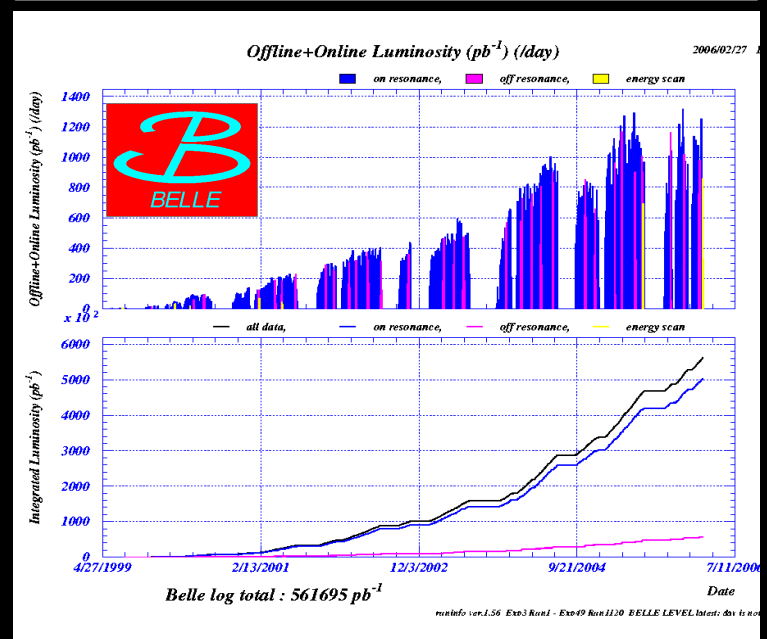
- reconstruction of final (CP eigen)state
- determination of B^0 flavour at decay time ('tagging')
- measurement of decay vertices $\rightarrow \Delta t \sim \Delta z / (c \beta \gamma)$

The asymmetric B factories

Peak luminosity $1.00 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
 > 3 times higher than design
 Integrated luminosity 320 fb^{-1}
 Results in this talk based on 232M BB
 C.M. boost $\beta\gamma \sim 0.55$



Peak luminosity $1.63 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
 ~1.5 times higher than design
 Integrated luminosity 500 fb^{-1}
 Results in this talk based on 386M BB
 C.M. boost $\beta\gamma \sim 0.42$



Memento: at the $Y(4S)$, $1 \text{ fb}^{-1} \sim 1.1 \text{ M BB events}$

Basic (experimental) techniques

- Signal identified through (almost) uncorrelated kinematic variables:

$$m_{ES} \equiv \sqrt{E_{beam}^{*2} - p_B^{*2}} \quad (\mathbf{s}_{m_{ES}} \approx \mathbf{s}_{beam} \approx 2.7 MeV)$$

$$\Delta E \equiv E_{beam}^* - E_B^* \quad (\mathbf{s}_{\Delta E} \approx \mathbf{s}_{E_B^*} \approx 10 \div 50 MeV)$$

- Tagging based on charge correlation of decay products with B^0 flavour → Different algorithms, similar effective efficiency

$$Q = \sum e_i (1 - 2w_i)^2 \sim 30\% \quad [s(\sin 2b) \sim 1/\sqrt{Q}, \text{ cf. w/ } Q \sim 3\% \text{ at hadron machines}]$$

- Δz resolution $\sim 170 \mu m$, dominated by tagging vertex
- A_{CP} determined on unbinned maximum likelihood fits
 - ◆ after cuts on selection variables (Belle)
 - ◆ on more inclusive event samples, with multivariate analysis (BABAR)

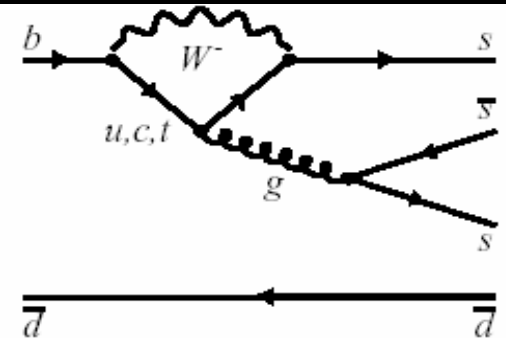
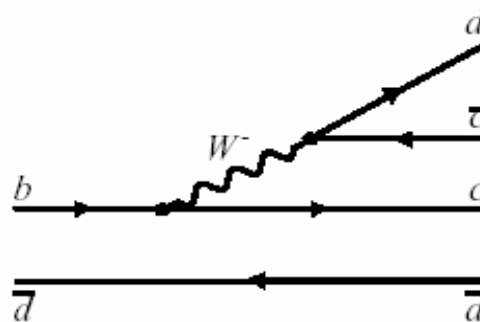
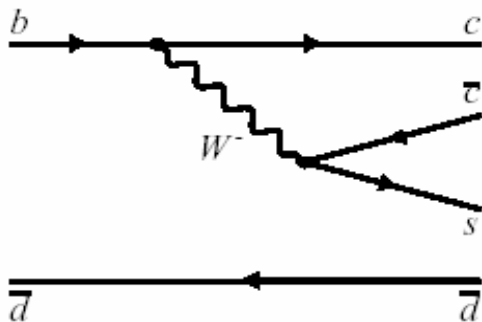
Several independent measurements of β

- Can independently measure β using three different categories of B^0 decays

a) $b \rightarrow c\bar{c}s$
(charmonium)

b) $b \rightarrow c\bar{c}d$ charm
(and charmonium)

c) Penguin - dominated
 $b \rightarrow d\bar{d}s, b \rightarrow s\bar{s}s$

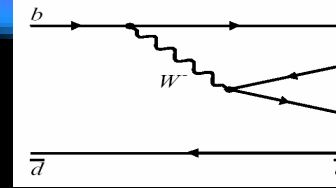


$J/\psi K_S^0, \psi(2S) K_S^0, \psi(3770) K_S^0,$
 $h_c K_S^0, J/\psi K_L^0,$
 $J/\psi K^{*0} (K^{*0} \rightarrow K_S^0 p^0)$

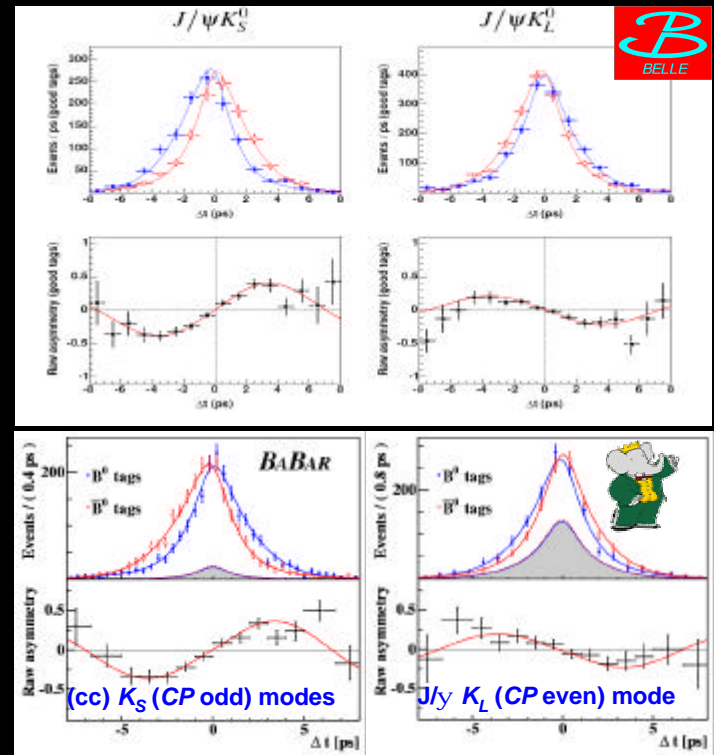
$D^{*+} D^-, D^+ D^-$
 $J/\psi p^0, D^{*+} D^{*-}$

