



# B-meson rare decays and CKM matrix elements from Belle

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# Selected topics from many (>60) results:



## Rare and radiative decays:

Mode	Relevant for:	$\int Ldt$	Status
$\pi\pi, K\pi, KK$	$\varphi_3$ ( $\varphi_2$ ), DCPV	29.1 fb <sup>-1</sup>	Preliminary
$D_{CP}K^-$	$\varphi_3$	29.1 fb <sup>-1</sup>	Preliminary
$\phi K^{(*)}$	$\varphi_1$ , DCPV	21.6 fb <sup>-1</sup>	Preliminary
$\eta' K^{(*)}$	$\varphi_1$ , DCPV	10.4 fb <sup>-1</sup>	Published
$\eta K^{(*)}$	$\varphi_1$ , DCPV	21.3 fb <sup>-1</sup>	Preliminary
$K\pi\gamma, K\pi\pi\gamma, \rho\gamma$	$V_{td}/V_{ts}$ , DCPV	29.1 fb <sup>-1</sup>	Preliminary
$K^{(*)}l^+l^-, X_S l^+l^-$	$V_{td}/V_{ts}$ , DCPV	29.1 fb <sup>-1</sup>	Published

# Semileptonic (& exclusive) decays:



Mode	Relevant for:	$\int Ldt$	Status
$D^{-l^+ \nu}, D^{*-l^+ \nu}$	$V_{cb}$	10.2 fb <sup>-1</sup>	Published
$Xe^+ \nu$	$V_{cb}$	5.1 fb <sup>-1</sup>	Preliminary
$\pi^{-l^+ \nu}$	$V_{ub}$	29.1 fb <sup>-1</sup>	Preliminary
$D_s^+ \pi^-$	$V_{ub}$	21.3 fb <sup>-1</sup>	Preliminary

# B-decay dynamics:

$D^{(*)0} h^0 (\pi^0, \eta, \omega)$	Colour supp.	21.3 fb <sup>-1</sup>	Published
$KK\pi, K\pi\pi, KKK$	Factor., $\phi_3/\phi_1$	29.1 fb <sup>-1</sup>	Submitted
$\chi_{c0} K^+$	Factorization	29.1 fb <sup>-1</sup>	Published
$p\bar{p} K^+$	Dynam., DCPV	29.4 fb <sup>-1</sup>	Submitted
$p\bar{p}, \bar{\Lambda} p, \bar{\Lambda} \Lambda$	Dynam.	29.4 fb <sup>-1</sup>	Submitted

## Background suppression

Continuum  $e^+e^- \rightarrow qq$  (2jets)  
background dominant in most of  
rare decays :

$$\sigma_{BB} \cdot BF / \sigma_{qq} \sim O(10^{-5} - 10^{-6})$$

- Various event shape variables :  
Fox-Wolfram moments, thrust...  
( $\overline{BB}$  : spherical, continuum: jetty)
- Angle between B thrust axis and  
thrust of the remaining tracks  
(continuum: aligned)
- B angular distribution:  $\sin^2\theta$   
(continuum:  $1+\cos^2\theta$ )
- Fisher discriminant to maximize  
signal/background separation

## Identification of B

(momenta and energies in the  $Y(4S)$  rest  
frame)

$E_B = 5.28 \text{ GeV}$  and  $|\vec{p}_B| \approx 0.350 \text{ GeV}$  are  
known  $\Rightarrow$  use energy-momentum conservation:

$$\begin{aligned} \bullet \Delta E &= \sum E_i - E_{\text{beam}} \quad (\text{energy difference}) \\ \bullet M_{bc} &= \sqrt{E_{\text{beam}}^2 - \left(\sum \vec{p}_i\right)^2} \quad (\text{beam energy} \\ &\quad \text{constrained mass}) \end{aligned}$$

## K/ $\pi$ separation

likelihood ratio  $L_{K(\pi)}$  formed from the PID  
system info (  $dE/dx$ , aerogel Cherenkov,  
TOF)

$L_K / (L_\pi + L_K) \sim 1 \Rightarrow$  kaon,  $\sim 0 \Rightarrow$  pion  
( some K/ $\pi$  separation also in  $\Delta E$  )

