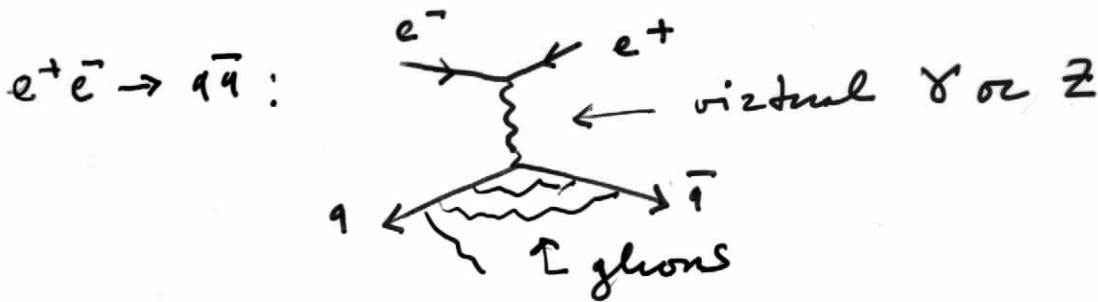


Forward-Backward Asymmetry for e^+e^- -annihilation into hadrons

Ermolaev -
Greco -
Trojan,
2002

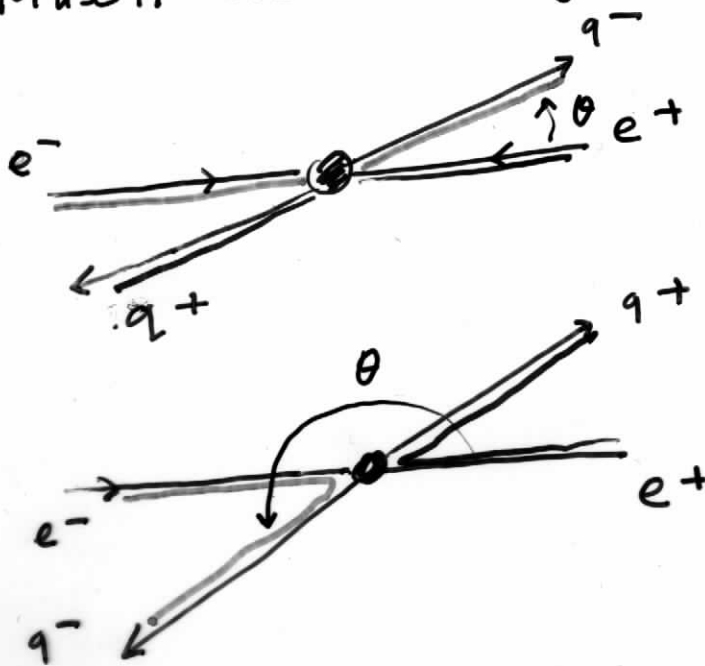
$$e^+e^- \rightarrow \text{hadrons} = (e^+e^- \rightarrow q\bar{q}) \times (q\bar{q} \rightarrow \text{hadrons})$$



When $s \equiv (P_{e^-} + P_{e^+})^2 \gg (100 \text{ GeV})^2$, electroweak radiative corrections can yield double-logarithmic contributions:



Multi-boson exchange \Rightarrow FBA.



$\theta \ll 1$ - Forward kinem.