$f K^0, K^+ K^- K_S^0,$
 $K_S^0 K_S^0 K_S^0, h' K^0, K_S^0 p^0,$
 $w K_S^0, f_0(980) K_S^0$

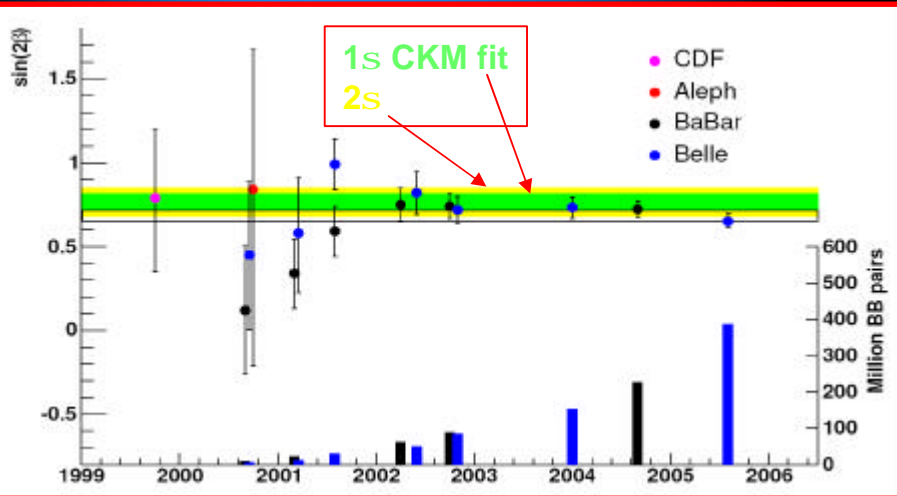
The precision frontier: $\sin 2\beta$ from $B^0 \rightarrow \text{charm} \text{onium } K^0$



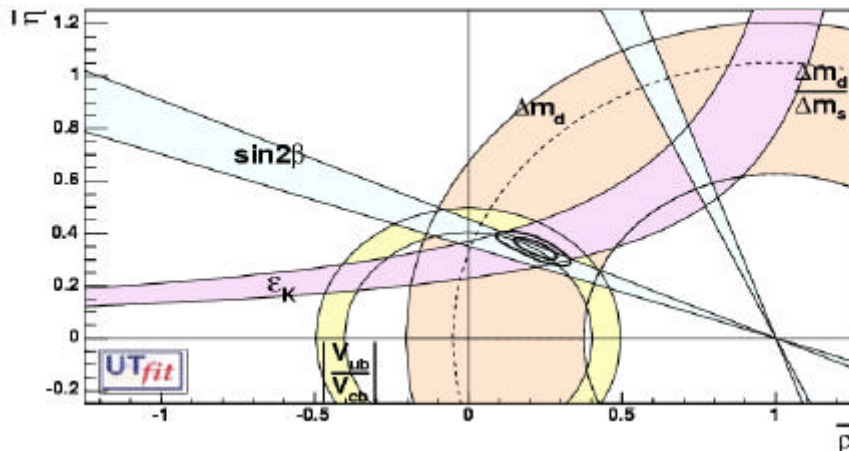
- Very clean theoretically
 - ◆ dominant penguin amplitude (suppressed by λ^2_{Cab}) has same phase as tree \rightarrow
 $C_F=0$, or $A_{CP}(\Delta t) = -\eta_f \sin 2\beta \sin(\Delta m \Delta t)$ in SM
 - ◆ confirmed by recent model-independent analyses [e.g. PRL 95 131802 (2005)]
 $\Delta S = 0.000 \pm 0.017$
- ... and experimentally
 - ◆ large BF
 - ◆ clean signature
- Stands as a 'platinum mode'
- Latest measurements:
 - ◆ Belle [hep-ex/0507037, 386M BB]:
 $\sin 2\beta = 0.652 \pm 0.039 \pm 0.020$
(was $0.728 \pm 0.056 \pm 0.023$)
 - ◆ BABAR [PRL94, 161803 (2005), 227M BB]:
 $\sin 2\beta = 0.722 \pm 0.040 \pm 0.023$



$\sin 2\beta$ from charmonium K^0 (II)



- ➔ Experimental measurement $\sin 2\beta_{[WA]} = 0.687 \pm 0.032$ now as precise as external constraints
- $\sin 2\beta_{[UTFit]} = 0.793 \pm 0.033$ (sides) $[0.734 \pm 0.024]$ (all)
- ➔ Improved experimental precision will directly impact UT fits

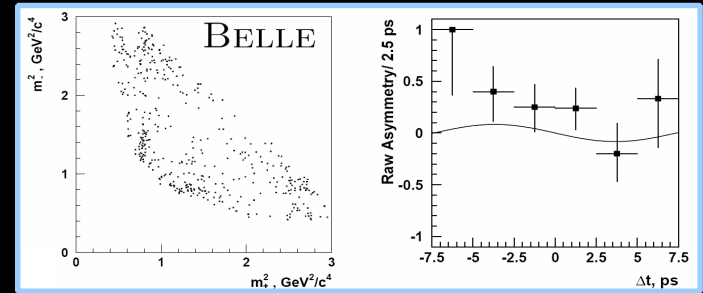
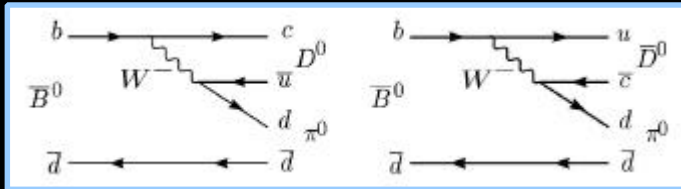


- ➔ Important reference point for constraining the UT
- in fact, a great success of the SM!

Interlude: breaking the $2\beta/\pi - 2\beta$ ambiguity

Use $b \rightarrow cu d [B^0 \rightarrow D_{CP}(K_S \pi^+ \pi^-) h^0]$ decays

[A. Bondar, T. Gershon, P. Krokovny, PL B624 1 (2005)]



- Theoretically clean (no penguins)
- Neglect DCS $B^0 \rightarrow D_{CP} h^0$ decay
- Interference of Dalitz amplitudes sensitive to $\cos 2\beta$

$$M_{B^0} = f_+ \cos(\Delta m \Delta t / 2) - i e^{+i2\phi_1} \eta_{h^0} (-1)^l f_- \sin(\Delta m \Delta t / 2)$$

$$M_{\bar{B}^0} = f_- \cos(\Delta m \Delta t / 2) - i e^{-i2\phi_1} \eta_{h^0} (-1)^l f_+ \sin(\Delta m \Delta t / 2)$$

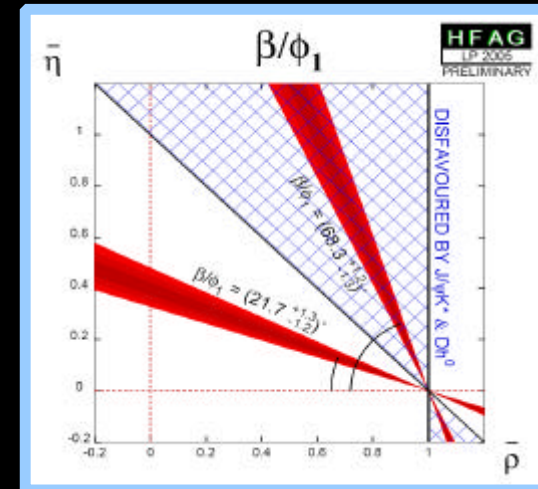
$$|f_{\pm}| \equiv |f(m_{K_S^0}^2, m_{K_S^0}^2)|^2$$