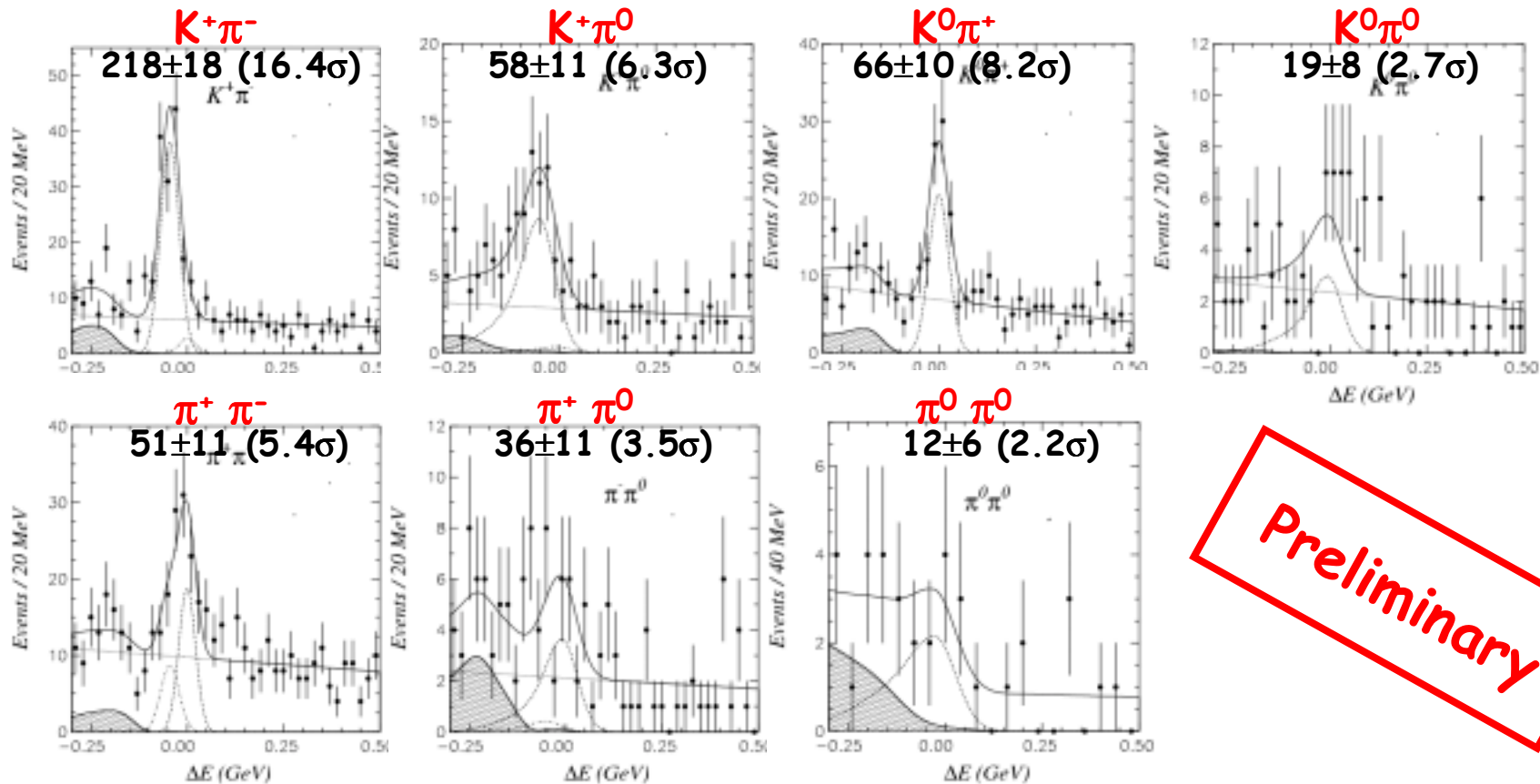
# $B \rightarrow \pi\pi/K\pi/KK$ (1)



Updated results (31.7M BB):

- Signal/background separation optimized for each decay mode
- Feed-across charmless decays background studied carefully  
 $\Rightarrow$  well controlled fit systematics

$\Delta E$  calculated with  $\pi^\pm$  mass



Preliminary

# B $\rightarrow$ $\pi\pi/K\pi/KK$ (2)



## DCPV via T- P interference

- measure BF's and their ratios  $\rightarrow \varphi_3$   
(theoretically challenging)

## Observations:

- Hierarchy:  $K^+ K^- < \pi^+ \pi^- < K^+ \pi^-$   
 $\rightarrow$   **$K^+ \pi^-$  mostly penguin?**
- Isospin invariance (penguin dominance sum rule):  

$$BF(K^+ \pi^-) + \tau_0 / \tau_+ \bullet BF(K^0 \pi^+) - 2 [ BF(K^0 \pi^0) + \tau_0 / \tau_+ \bullet BF(K^+ \pi^0) ] = (0.08 \pm 0.9) \times 10^{-5}$$

$$(\tau_0 / \tau_+ = 1.09 \pm 0.04 \text{ Belle})$$
 $\rightarrow$  **penguin dominance?**
- $\pi^0 \pi^0$  not observed yet

BF [ $10^{-5}$ ](UL@90% CL)