$\theta \sim \pi$ - Backward kinem

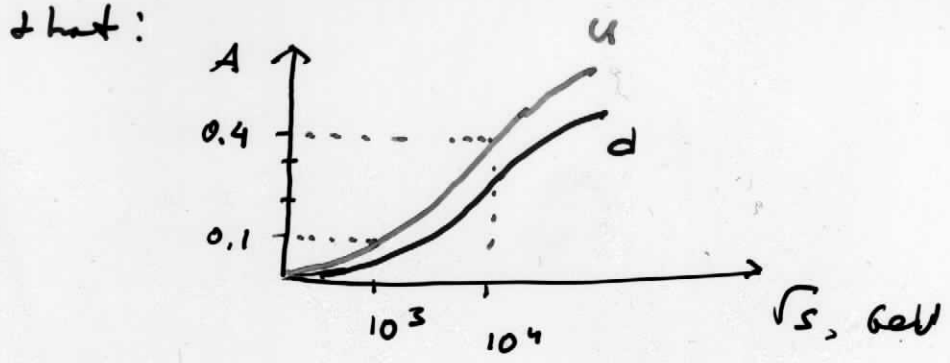
— way of (-) charge
— way of (+) charge

$$q^+ = u, \bar{d}, c, \bar{s}$$

$$q^- = d, \bar{u}, s, \bar{c}$$

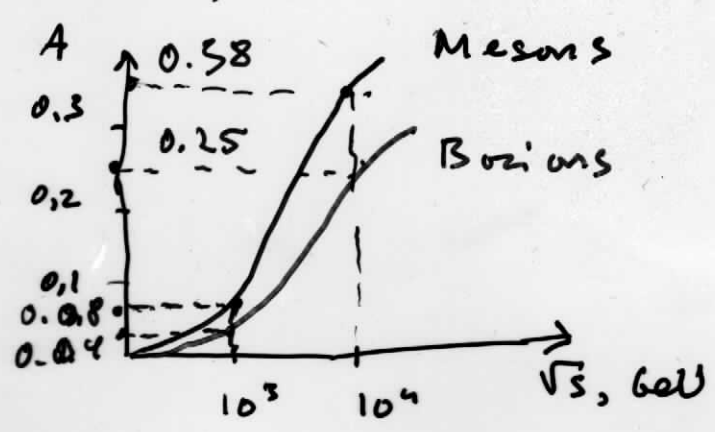
\swarrow Forward scattering amplitude
 $M_F \neq M_B$
 Effect of Multi-EW-top exchanges
 \nwarrow Backward scattering amplitude
 $\Rightarrow A = \frac{d\sigma_F - d\sigma_B}{d\sigma_F + d\sigma_B} \neq 0$
 \uparrow FB asymmetry
 Forward cross section
 Backward cross section

Had quarks been experimentally detected, A would have depended on the total energy like that:



Hadronization effects change A. They are different for baryons and mesons (all are charged).

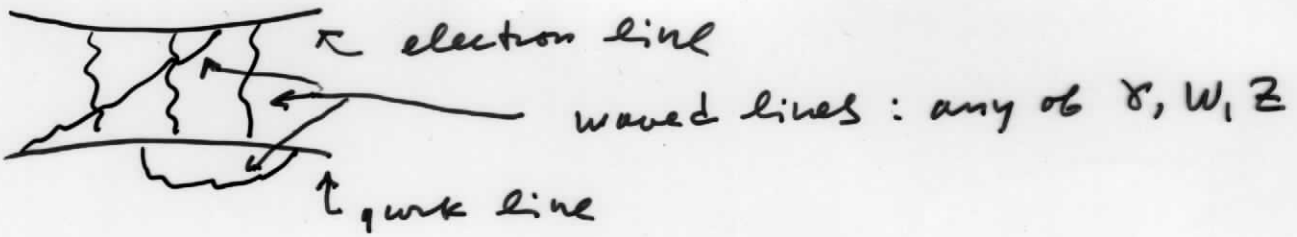
As a result,



Hadronization of quarks - numerically (JETSET)

Sub-process $e^+e^- \rightarrow q\bar{q}$ - analytically:

Infra-Red Evolution Equations



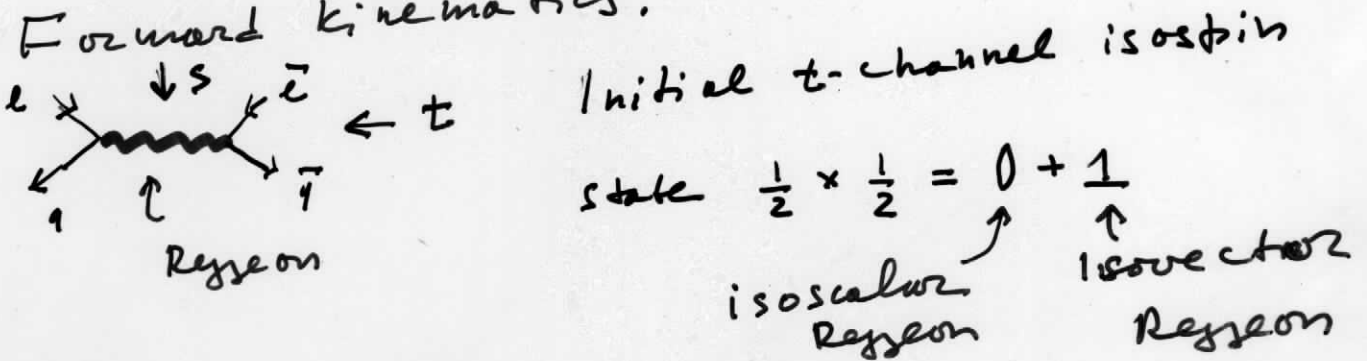
Convenient: $e_i, \bar{e}^k \rightarrow q_i, \bar{q}^k$

Most difficult case: $e_i, q_{i'}$ from left doublets
 $\bar{e}^k, \bar{q}^{k'}$ from right doublets

Scattering amplitude is a matrix $M_{i'k}^{ik'}$

Both the Forward and the Backward kinematics are of the Regge type and are considered with the same technique

Forward kinematics:



$$M_{i'k}^{ik'} = (P_0)_{i'k}^{ik'} \cdot M_0 + (P_1)_{i'k}^{ik'} \cdot M_1$$

↑ invariant amplitudes

$$(P_0)_{i'k}^{ik'} = \frac{1}{2} \delta_{i'}^i \delta_k^{k'}, \quad (P_1)_{i'k}^{ik'} = 2 (t_A)_{i'}^i (t_A)^k_{k'}$$

↑ $SU(2)$ -generators

$$P_A P_B = \delta_{AB} P_B$$

In order to get rid of Infra-Red singularities (from virtual photons) we have to introduce an IR cut-off μ .

We assume $\mu \sim M_W, Z$

Therefore, $M_{0,1} = M_{0,1}(s, \mu^2)$. Now we can drop all masses and evaluate $M_{0,1}$ with respect to μ .

It is convenient to use the Sommerfeld-Watson (Mellin) transform:

$$M_i^{(\pm)} = \int_{-i\infty}^{i\infty} \frac{d\omega}{2\pi i} \left(\frac{s}{\mu^2}\right)^\omega \zeta^{(\pm)}(\omega) F_i^{(\pm)}(\omega), \quad i=0,1$$

$$\zeta^{(\pm)} = (e^{\pm i\pi\omega} \pm 1) / 2 = \text{signature factors}$$

Born approximation:

$$F_i^{(+)} = \frac{a_i}{\omega}, \quad a_0 = \frac{3g^2 + g'^2 \gamma_1 \gamma_2}{4}$$

$$a_1 = -\frac{g^2 + g'^2 \gamma_1 \gamma_2}{4}$$

$$g' = g \tan \theta_W, \quad \gamma_{1,2} - \text{hypercharges}$$

Beyond Born:

numerical factors

$$\omega F_i^{(+)} = a_i + \frac{b_i}{8\pi^2} \frac{d}{d\omega} F_i^{(+)} + \frac{1}{8\pi^2} (F_i^{(+)})^2$$

$$b_0 = \frac{g'^2 (\gamma_1 - \gamma_2)^2}{4}, \quad b_1 = \frac{2g^2 + g'^2 (\gamma_1 - \gamma_2)^2}{4}$$