- Dalitz model fitted in D^* -tagged D^0 decays
- $\phi_1 = (16 \pm 21 \pm 12)^\circ$
 - rules out $\phi_1 = 68^\circ$ @ 97% CL [Belle. hep-ex/0507065]

$B^0 \rightarrow J/\psi K^{*0} (K^{*0} \rightarrow K_S \pi^0)$

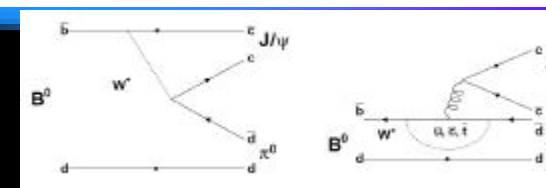
Extract $\cos 2\beta$ from interference of CP -even and CP -odd states ($L=0,1,2$) in time-dependent transversity analysis

- $\cos 2\beta < 0$ excluded at 86% C.L. [BABAR, PRD 71, 032005 (2005)]



$b \rightarrow c\bar{c}d$ decays :

$B^0 \rightarrow J/\psi\pi^0, D^{(*)+}D^{(*)-}$

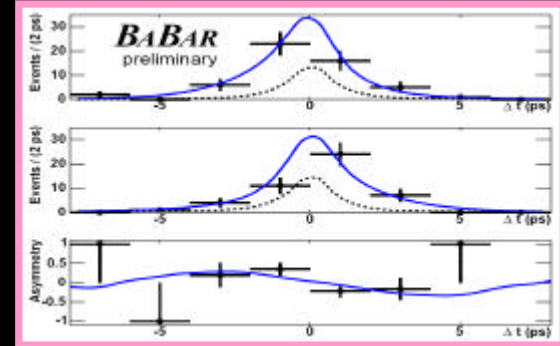


• Potentially penguin-polluted trees: $S \neq \sin 2b, C \neq 0$

• $J/\psi\pi^0$ [being submitted to PRD] updated meas.:

$$S_{J/\psi\pi^0} = -0.68 \pm 0.30 \pm 0.04$$

$$C_{J/\psi\pi^0} = -0.21 \pm 0.26 \pm 0.09$$



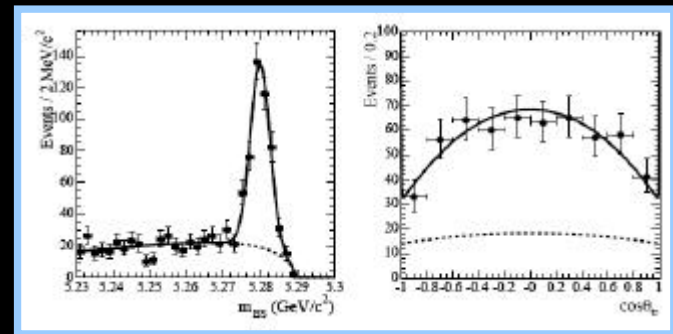
• $D^{*+}D^{*-}$: [PRL 95, 151804 (2005)] updated meas.:

$$f_{\text{odd}} = 0.125 \pm 0.044 \pm 0.070$$

[VV decay: both CP-odd and CP-even components.
CP-odd fraction extracted with transversity analysis]

$$S_+ = -0.75 \pm 0.25 \pm 0.03$$

$$C_+ = +0.06 \pm 0.17 \pm 0.03$$



• $D^{*+}D^{*-}$ [PRL 95, 131802 (2005)]:

$$S_{DD} = -0.29 \pm 0.63 \pm 0.06$$

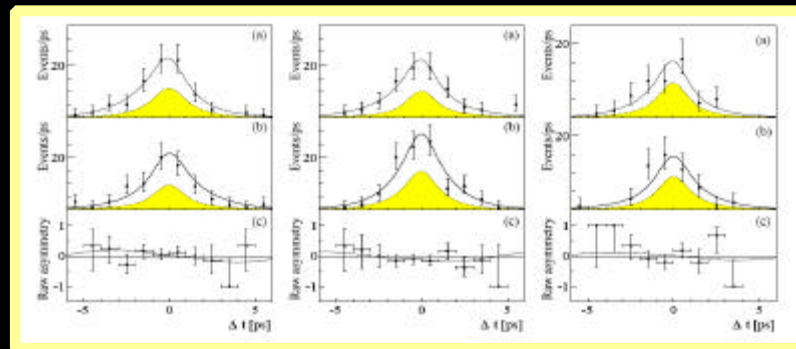
$$C_{DD} = +0.11 \pm 0.35 \pm 0.06$$

$$S_{D^*+D^-} = -0.54 \pm 0.35 \pm 0.07$$

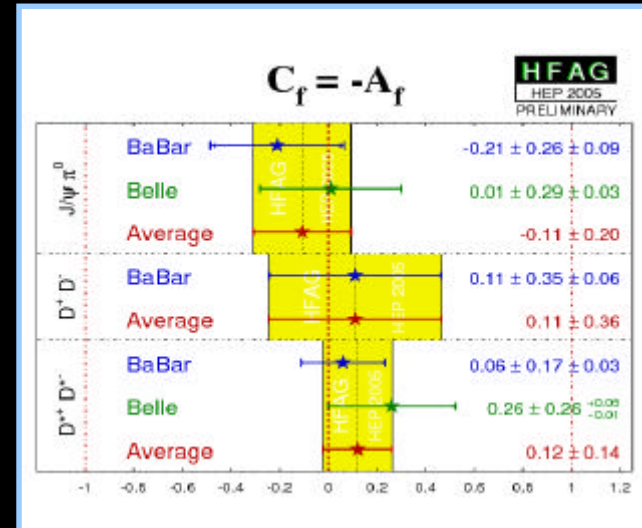
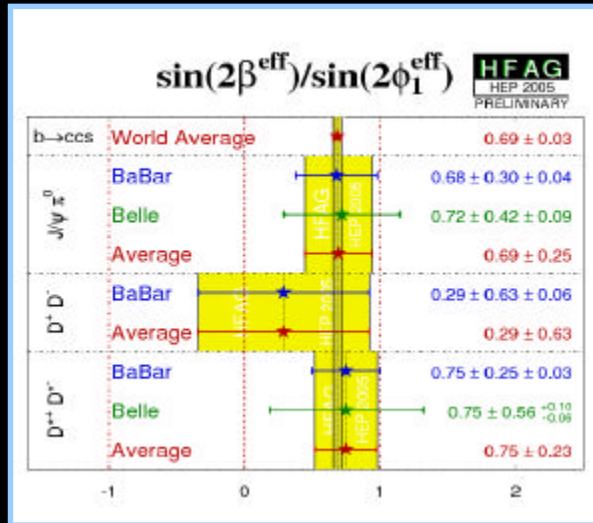
$$C_{D^*+D^-} = +0.09 \pm 0.25 \pm 0.06$$

$$S_{D^*-D^+} = -0.29 \pm 0.33 \pm 0.07$$

$$C_{D^*-D^+} = +0.17 \pm 0.24 \pm 0.04$$



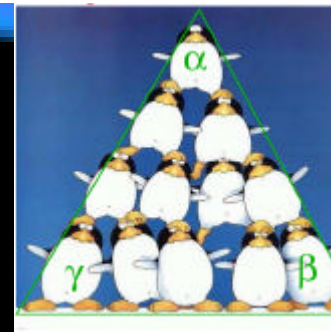
$b \rightarrow c\bar{c}d$ decays : summary