$K^+ \pi^-$	$2.18 \pm 0.18 \pm 0.15$
$K^+ \pi^0$	$1.25 \pm 0.24 \pm 0.12$
$K^0 \pi^+$	$1.88 \pm 0.30 \pm 0.15$
$K^0 \pi^0$	$0.77 \pm 0.32 \pm 0.16$
$\pi^+ \pi^-$	$0.51 \pm 0.11 \pm 0.04$
$\pi^+ \pi^0$	$0.70 \pm 0.22 \pm 0.08$
$\pi^0 \pi^0$	$< 0.56$
$K^+ K^-$	$< 0.05$
$K^0 K^+$	$< 0.38$
$K^0 K^0$	$< 1.3$

**Preliminary**

# B → ππ/Kπ/KK (3)



## Branching fractions ratios:

$$2\text{BF}(K^+\pi^0)/\text{BF}(K^0\pi^+) = 1.33 \pm 0.33 \pm 0.14 \quad (\text{A})$$

$$\text{BF}(K^+\pi^-)/2\text{BF}(K^0\pi^0) = 1.43 \pm 0.60 \pm 0.28 \quad (\text{B})$$

$$\begin{aligned} \tau_+/\tau_0 \text{BF}(K^+\pi^-)/2\text{BF}(K^0\pi^+) \\ = 1.27 \pm 0.23 \pm 0.09 \pm 0.04 \quad (\text{C}) \end{aligned}$$

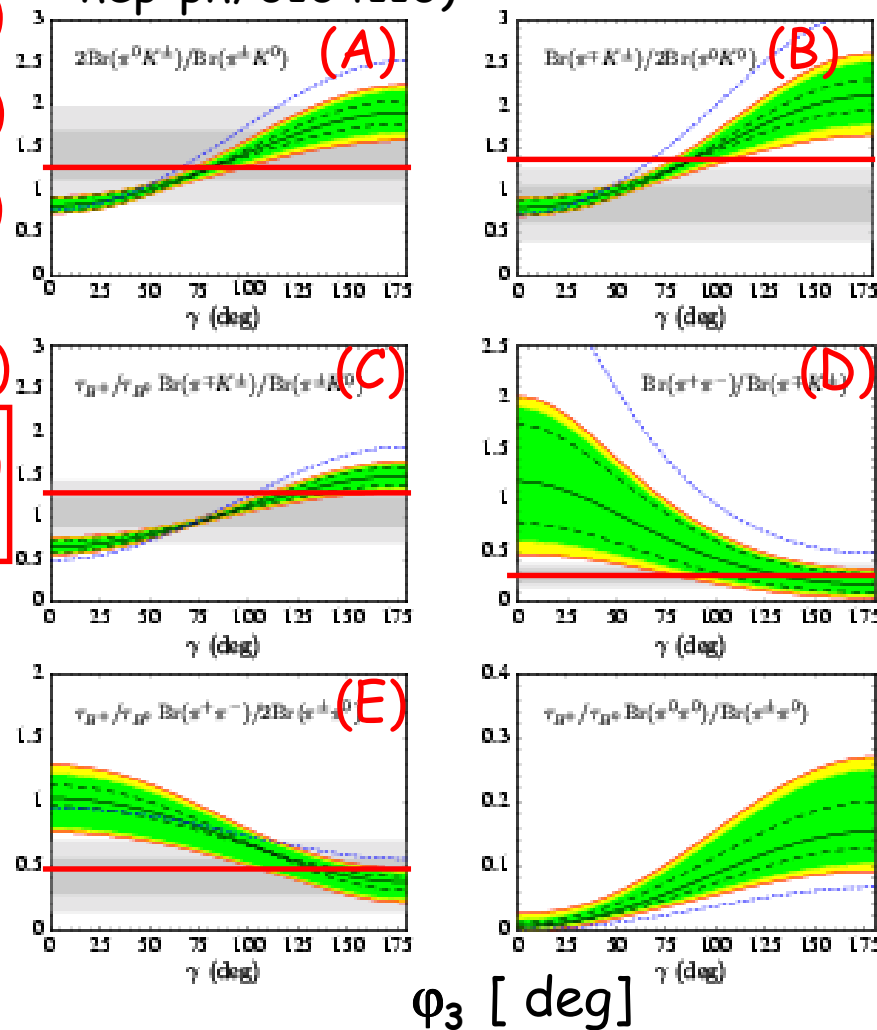
$$\text{BF}(\pi^+\pi^-)/\text{BF}(K^+\pi^-) = 0.24 \pm 0.06 \pm 0.02 \quad (\text{D})$$

$$\begin{aligned} \tau_+/\tau_0 \text{BF}(\pi^+\pi^-)/2\text{BF}(\pi^+\pi^0) \\ = 0.40 \pm 0.15 \pm 0.05 \pm 0.01 \quad (\text{E}) \\ \neq 1 \quad (\approx 4\sigma \text{ effect}) \end{aligned}$$

⇒ clear evidence for large interf. in ππ system (Δφ and/or Δδ ?)

All pointing to large φ<sub>3</sub>, but still consistent with indirect determinations

BF ratios vs φ<sub>3</sub> (QCD factorization)  
(Beneke, Buchalla, Neubert, Sachrajda hep-ph/0104110)



φ<sub>3</sub> [ deg ]

# $B^- \rightarrow D^0 K^- (1)$

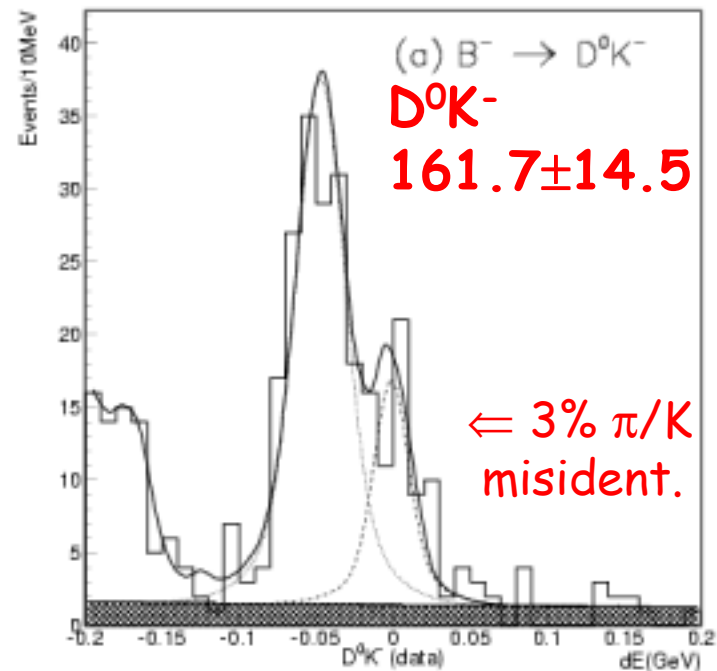


- interference of tree processes  $b \rightarrow c / b \rightarrow u$  in  $B^- \rightarrow D^0 K^- / \bar{D}^0 K^-$   
 $\Rightarrow \varphi_3$  measurement  
 several methods : Gronau, Wyler(91) ... Atwood, Dunietz, Soni(97)  
 e.g. charge asymmetries in  $B^\pm \rightarrow D_{1(2)} K^\pm$   
 $CP(D_1) = +, CP(D_2) = -$

However:

1. good PID needed to suppress  $D^0 \pi^\pm$   
 $BF(D^0 K^\pm) / BF(D^0 \pi^\pm) \approx 0.07$  (Belle)  $\Rightarrow$
2. Small ratio:  
 $r = A(B^- \rightarrow \bar{D}^0 K^-) / A(B^- \rightarrow D^0 K^-)$   
 $\approx |V_{ub}^* V_{cs}| / |V_{ub}^* V_{cs}| * [\text{col.sup.}]$   
 $\approx 0.4 * 0.25 \approx 0.1$   
 $\rightarrow$  asymmetries 'not large'
3.  $BF(D^0 \rightarrow X_{CP}) \approx 1\%$

$\Delta E$  calculated with  $\pi^\pm$  mass



(Preliminary)



# $B^- \rightarrow D^0 K^- (2)$



- Results for 31.1 M BB:

$$D_1 : K^+ K^-, \pi^+ \pi^-$$

$$D_2 : K_S^0 \pi^0, K_S^0 \omega, K_S^0 \phi, K_S^0 \eta(\gamma), K_S^0 \eta'(\eta \pi^+ \pi^-)$$

- Cabibbo suppression:

$$BF(D^0 K^-) / BF(D^0 \pi^-) = 0.094 \pm 0.009 \pm 0.007$$

$$BF(D_1 K^-) / BF(D_1 \pi^-) = 0.125 \pm 0.036 \pm 0.010$$

$$BF(D_2 K^-) / BF(D_2 \pi^-) = 0.119 \pm 0.028 \pm 0.006$$

- Charge asymmetries:

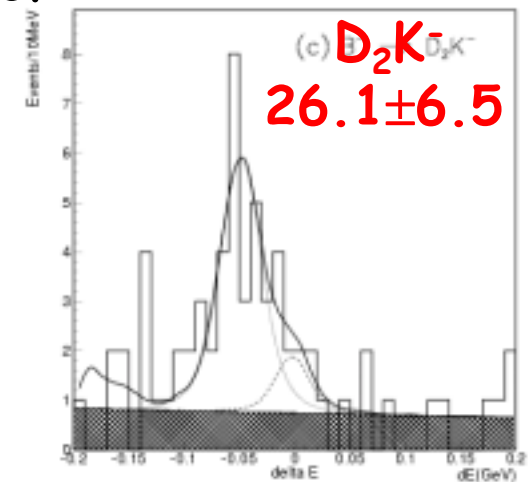
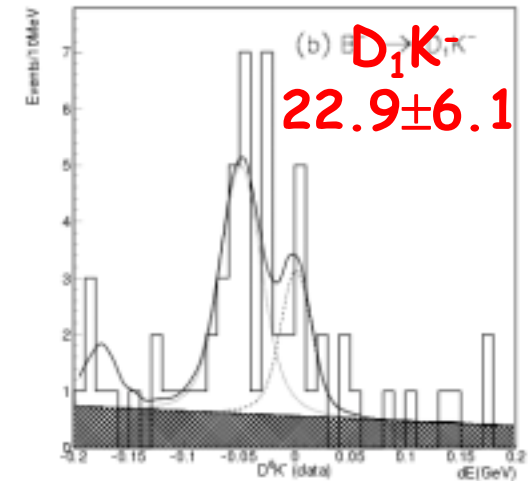
$$A_{CP}(D_1 K^-) = +0.29^{+0.29}_{-0.24} \pm 0.05 \quad (\delta A_{1(2)}, \delta R_{1(2)} \approx 0.1)$$

$$A_{CP}(D_2 K^-) = -0.22^{+0.26}_{-0.21} \pm 0.04 \quad @ 300 \text{ fb}^{-1}$$

$$A_{CP} = \frac{2r \sin \delta \sin \varphi_3}{1+r^2+2r \cos \delta \cos \varphi_3}$$

$$R_{1(2)} = \frac{BF(D_{1(2)} K^-) / BF(D_{1(2)} \pi^-)}{BF(D^0 K^-) / BF(D^0 \pi^-)}$$

$$(\delta \rightarrow \delta + \pi \text{ for } D_2)$$



(Preliminary)



- **Technique: 'ν reconstruction'** (good hermeticity and calorimetry needed)
- $B \rightarrow X l \bar{\nu} : \vec{p}_\nu = -\sum \vec{p}_i, P_\nu = (|\vec{p}_\nu|, \vec{p}_\nu)$   
(just another 4-momentum for  $\Delta E, M_{bc}$ )
- Cuts to improve resolutions: no other leptons in the event,  $|Q_{tot}| \leq 1$
- Consistency cuts:

$$|M_{miss}^2| = |E_{miss}^2 - p_\nu^2| < 2\text{GeV}^2$$

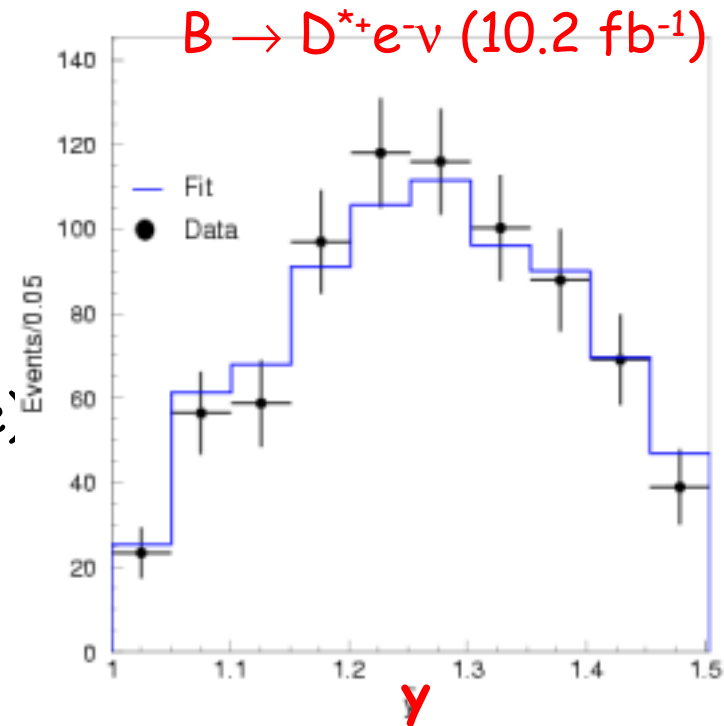
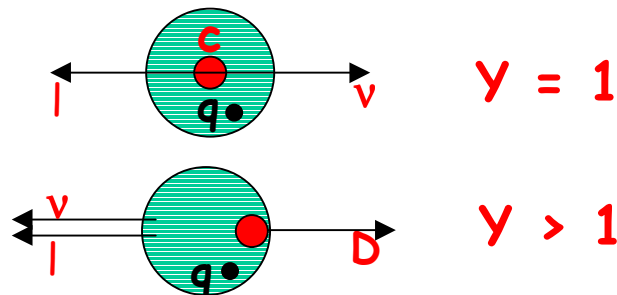
$$(E_{miss} = 2E_{beam} - \sum E_i)$$

$$|\cos\theta_{B,-Xl}| \leq 1$$

$$(\cos\theta_{B,-Xl} = (2E_B E_{Xl} - M_B^2 - M_{Xl}^2) / 2p_B p_{Xl})$$



$|V_{cb}|$  from  $dN/dy$ ;  $y = v_B v_{D^*}$   
( $\gamma(D^{(*)})$  in B rest frame)



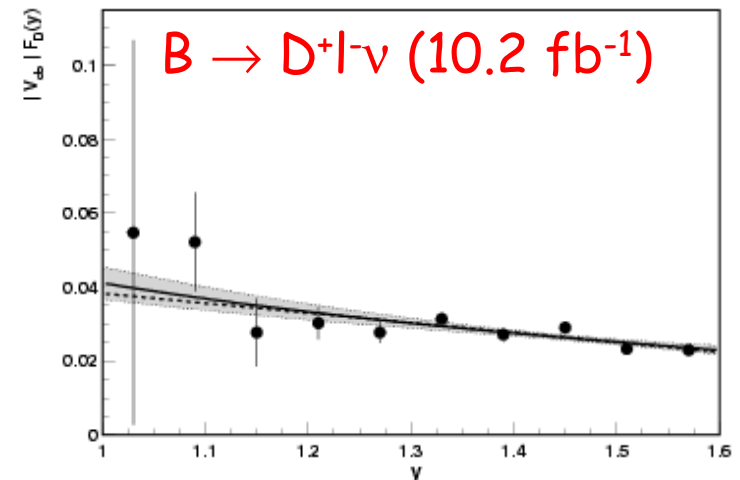
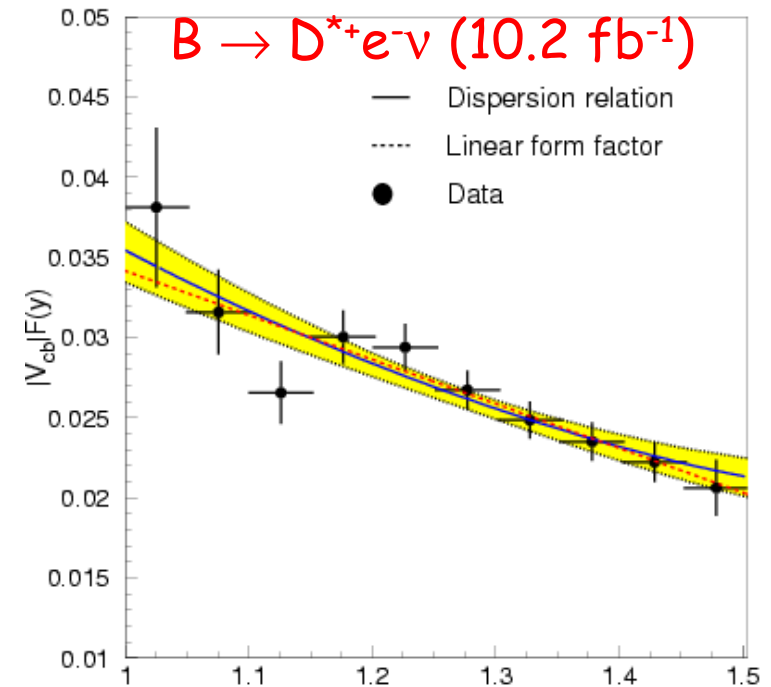


The decay rate:

$$\frac{d\Gamma}{dy} = \frac{G_F^2}{48\pi^3} |V_{cb}|^2 |F_D(y)|^2 K_D(y)$$

- $K_D(y)$  - known kinematic factors  
 $K_D \propto (y^2-1)^{3/2}$ ,  $K_{D^*} \propto (y^2-1)^{1/2}$   
 $\rightarrow$  at  $y=1$ : V-A kinematics favours  $D^* l \nu$
- $F_D(y)$  -  $B \rightarrow D^{(*)}$  form factor  
 HQET relations simplify the  $F_D$   
 HQS :  $M_Q \rightarrow \infty$ ,  $F(1) \rightarrow 1$   
 (+ HQS-breaking corr.)  
 QCD dispersion relations constrain  
 the shape:  $F_D = F(1)(1 - \rho^2(y-1) + \dots)$

Extrapolate to  $y=1$  to extract  $F(1)|V_{cb}|$   
 $\rightarrow F(1)|V_{cb}|$ ,  $\rho^2$  correlated



$$B \rightarrow D^{(*)+}l^- \nu$$



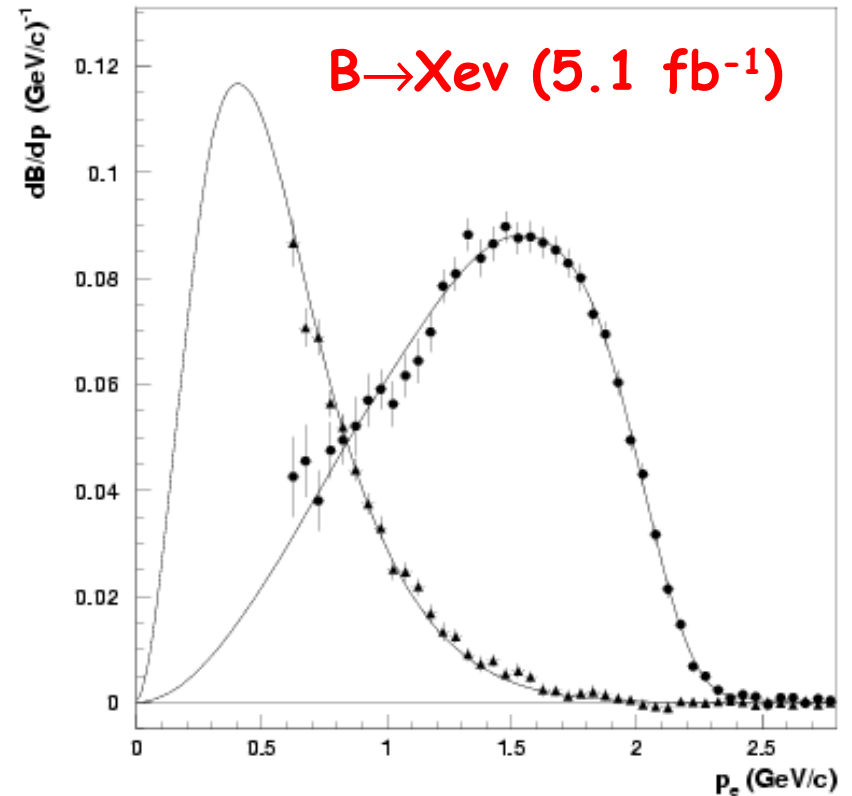
	$D^+l^- \nu$	$D^{*+}e^- \nu$
$ V_{cb} F_D(1)(\times 10^{-2})$	$4.11 \pm 0.44 \pm 0.52$	$3.54 \pm 0.19 \pm 0.18$
$\rho^2$	$1.12 \pm 0.22$	$1.35 \pm 0.17 \pm 0.19$
$F_D(1)$ used	$0.98 \pm 0.07$	$0.913 \pm 0.042$
$ V_{cb} (\times 10^{-2})$	$4.19 \pm 0.45 \pm 0.53 \pm 0.30$	$3.88 \pm 0.21 \pm 0.20 \pm 0.19$
BF (%)	$2.13 \pm 0.12 \pm 0.39$	$4.77 \pm 0.38 \pm 0.48$

- Dominant systematics:  $\nu$  reconstruction modeling, tracking efficiency,  $\pi_{\text{slow}}$  reconstruction
- $D^+l^- \nu$  less precise but valuable for  $F_D$  studies

# $B \rightarrow X e^+ \nu$



- $B\bar{B}$  tagged with a lepton ( $e, \mu$ )  
 $p^* > 1.4 \text{ GeV}$
- $B \rightarrow X e^+ \nu$  tagged with  $e^\pm$  on the 'other side'
- Lepton charge correlation to separate  
 $b \rightarrow l^-$  and  $b \rightarrow c \rightarrow l^+$
- $B^0 - \bar{B}^0$  mixing unfolded
- $BF(B \rightarrow X e \nu) = 10.86 \pm 0.14 \pm 0.47 \%$   
 $|V_{cb}| = (4.0 \pm 0.1 \pm 0.4) * 10^{-2}$   
(ISGW model)



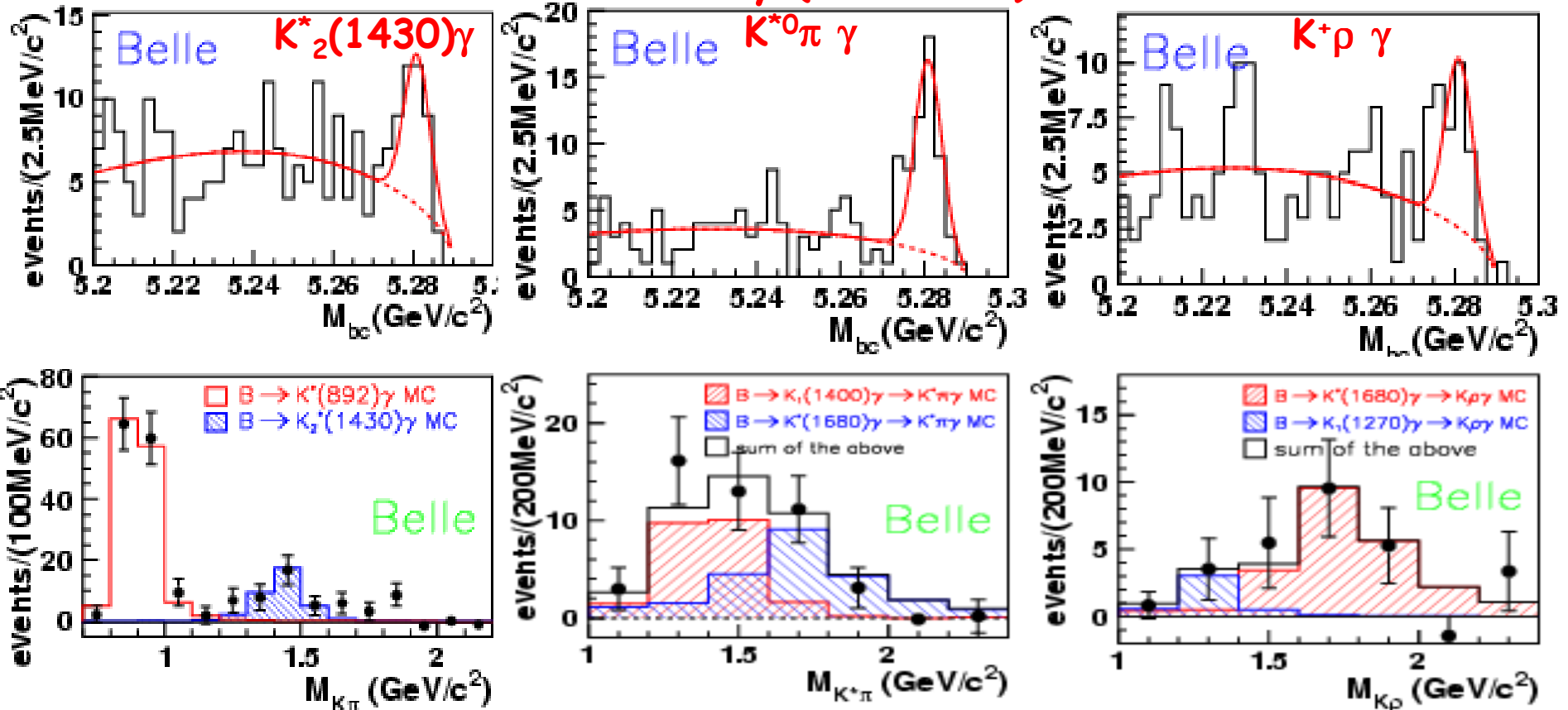
Preliminary

# Exclusive $B \rightarrow X_s \gamma$



- Semi-inclusive  $X_s \gamma$  ( $X_s = K + 1-4 \pi$ 's) difficult experimentally, nevertheless a big success of theory:
  - Belle ( $5.8 \text{ fb}^{-1}$ ):  $\text{BF}(B \rightarrow X_s \gamma) = (3.36 \pm 0.53 \pm 0.42 \pm 0.52) \cdot 10^{-4}$
  - Theory (NLO):  $(3.57 \pm 0.30) \cdot 10^{-4}$  (M. Misiak 2002)
- Try to decompose  $X_s$  into exclusive 'kaonic' final states

Preliminary ( $21.3 \text{ fb}^{-1}$ )



# Exclusive $B \rightarrow X_s \gamma$



	BF [ $10^{-5}$ ]
$K^{*0} \gamma$	$4.96 \pm 0.67 \pm 0.45$
$K^{*+} \gamma$	$3.89 \pm 0.93 \pm 0.41$
$K_2^{*0}(1430) \gamma$	$1.26 \pm 0.66 \pm 0.10$
$K^{*0} \pi^+ \gamma$	$5.6 \pm 1.1 \pm 0.9$
$K^+ \rho^0 \gamma$	$6.5 \pm 1.7 \pm 1.1$

**Preliminary (21.3 fb<sup>-1</sup>)**

- A large fraction (> 60%) of BF(  $X_s \gamma$  ) accounted for
- Interesting angular analyses possible in future (photon helicity measurement)
- $B \rightarrow p \gamma$  not seen yet :  $BF( p \gamma ) / BF( K^* \gamma ) < 0.19$  (90% C.L.)  
(preliminary, 10.4 fb<sup>-1</sup>)

# Summary



- Many new decay modes have been observed in the  $\leq 30 \text{ fb}^{-1}$  data sample
- Some of them start to be interesting for  $\varphi_3$  ,  $\varphi_1$  measurements
- Measurements of  $|V_{cb}|$  ,  $|V_{ub}|$  are steadily improving
- Many new analyses are becoming possible with the large data sample