Solution:
$$F_i^{(+)} = a_i \frac{D_{p_i-1}(w/\lambda_i)}{D_{p_i}(w/\lambda_i)},$$

with $\lambda_i = \sqrt{t_i/8\pi^2}$, D_p - Parabolic cylinder function

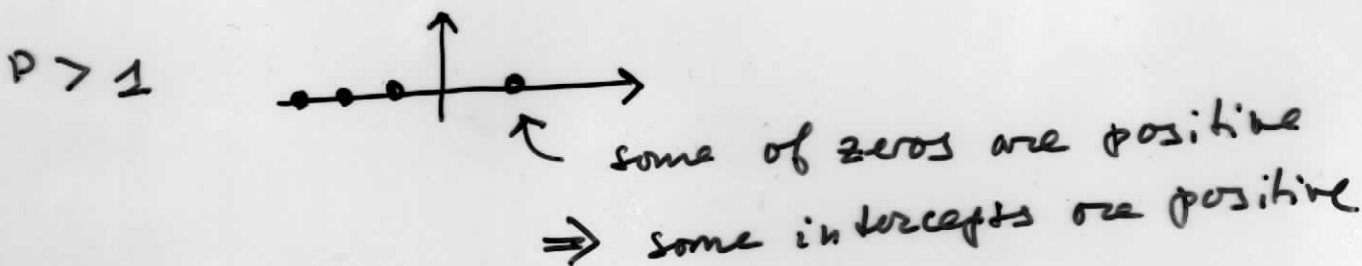
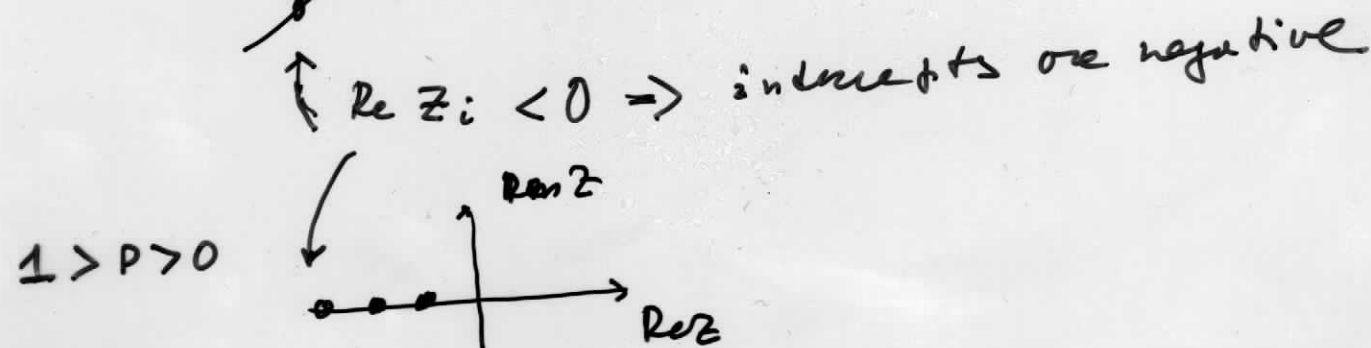
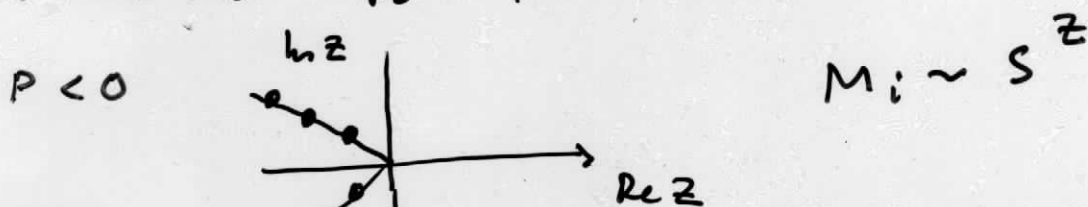
$$p_i = a_i/b_i.$$

$$-t \lesssim M_{w,z}^2: M_i^{(+)} = a_i \int_{-i\infty}^{i\infty} \frac{dw}{2\pi i} \left(\frac{s}{\mu^2}\right)^w \frac{D_{p_i-1}(w/\lambda_i)}{D_{p_i}(w/\lambda_i)}$$

$$s \gg -t \gg M_{w,z}^2: M_i^{(+)} = a_i \int_{-i\infty}^{i\infty} \frac{d\ell}{2\pi i} \left(\frac{s}{t}\right)^\ell \frac{D_{p_i-1}(\ell + \lambda_i \ln t/\mu^2)}{D_{p_i}(\ell + \lambda_i \ln t/\mu^2)}$$