All results consistent with SM expectation of tree dominance

- $\Delta S_{DD} = S_{DD} - \sin 2\beta \sim 0.02 - 0.05$ [Z-Z. Xing, PR D61 014010 (2000)]
- Still below current experimental sensitivity

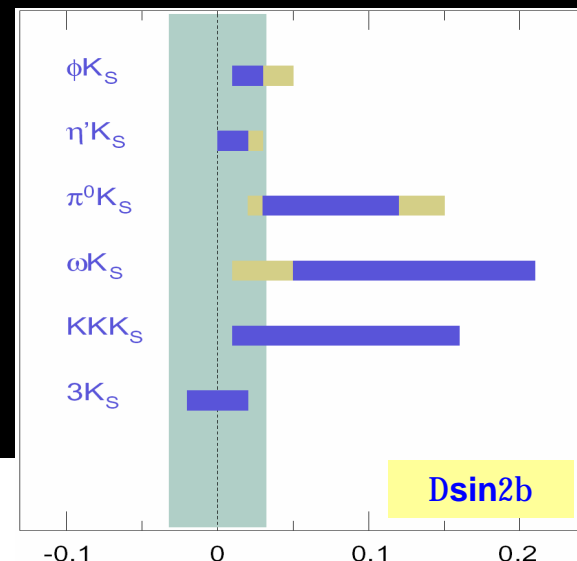
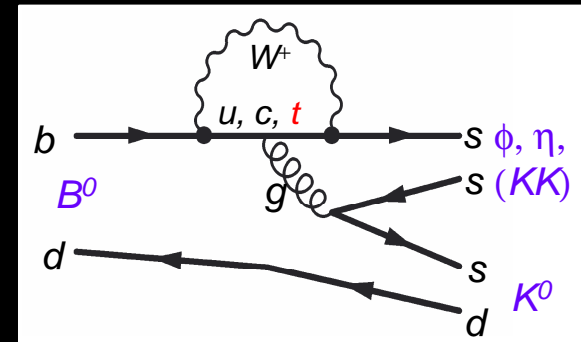
A path to New Physics: $b \rightarrow s$ penguins



- Small effects (e.g. from propagators of heavy particles circulating in the loop) more easily detectable since Tree is missing
- CKM factors same as $J/\psi K_s$. If single phase, SM predicts:

$$\begin{aligned} S_{\text{peng}} &= S_{\text{charmonium}} = \sin 2\beta \\ C_{\text{peng}} &= C_{\text{charmonium}} = 0 \end{aligned}$$

- Deviations from this pattern could be sign of NP
- Theory issue:
 - ❖ more than 1 amplitude/phase are (usually) involved
 - ❖ e.g., $b \rightarrow u\bar{u}s$ CS tree (g) in channels involving non-strange neutral mesons
 - ❖ Intense theoretical work lately to calculate SM corrections to the naïve picture
 - ✓ SU(3)-based model-independent bounds
 - ✓ QCD Factorization
 - ✓ theory parameters constrained to measured BFs (expected to improve in the future)



Example from recent calculations
(QCD factorization)
2-body: [Beneke; PL B620, 143 (2005)]
3-body: [Cheng,Chua,Soni; PRD72, 094003 (2005)]

$b \rightarrow s$ penguin: experimental issues

Small branching fractions

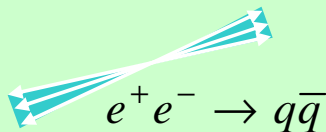
Large background from $e^+e^- \rightarrow q\bar{q}$

($q = u, d, s, c$)

- In addition to standard ΔE and m_{ES} , use event-shape discriminating variables in M.L. fit

B produced (almost) at rest in $\Upsilon(4S)$ frame

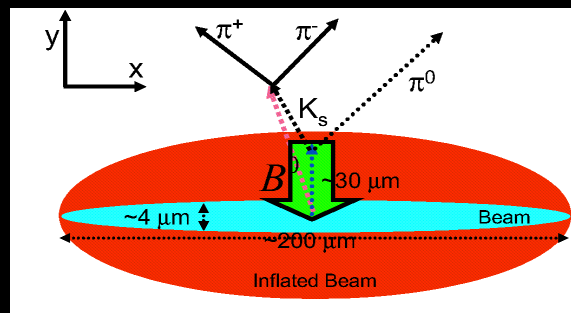
$B\bar{B}$



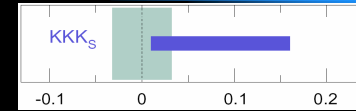
No charged tracks from decay vertex for some channels

- extrapolate back the K_s
 - require K_s to decay in the inner part of vtx detector
 - use constraint of the beam spot in the transverse plane
 - cross-check using $J/\psi K_s$

Decay mode	BF($B \rightarrow f$) $\times 10^6$	$\Pi_i \text{BF}_i$ $\times 10^6$
$B @ J/\psi K^0$	850.0	100.3
$B @ \eta' K^0$	63.2	16.6
$B @ K^+ K^- K^0$	20.6	17.4
$B @ \phi K^0$	8.3	3.4
$B @ \omega K_S$	2.4	2.1
$B @ f_0 K_S$	2.7	1.8
$B @ K_S K_S K_S$	3.1	1.4
$B @ \pi^0 K_S$	5.8	3.9
$B @ \pi^0 \pi^0 K_S$	11	7.5



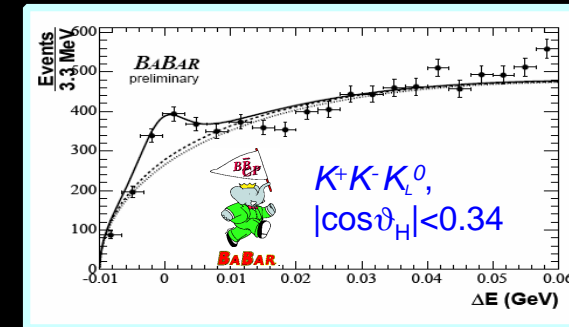
Exploring new submodes



$B^0 \rightarrow K^+K^-K_L^0$ (ϕK^0 excluded)

K_L^0 direction measured in EMC or IFR, energy from B -mass constraint

- 777 \pm 80 events in sample (452 \pm 28 in $K^+K^-K_S^0$)
- $S_{K^+K^-K_L^0} = 0.07 \pm 0.28 \pm 0.12$, $C_{K^+K^-K_L^0} = 0.54 \pm 0.22 \pm 0.09$
- CP content** in $K^+K^-K^0$ sample
 - from angular momentum analysis of $K^+K^-K_S^0$: $f_{CP\text{-even}} = 0.89 \pm 0.08 \pm 0.06$
 - consistent w/ Belle's isospin analysis [PRD69 012001 (2004)]
- $\sin 2\beta_{K^+K^-K^0} = 0.41 \pm 0.18 \pm 0.07 \pm 0.11_{CP}$



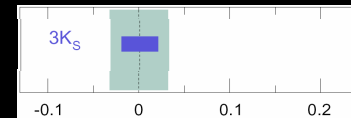
hep-ex/0507016

$B^0 \rightarrow K_S K_S K_S$

o CP eigenstate ($\eta_{3K_S} = +1$), $|\Delta\sin 2\beta| < 0.05$

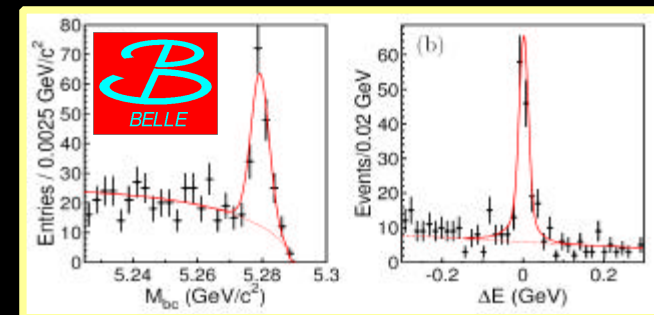
o small BF

- add more data (Belle)
- add $K_S K_S K_S (\pi^0 \pi^0)$ (BABAR)



$$S_{3K_S^0} = +0.63^{+0.28}_{-0.32} \pm 0.04 \quad \text{BABAR}$$

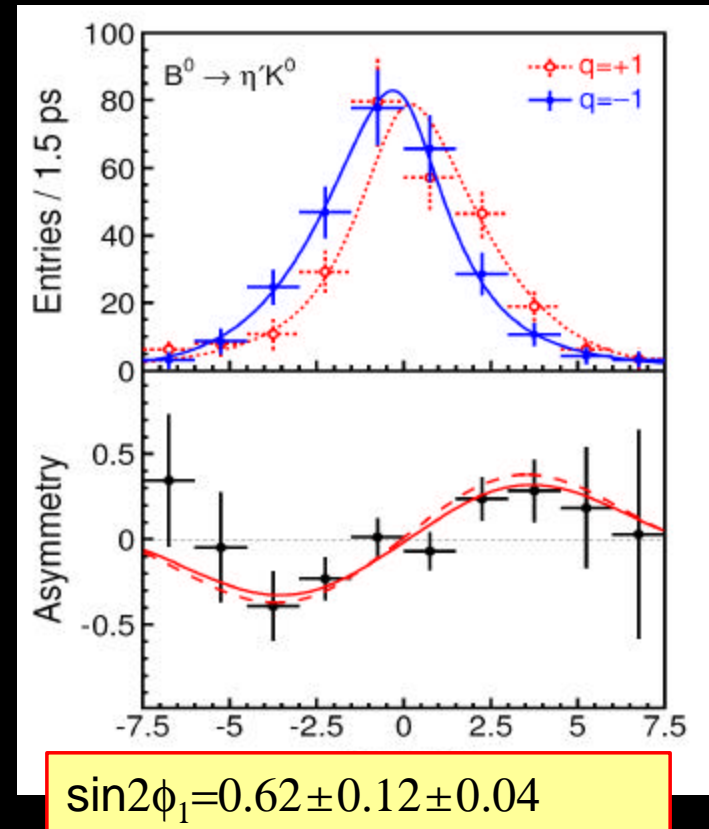
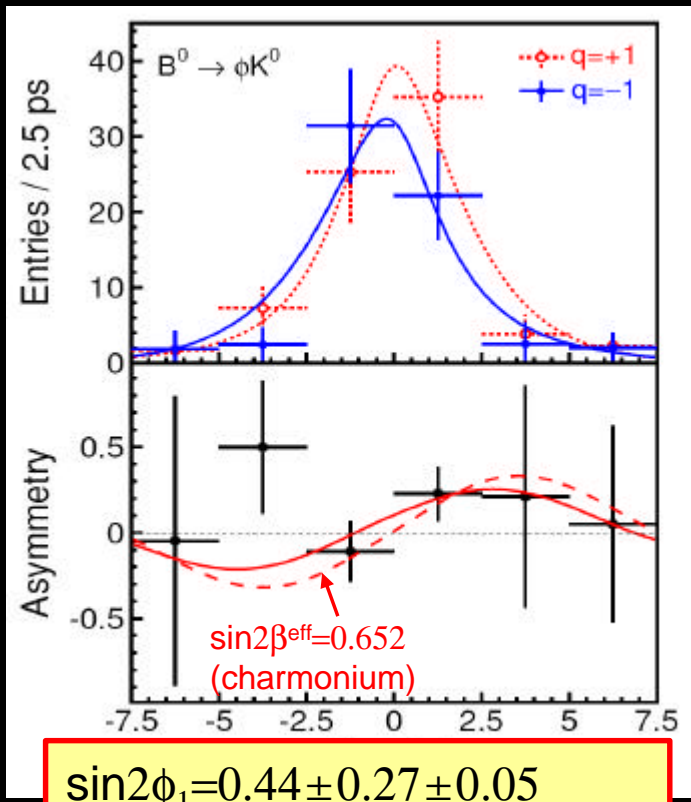
$$S_{3K_S^0} = +0.58 \pm 0.36 \pm 0.08 \quad \text{Belle}$$



Belle results on $b \rightarrow s\bar{s}s, b \rightarrow q\bar{q}s$



Updated results on $B^0 \rightarrow \phi K^0, \eta' K^0, f_0 K_S, \pi^0 K_S, \omega K_S, K^+ K^-$
 $K_S, K_S K_S K_S$ [hep-ex/0507037] “ K^0 ” includes both K_S and K_L

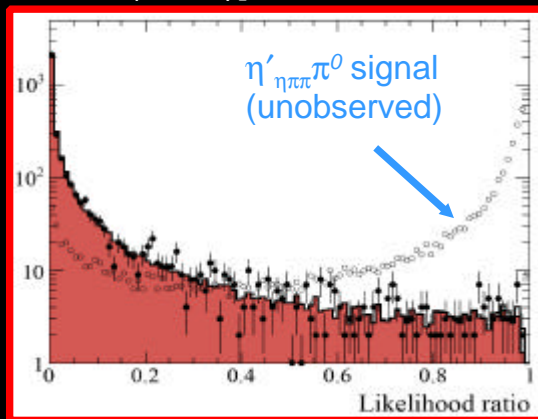
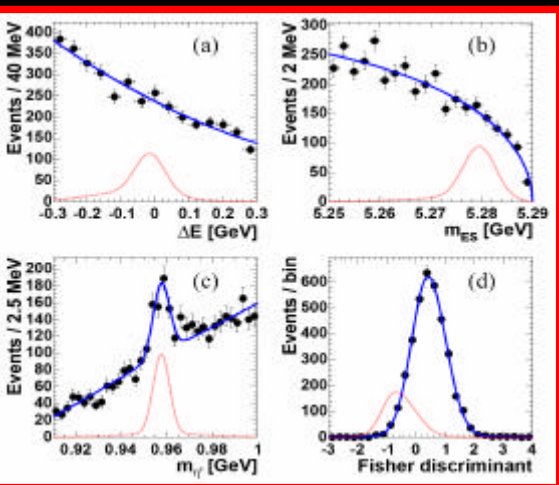


Searches for $\eta'\pi^0$, $\eta\pi^0$, $\eta'\eta$



- Expected BF $\sim 0.2 \div 2.0 \times 10^{-6}$
- Use $\eta_{\gamma\gamma}$, $\eta_{3\pi}$, $\eta'_{\eta\pi\pi}$, $\eta'_{\rho\gamma}$ modes

- Decays dominated by 'flavor-singlet' penguin and ($\eta\eta'$) color-suppressed tree.
- More precise measurements can reduce (by $\sim 20\%$) the theoretical uncertainty of CS tree amplitude for $\eta' K^0$ decays in SU(3)-based analysis [Gronau, Rosner, Zupan PL B596, 107 (2004)]