Singularities of the integrands are

zeros of $D_{p_i}(z)$: If $D_p(z) = 0$,



Forward kinematics:
 iso scalar Reggeon

$$P_u = \frac{3g^2 + g'^2 \gamma_1 \gamma_2}{g'^2 (\gamma_1 + \gamma_2)^2} \approx 25$$

$$P_d = \frac{3g^2 - g'^2 \gamma_1 \gamma_2}{g'^2 (\gamma_1 - \gamma_2)^2} \approx 6$$

$$\Delta_u^F \approx 0.13, \Delta_d^F \approx 0.08$$

Backward kinematics:

$$P_u \approx P_d \approx -\frac{1}{4}$$

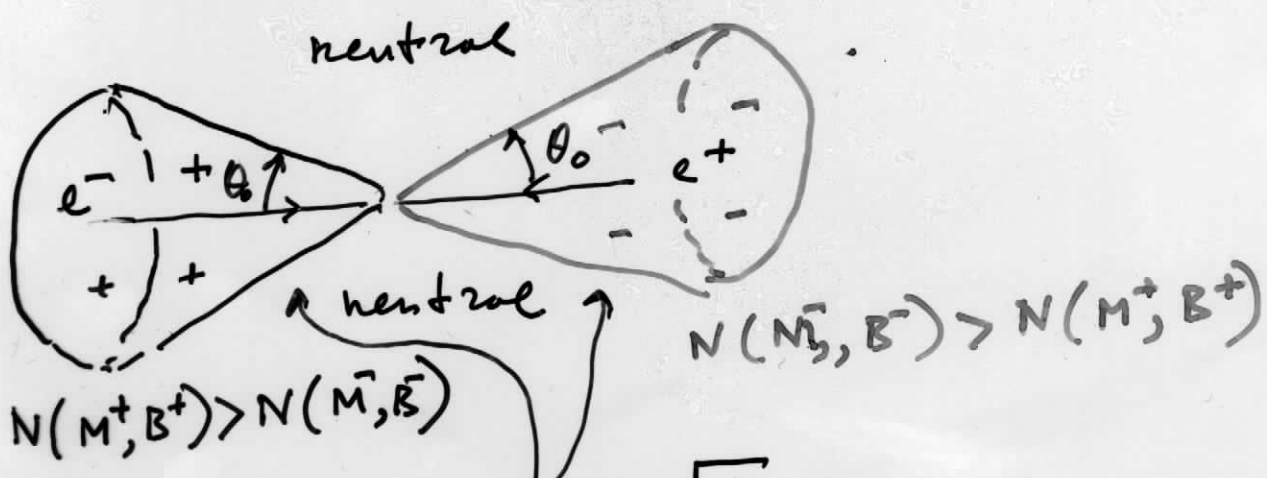
QED, $e^+e^- \rightarrow \mu^+\mu^-$: $P = -\frac{1}{4}$

Goodman-Gribov
 - Frolov-Lifshitz,
 1967

Universal behavior of the
 backward scattering.

$$\text{intercepts} \approx 0.27$$

The cases when the lepton and the quarks have
 other helicities are considered the same way.



$$\text{Opening angle} \sim 2\sqrt{\frac{t}{s}}$$

$$\text{When } \sqrt{t} = 100 \text{ GeV}, \sqrt{s} = 1 \text{ TeV},$$

$$\theta_0 \approx 10^\circ$$

Conclusion

1. Accounting for the electroweak DL contributions for e^+e^- -annihilation into hadrons leads to the Forward-Backward Asymmetry (FBA) for charged hadrons

2. Value of FBA is

When $\sqrt{s} = 1 \text{ TeV}$,

0.08	Mesons
0.05	Bosons

When $\sqrt{s} = 10 \text{ TeV}$,

0.37	Mesons
0.25	Bosons

and steeply rises with increase of the annihil. energy

3. FBA exists also for Proton-antiproton collisions at high energies:

$p\bar{p} \rightarrow$ charged mesons, bosons