Likelihood ratio
 $\mathcal{L}_{sig}/[\mathcal{L}_{sig} + \sum \mathcal{L}_{bkg}]$
 from m_{ES} , ΔE , $m_{\eta'}$, Fisher

$$B(B^0 \rightarrow \eta'\eta) = (0.2_{-0.5}^{+0.7} \pm 0.4) \times 10^{-6} (< 1.7 \times 10^{-6})$$

$$B(B^0 \rightarrow \eta\pi^0) = (0.6_{-0.4}^{+0.5} \pm 0.1) \times 10^{-6} (< 1.3 \times 10^{-6})$$

$$B(B^0 \rightarrow \eta'\pi^0) = (0.8_{-0.6}^{+0.8} \pm 0.1) \times 10^{-6} (< 2.1 \times 10^{-6})$$

[BABAR, hep-ex/0603013, submitted to PRL]



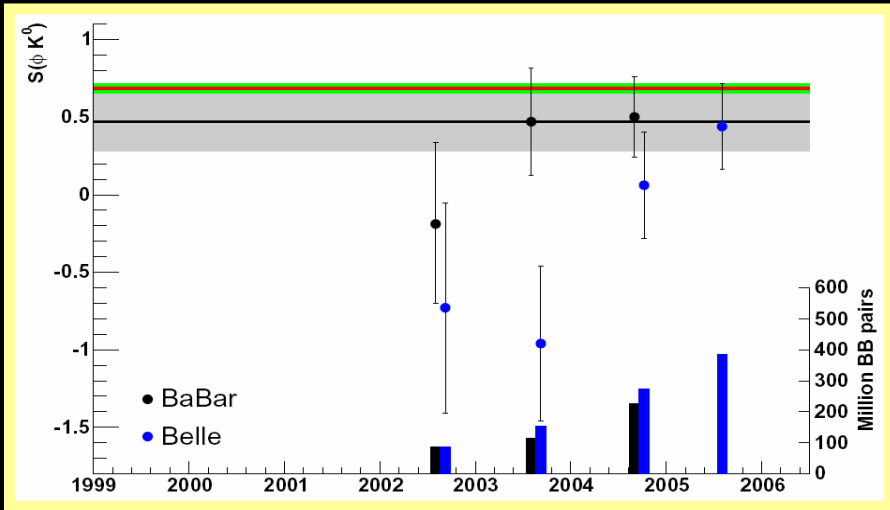
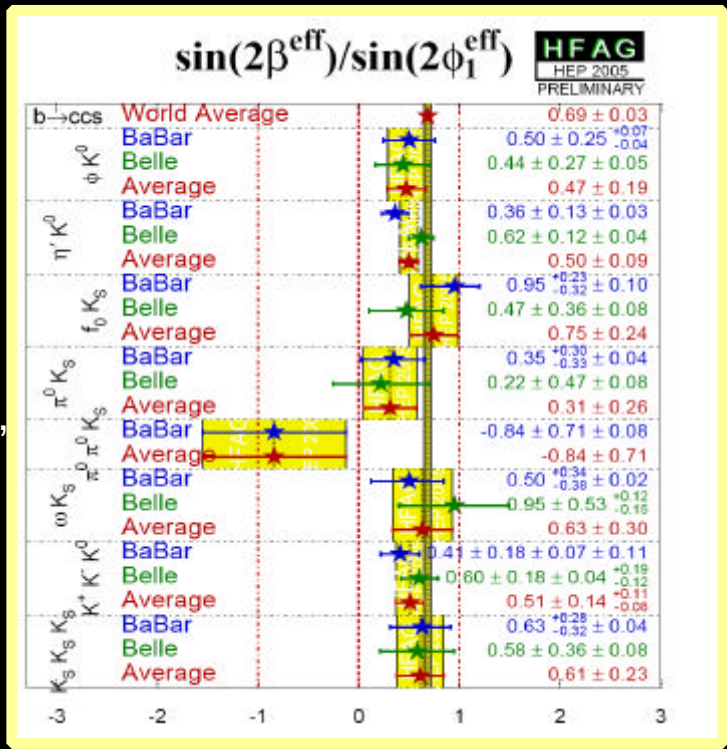
Belle [hep-ex/0603001, subm. to PRL] finds

$$BF(B^0 \rightarrow h'p^0) = [2.79_{-0.96}^{+1.02} (stat)_{-0.34}^{+0.35} (syst)] \times 10^{-6}$$



$b \rightarrow s$ penguins: current experimental status

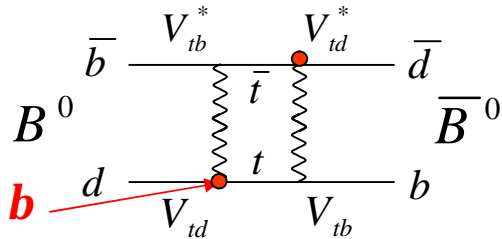
- ➔ Good agreement between *BABAR* and Belle
 - similar errors!
- ➔ Consistency among different channels
- ➔ Almost all modes within ~ 1 sigma from charmonium (but sign opposite to prediction)
 - deviations further reduced by shift of charmonium average
- ➔ Remember: due to different SM and NP corrections, **AVERAGING NOT ALLOWED**
- ➔ Need more statistics



Measuring α at the B factories

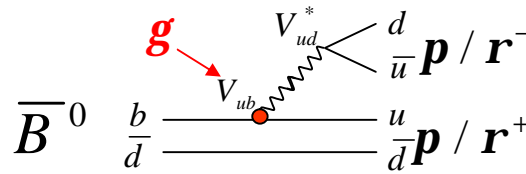
$$\alpha = \pi - (\beta + \gamma)$$

$B^0 \bar{B}^0$ mixing



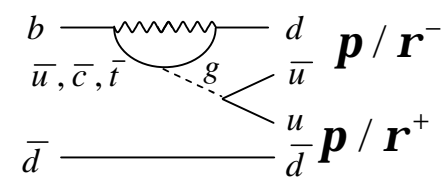
$$q/p \propto V_{tb}^* V_{td} / V_{tb} V_{td}^*$$

Tree decay



$$A \propto V_{ud}^* V_{ub}$$

Penguin decay



$$A \approx V_{td}^* V_{tb}$$

- Difficult to reliably estimate how much penguins contribute
 - BF($B^0 \rightarrow K^+ \pi^-$) (\sim pure penguin) indicates they cannot be neglected
 - In general $C_{hh} \neq 0$, and we measure $S_{hh} = \sqrt{1 - C_{hh}} \sin(2\alpha_{\text{eff}})$

$$I_{hh} \equiv \frac{q}{p} \frac{\bar{A}}{A} = -e^{2i\alpha} \frac{1 - P/T e^{-i\alpha}}{1 - P/T e^{i\alpha}} \equiv |I| e^{-2i\alpha_{\text{eff}}}$$

a: coping with penguins

Gronau/London analysis

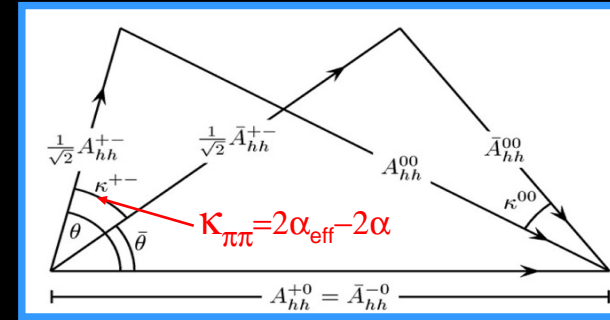
- Using isospin symmetry, $B \rightarrow hh$ amplitudes related by:

$$A(B^+ \rightarrow h^+h^0) = 1/\sqrt{2} \cdot A(B^0 \rightarrow h^-h^+) + A(B^0 \rightarrow h^0h^0)$$

- Neglecting EW penguins, $B^+ \rightarrow h^+h^0$ ($\Delta I = 2$) pure tree

$$\rightarrow A(B^+ \rightarrow h^+h^0) = \bar{A}(B^- \rightarrow h^-h^0)$$

- B and \bar{B} triangles do not match, and $\alpha = \alpha_{\text{eff}} - \kappa/2$
- Need to measure 6 BFs, including $A(B^0 \rightarrow h^0h^0)$ from *tagged* samples
- still a 8-fold ambiguity



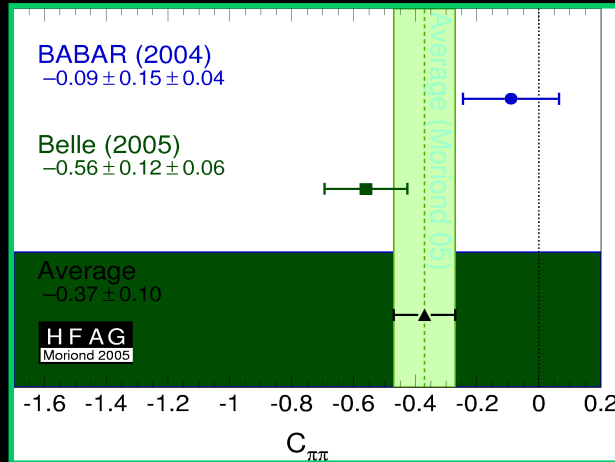
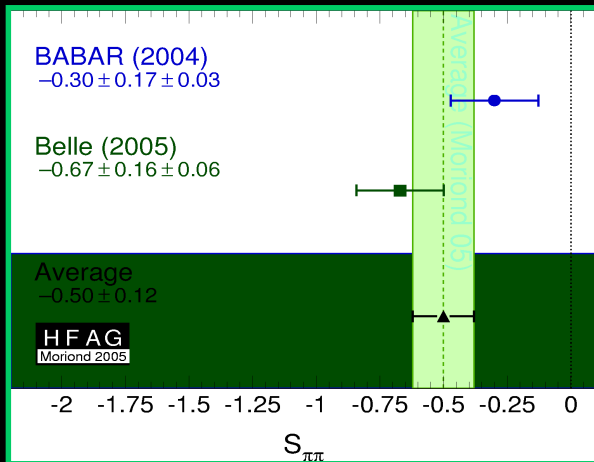
Grossman/Quinn bound:

$$\sin^2(\alpha_{\text{eff}} - \alpha) \leq \frac{BF(B \rightarrow h^0h^0)}{BF(B^\pm \rightarrow h^\pm h^0)}$$

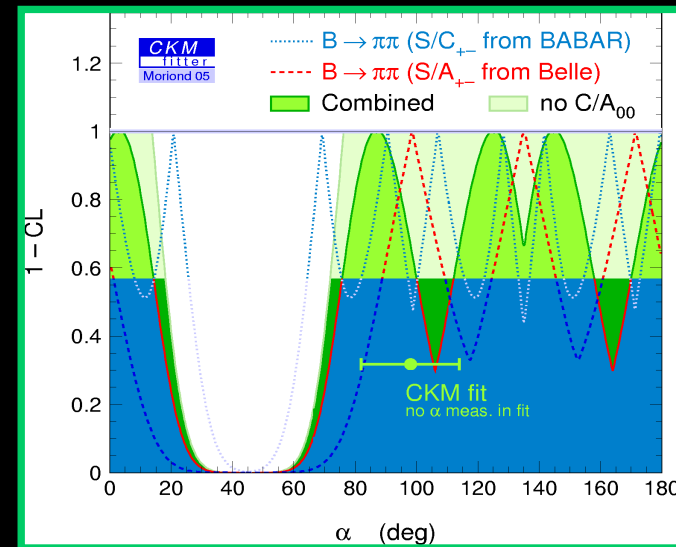
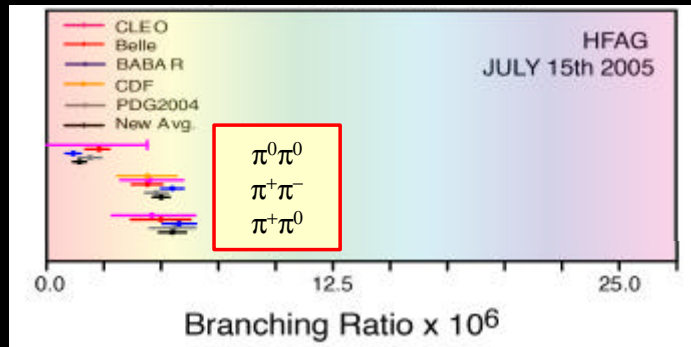
Don't need to tag B flavour

Useful if $BF(B \rightarrow h^0h^0)$ is small

The classic mode: $\pi\pi$



Fat $\pi\pi$ triangles \rightarrow weak SU(2) bound



$$\sin^2(a_{\text{eff}} - a) \leq \frac{BF(B \rightarrow p^0 p^0)}{BF(B^\pm \rightarrow p^\pm p^0)}$$

$$|\alpha - \alpha_{\text{eff}}| < 35^\circ$$

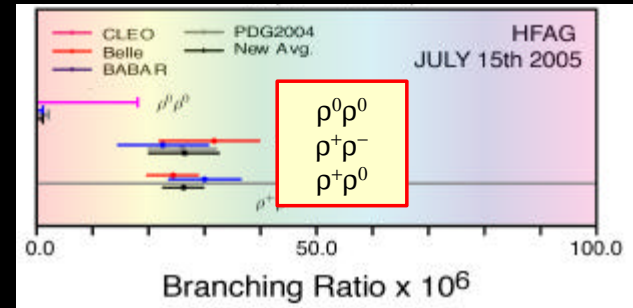
SU(2) bound works for $\rho\rho$!

- Experimentally challenging ($2 \pi^0$ s, wide ρ s, VV final state)
- However:

- ✓ $\text{BF}(\rho^+\rho^-) \sim 6$ times larger than $\pi^+\pi^-$
- ✓ almost purely CP -even:

$$f_L = 0.978 \pm 0.014^{+0.021}_{-0.029} \quad (\text{BABAR})$$

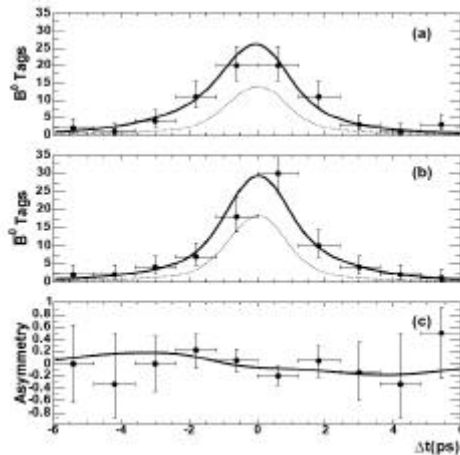
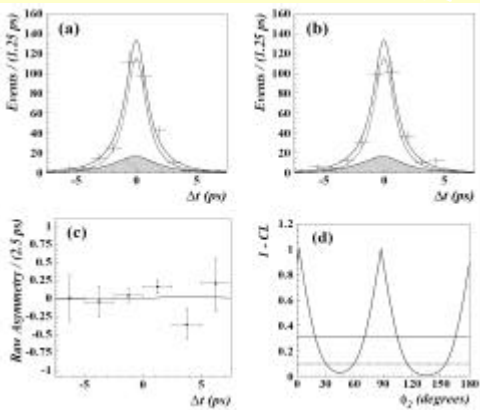
$$f_L = 0.941^{+0.034}_{-0.040} \pm 0.030 \quad (\text{Belle})$$



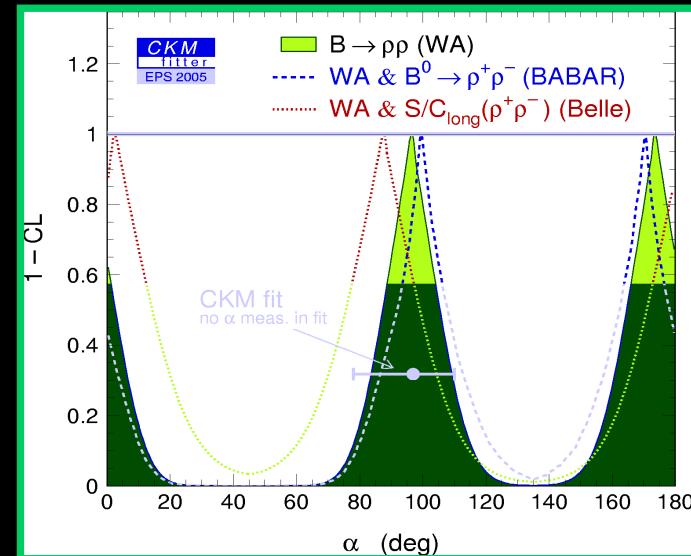
$$|\alpha - \alpha_{\text{eff}}| < 11^\circ \text{ @ } 68\% \text{ C.L.}$$



hep-ex/0601024 275 M BB
subm. to PRL **NEW!**



PRL 95 041805 (2005)



The 3rd way to α : TD Dalitz analysis of

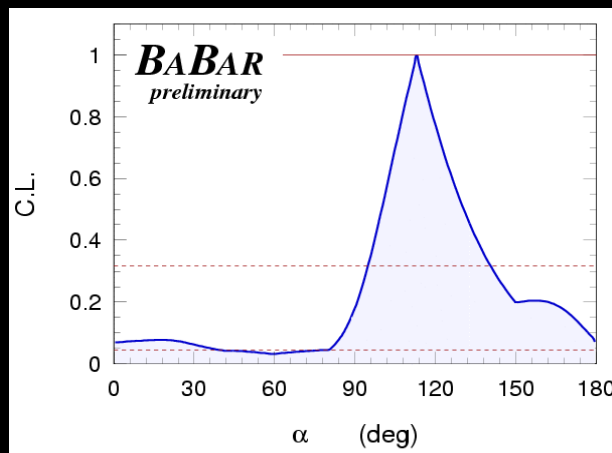
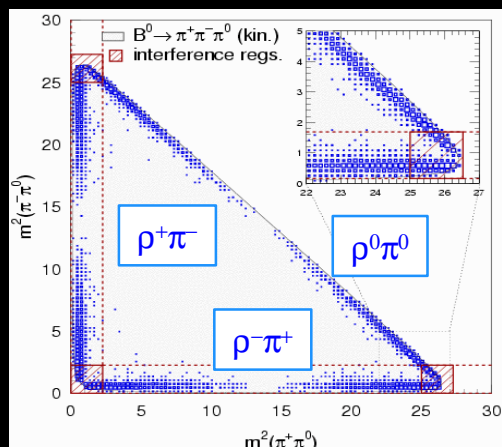


- Assume ρ dominance and use phase information across Dalitz plane to extract α

*A. Snyder and H. Quinn,
Phys. Rev. D, 48, 2139 (1993)*

$$A(B^0 \rightarrow p^+ p^- p^0) = f_+ A(r^+ p^-) + f_- A(r^- p^+) + f_0 A(r^0 p^0)$$

$$\bar{A}(B^0 \rightarrow p^+ p^- p^0) = f_+ \bar{A}(r^+ p^-) + f_- \bar{A}(r^- p^+) + f_0 \bar{A}(r^0 p^0)$$

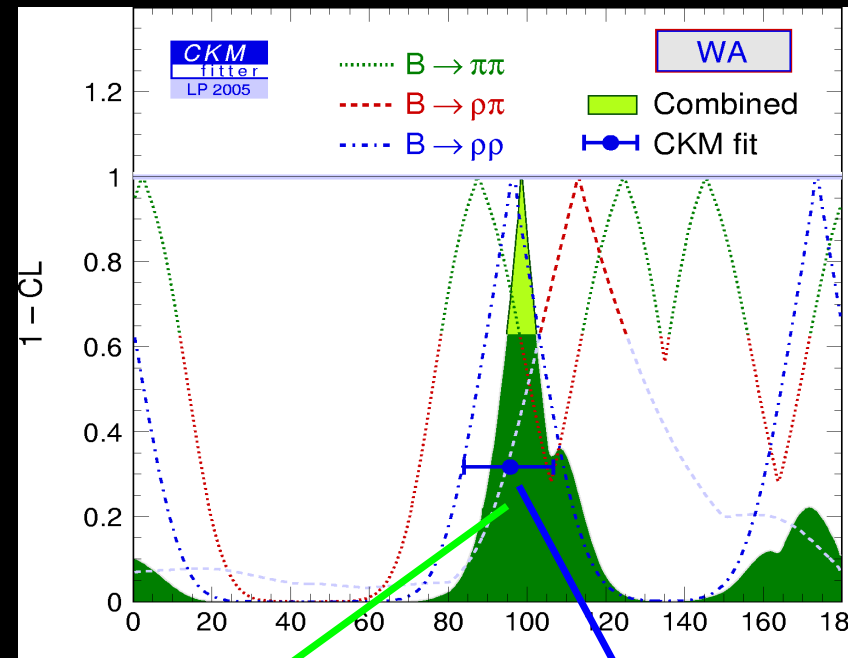


No ambiguity : only one solution:

$$a = (113_{-17}^{+27} \pm 6)^\circ$$

Putting all together:

- All three modes give consistent and complementary measurements of α
- $\pi\pi$ constraint weak
- $\rho\rho$ most precise
- TD analysis of 3π Dalitz plot in $\rho\pi$. Weak constraint at 90% CL, but disfavors $\rho\rho$ mirror solution near 170°



$$a[hh] = (99^{+12}_{-9})^\circ$$

$$a_{CKM} = (95^{+10}_{-13})^\circ$$

Summary and outlook

- BABAR and Belle measure $\sin 2\beta$ in $(c\bar{c})K^0$ modes to 5% precision

$$\sin 2\beta_{\text{charmonium}} = 0.687 \pm 0.032$$

- Comparison with $\sin 2\beta^{\text{eff}}$ in $b \rightarrow s$ penguin modes could reveal New Physics effects
 - ◆ need to carefully evaluate SM contributions
- $\sin 2\beta^{\text{eff}}$ measurements are statistically limited
 - ◆ uncertainties scaled faster than $1/\sqrt{L}$ so far (adding new channels)
- Extraction of α depends crucially on penguin bounds ($\rho^0\rho^0/\rho^+\rho^0$)
- Theory often fed by experimental measurements
 - ◆ also improves with more data
- Expected precision vs. time:

