

# Particle Candidates for Dark Matter

(A. BOTTINO)

- ▷ Need for (and amount of) dark matter in the Universe
- ▷ Particle candidates for dark matter
- ▷ Supersymmetric particles as Weakly Interacting Massive Particles (WIMP)
- ▷ Probing the supersymmetric parameter space by WIMP direct detection
- ▷ Constraints from indirect searches for WIMPs
- ▷ Implications of a possible susy Higgs boson at a mass of 115 GeV (a hint from LEP2 ?)

## Dark Matter in the Universe

- ▷ Existence of dark matter required by a host of observational data:  
galactic halos, clusters of galaxies, large scale structures, CMB, high-redshift SNe Ia, ...

$$\boxed{0.05 \lesssim \Omega_m h^2 \lesssim 0.3} \quad (\text{conservative range})$$

$$\Omega_m \equiv \rho_m / \rho_c, \quad \rho_c = 1.88 \times 10^{-29} h^2 \text{ g} \cdot \text{cm}^{-3}$$

$$h \equiv H_0 / (100 \text{ km} \cdot \text{s}^{-1} \cdot \text{Mpc}^{-1}), \quad 0.6 \lesssim h \lesssim 0.8$$

- ▷ visible matter

$$\Omega_v \sim 0.003$$

- ▷ baryonic matter

\* from BBN  $0.018 \lesssim \Omega_b h^2 \lesssim 0.020$  (low D)

$$0.03 \lesssim \Omega_b \lesssim 0.06$$

\* CMB points to a somewhat higher value:  $\Omega_b h^2 \sim 0.03$

\* hard to build a Universe dominated by baryons

(Griffiths, Melchiorri and Silk: astro-ph/0101413)

Thus, some dark matter is baryonic, but most of it is non-baryonic

- ▷ Particle physics, for its own motivations, provides a number of possible relics

## Particle Physics

## DM Candidates

Neutrino physics  
related to  $\nu$  masses



light  $\nu$ 's  
heavy  $\nu$ 's

Supersymmetry



Lightest Susy Particle  
(neutralino, ...)

Strong CP-problem



axion

String theories



...

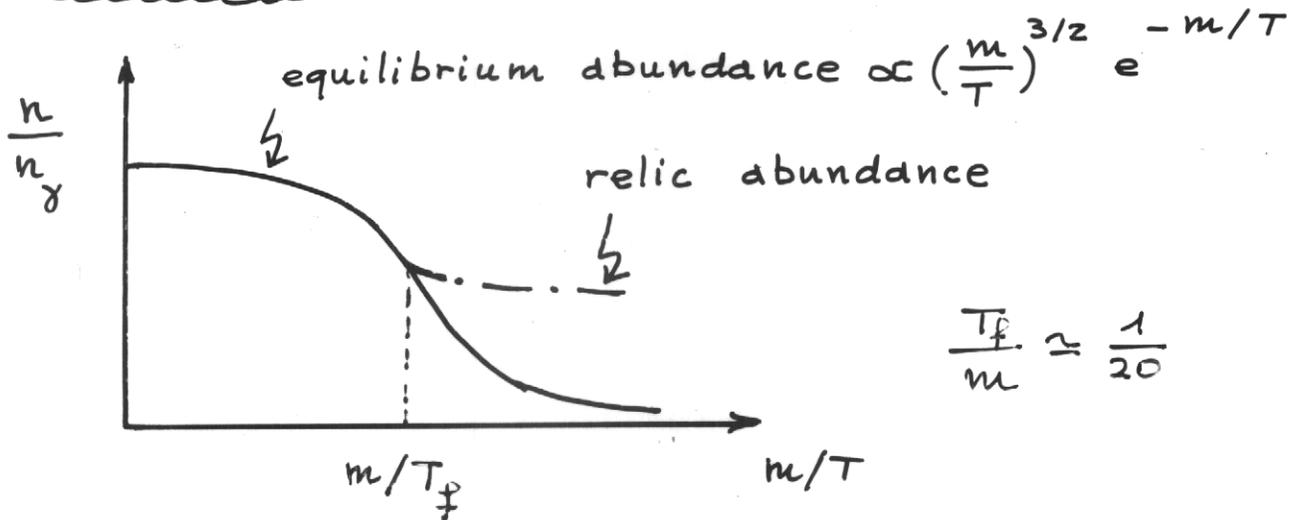
Topological defects associated with  
spontaneous symmetry breaking:  
monopoles, ...

## Thermal relics

▶ hot relics

relic abundance  $\approx$  abundance at equilibrium  
(almost independent of  $T_f$ )

▶ cold relics



$n \equiv$  density per comoving volume

relic abundance  $\Omega h^2 \approx \frac{10^{-37} \text{ cm}^2}{\langle \sigma_{ann} v \rangle}$

then the relic abundance of a weakly interacting particle may be sizeable

### Different scenarios

\* decoupling of particles which were never in chemical equilibrium

(see Giudice, Kolb and Riotto: hep-ph/0005123)

\* non-thermal production

## Relic neutrinos

For light ( $m_\nu \leq \text{MeV}$ ) neutrinos

$$\Omega_\nu h^2 = \frac{\sum_\nu m_\nu}{93 \text{ eV}} \quad \text{relic abundance}$$

For instance, to have  $\Omega_\nu \sim 0.1$  ( $0.6 \leq h \leq 0.8$ )

$$3.3 \text{ eV} \leq \sum_\nu m_\nu \leq 6.0 \text{ eV}$$

### Experimental indications of $\nu$ masses:

- a) solar  $\nu$ 's  $\Delta m^2 \sim 10^{-5} \div 10^{-4} \text{ eV}^2$  (if MSW)
- b) atmospheric  $\nu$ 's  $\Delta m^2 \sim (1 \div 8) \times 10^{-3} \text{ eV}^2$
- c) LSND  $0.2 \text{ eV}^2 \leq \Delta m^2 \leq 1 \text{ eV}^2$

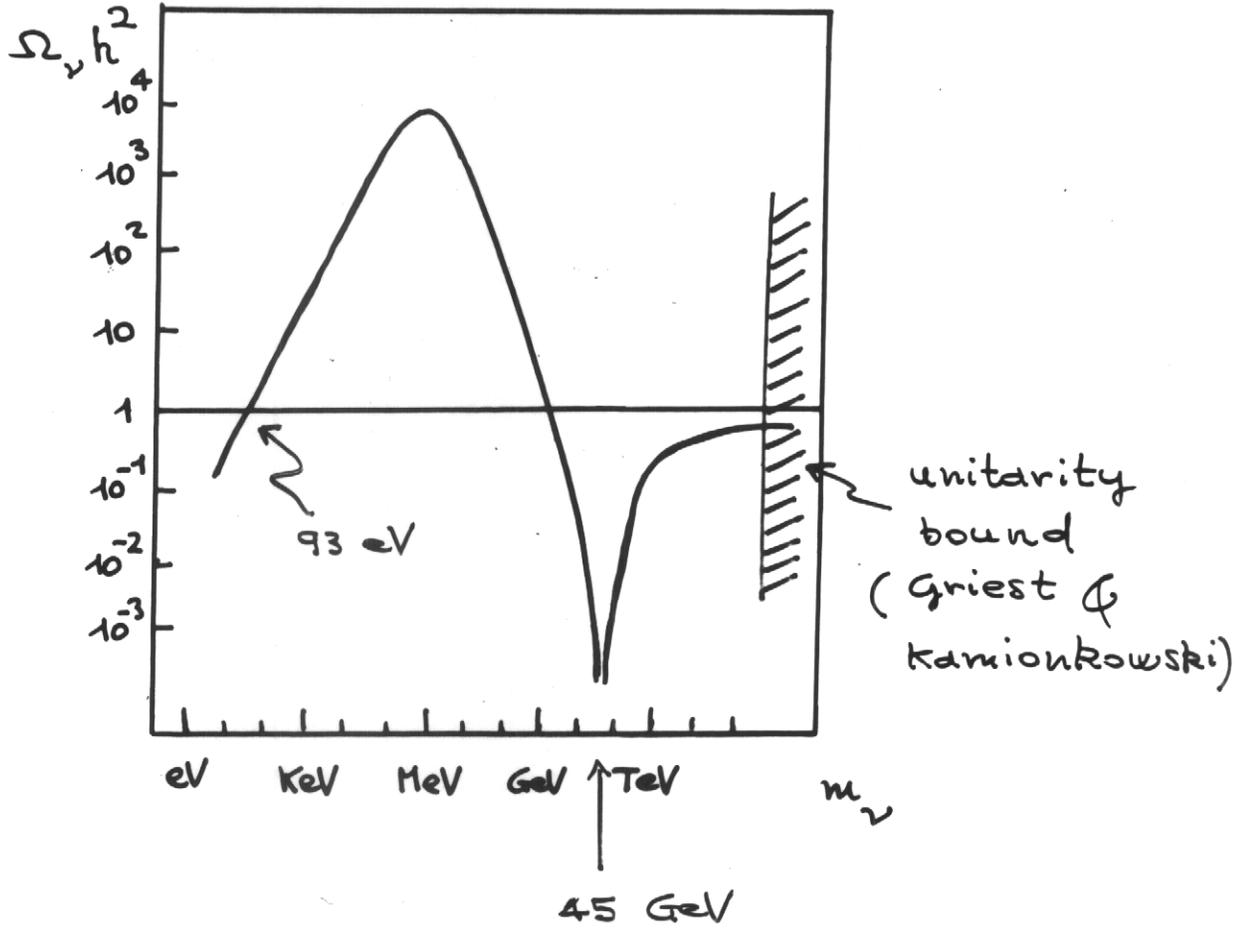
From the atmospheric  $\nu$  deficit, a very conservative estimate:

$$m_\nu \gtrsim 0.05 \text{ eV}$$

$$\Omega_\nu h^2 \gtrsim 6 \times 10^{-4}$$

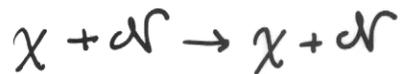
$$\Omega_\nu \gtrsim 0.001 \left( \frac{0.7}{h} \right)^2 \quad \text{not cosmologically interesting}$$

However,  $\Omega_\nu$  could be sizeably larger in case of a substantial degeneracy in  $\nu$  masses



## Searches for relic neutralinos

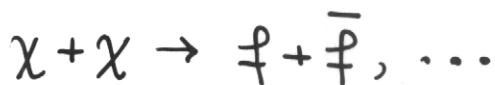
- ▶ direct search: elastic scattering of  $\chi$  off nuclei



- ▶ indirect searches:

\* signals due to  $\chi$ - $\chi$  annihilations taking place in celestial bodies (where  $\chi$ 's have been accumulated)  $\rightarrow \nu$ 's  $\rightarrow$  up-going  $\mu$ 's (Earth, Sun)

\* signals due to  $\chi$ - $\chi$  annihilations taking place in the halo



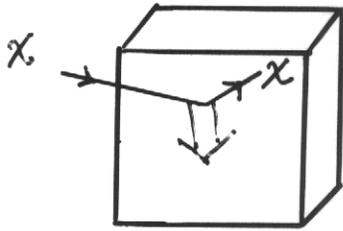
$\begin{array}{l} \hookrightarrow \nu, \bar{\nu} \\ \hookrightarrow \gamma \end{array} \left. \vphantom{\begin{array}{l} \hookrightarrow \nu, \bar{\nu} \\ \hookrightarrow \gamma \end{array}} \right\} \begin{array}{l} \text{keep directionality,} \\ \text{detectable if emitted} \\ \text{by regions of high } \chi \text{ density} \end{array}$

$\hookrightarrow$  gamma line  
( $2\gamma$ )



$\begin{array}{l} \hookrightarrow \bar{p} \\ \hookrightarrow e^+ \\ \hookrightarrow \bar{d} \end{array} \left. \vphantom{\begin{array}{l} \hookrightarrow \bar{p} \\ \hookrightarrow e^+ \\ \hookrightarrow \bar{d} \end{array}} \right\} \begin{array}{l} \text{searched for as} \\ \text{rare components} \\ \text{in cosmic rays} \end{array}$

# Direct search: $\chi$ -nucleus scattering



Ge  
NaI  
Xe  
TeO<sub>2</sub>  
.....

$$E_R = \frac{\vec{q}^2}{(2m_N)}$$

$\chi$ -velocity distribution  
in the Galaxy

Differential rate

$$\frac{dR}{dE_R} = N_T \frac{P_\chi}{m_\chi} \int_{v_{\min}}^{v_{\max}} dv f(v) v \left\{ \frac{d\sigma^c}{dE_R} + \frac{d\sigma^{SD}}{dE_R} \right\}$$

coherent  
(dominant)

spin dependent

$$\frac{d\sigma^c}{dE} \propto F(q)^2 A^2 \sigma_{\text{scalar}} \quad (\text{nucleon})$$

- Discrimination of the signal against the background is based on the expected annual modulation of the signal

Drukier, Freese and Spergel (1986)

Freese, Frieman and Gould (1988)

Usually, from the experimental data one extracts

$$\frac{dR}{dE_R} \rightarrow \rho_X \sigma_{\text{scalar}}^{(\text{nucleon})} \equiv \rho_l \underbrace{\frac{\rho_X}{\rho_l}}_{\rho_l} \sigma_{\text{scalar}}^{(\text{nucleon})}$$

assuming:

- 1) a Maxwell-Boltzmann speed distribution for  $f(v)$
- 2) dominance of the coherent cross-section over the spin-dependent one.

Caveats! See later on.

Notice that, to get  $\sigma_{\text{scalar}}^{(\text{nucleon})}$ , the uncertainty range for  $\rho_l$

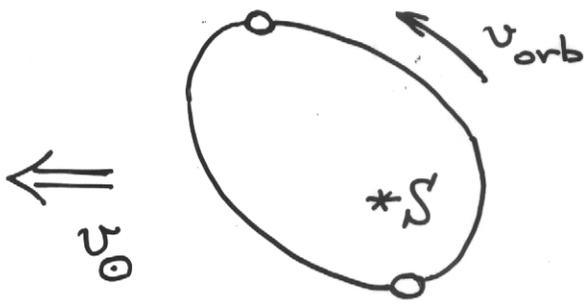
$$(0.1-0.2) \text{ GeV} \cdot \text{cm}^{-3} \lesssim \rho_l \lesssim 0.7 \text{ GeV} \cdot \text{cm}^{-3}$$

has to be taken into account.

"Default" value for  $\rho_l$ :  $\rho_l = 0.3 \text{ GeV} \cdot \text{cm}^{-3}$

$$\text{definition: } \rho_l^{0.3} \equiv \rho_l / (0.3 \text{ GeV} \cdot \text{cm}^{-3})$$

# Annual modulation



speed of the solar system in the Galactic Rest Frame

$$v_{\odot} = \underbrace{(220 \pm 30) \text{ km} \cdot \text{s}^{-1}}_{v_0} + 12 \text{ km} \cdot \text{s}^{-1}$$

peculiar velocity

speed of the earth in the GRF

$$v_{\oplus}(t) = v_{\odot} + v_{\text{orb}} \cos \gamma \cos [\omega(t - t_0)]$$

$\uparrow$  earth orbital speed       $\uparrow$  orbit inclination ( $\gamma = 60^\circ$ )

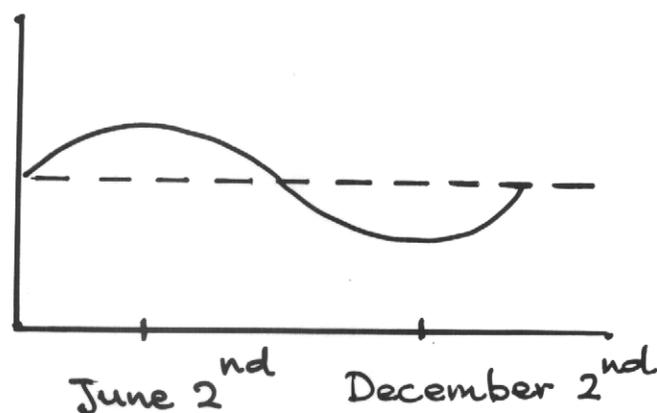
$\frac{2\pi}{1\text{yr}}$       June 2<sup>nd</sup>

Defining  $\eta(t) \equiv v_{\oplus}(t)/v_0$  ,  $\eta_{\text{av}} \equiv v_{\odot}/v_0$

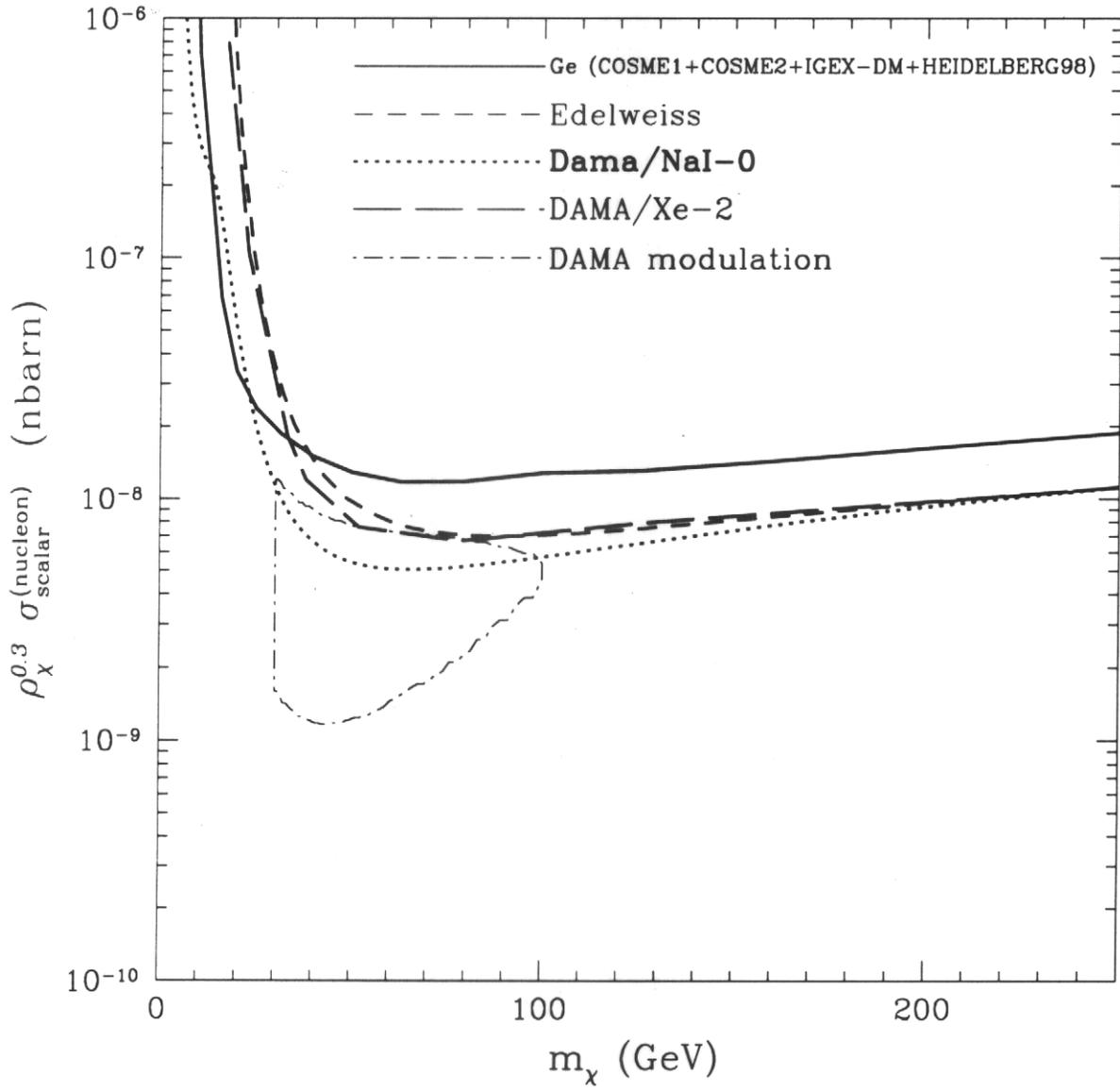
$$\eta(t) = \eta_{\text{av}} + \Delta\eta \cos[\omega(t - t_0)]$$

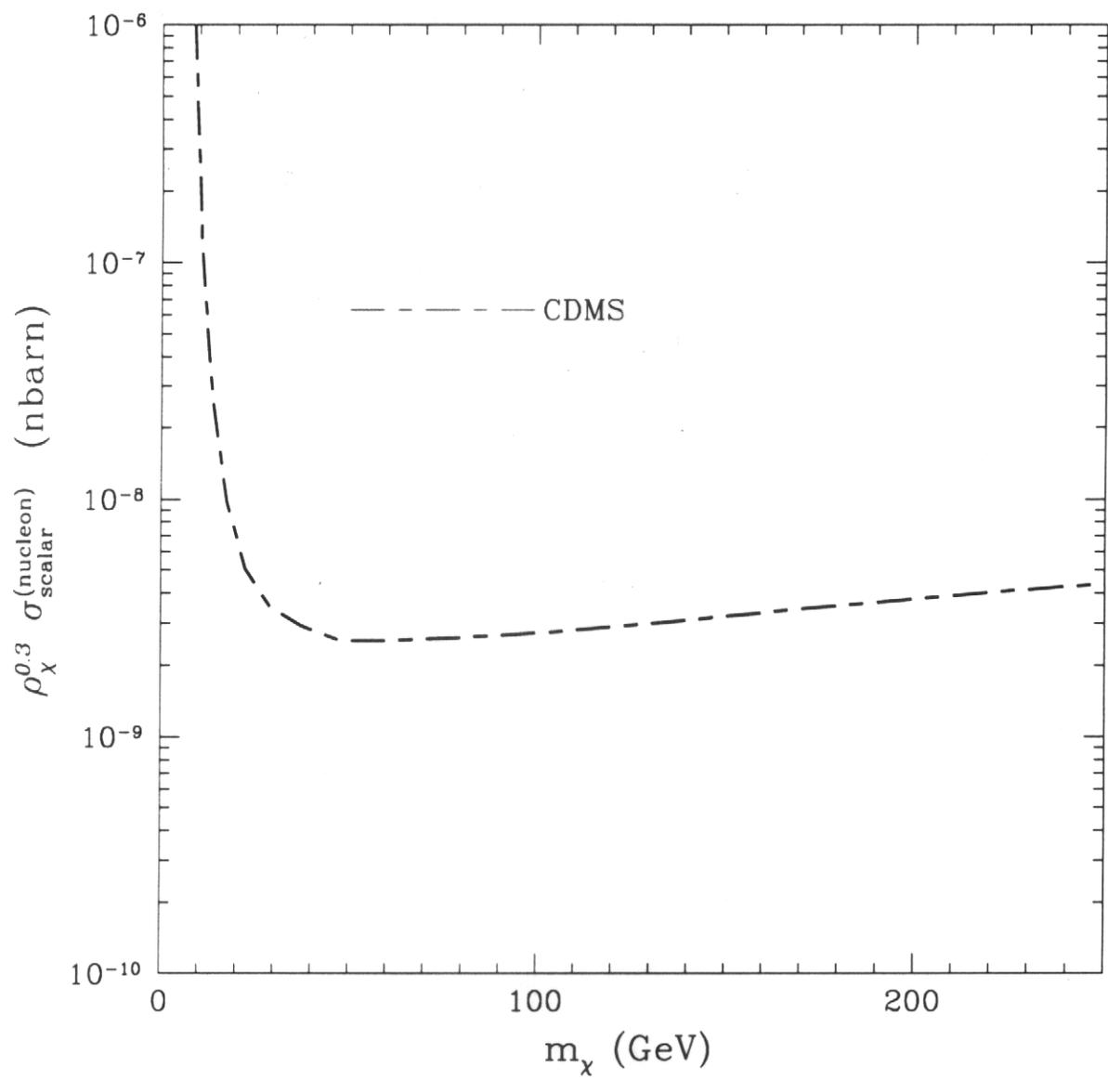
$$\eta_{\text{av}} = 1.05 , \quad \Delta\eta = 0.07$$

signal



$v_0 = 220 \text{ km s}^{-1}$





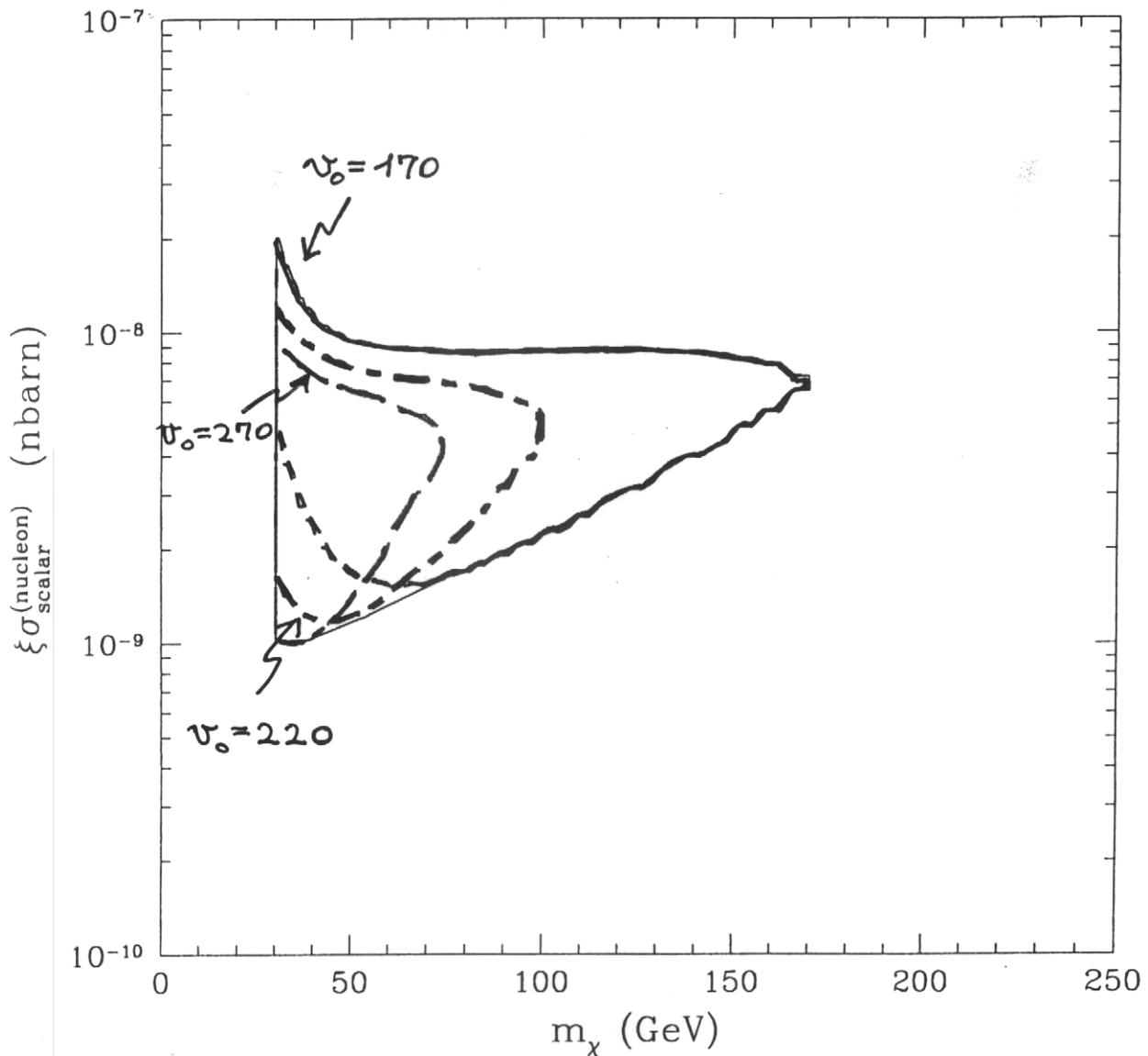
DAMA 3 $\sigma$  C.L. annual-modulation region

(exposure: 57986 kg·day)

Bernabei et al., Phys. Lett. B480 (2000) 23

preprint INFN/AE-00/01 ([www.lngs.infn.it](http://www.lngs.infn.it))

$$\rho_l = 0.3 \text{ GeV}\cdot\text{cm}^{-3}, \quad v_0 \text{ in km}\cdot\text{sec}^{-1}$$



What if we go beyond the standard Maxwell-Boltzmann velocity distribution?

### Recent investigations

\* Bulk rotation of the dark halo

Kamionkowski and Kinkhabwala, Phys. Rev. D57(1998) 3256

Donato, Fornengo and Scopel, Astrop. Phys. 9(1998) 247

Belli et al., Phys. Rev. D61(2000) 023512

\* Anisotropy in WIMP velocities

Vergados, Phys. Rev. D62(2000) 023519

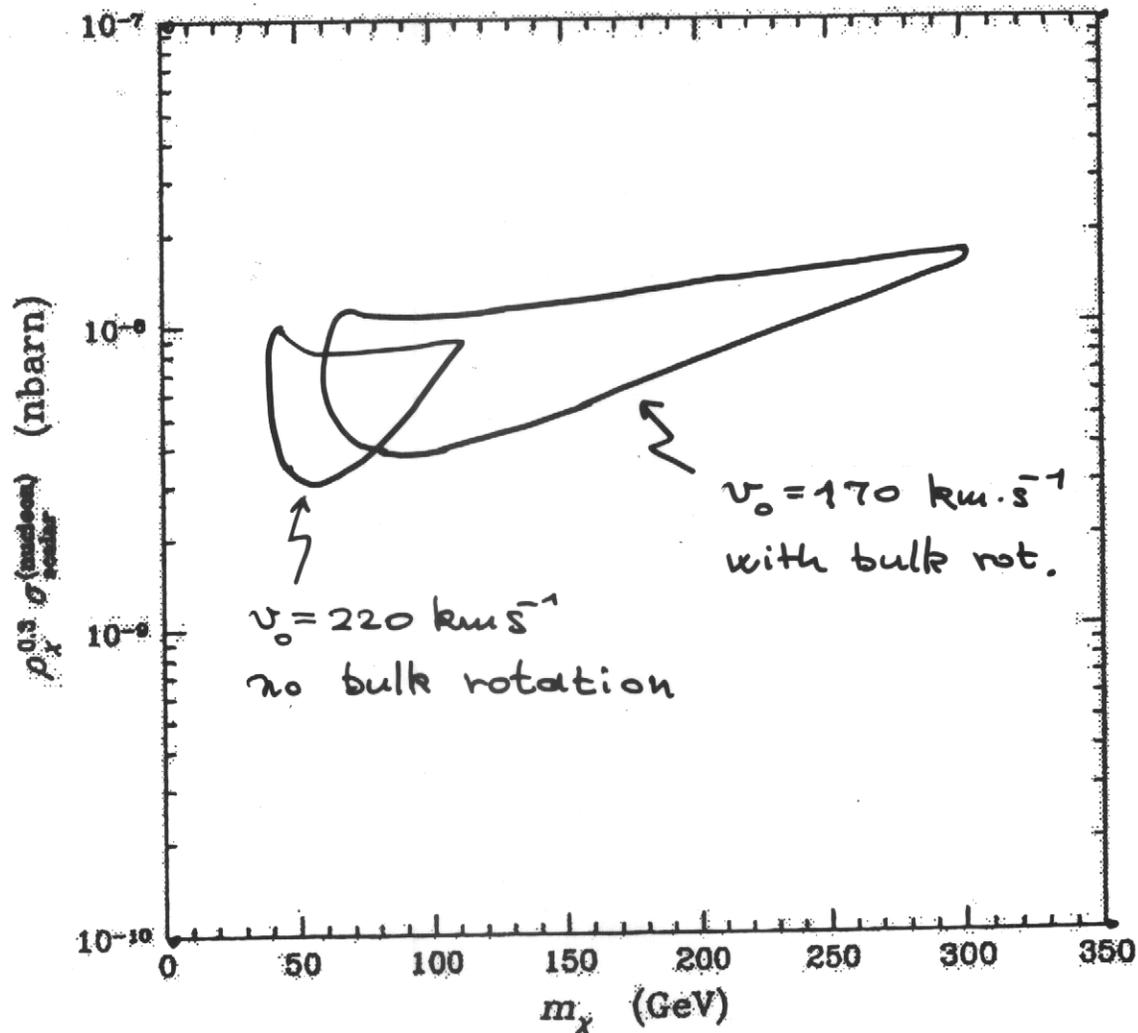
Ullio and Kamionkowski, hep-ph/0006183

Evans, Carollo and de Zeeuw, astro-ph/0008156

A.M. Green, astro-ph/0008318

Effect of a bulk rotation of the dark halo  
(and of the dispersion velocity  $v_0$ ).

From Belli et al., Phys. Rev. D 61 (2000) 023512



For the effect of dependence on  $v_0$  (no bulk rotation) see also

Brhlik and Roszkowski, Phys. Lett. B464 (1999) 303

Effect of an asymmetry in the WIMP velocity distribution from

A.M. Green, astro-ph/0008318

The parameter  $\lambda$  ( $0 \leq \lambda \leq 1$ ) quantifies the deviation from an isotropic distribution ( $\lambda=0$ )

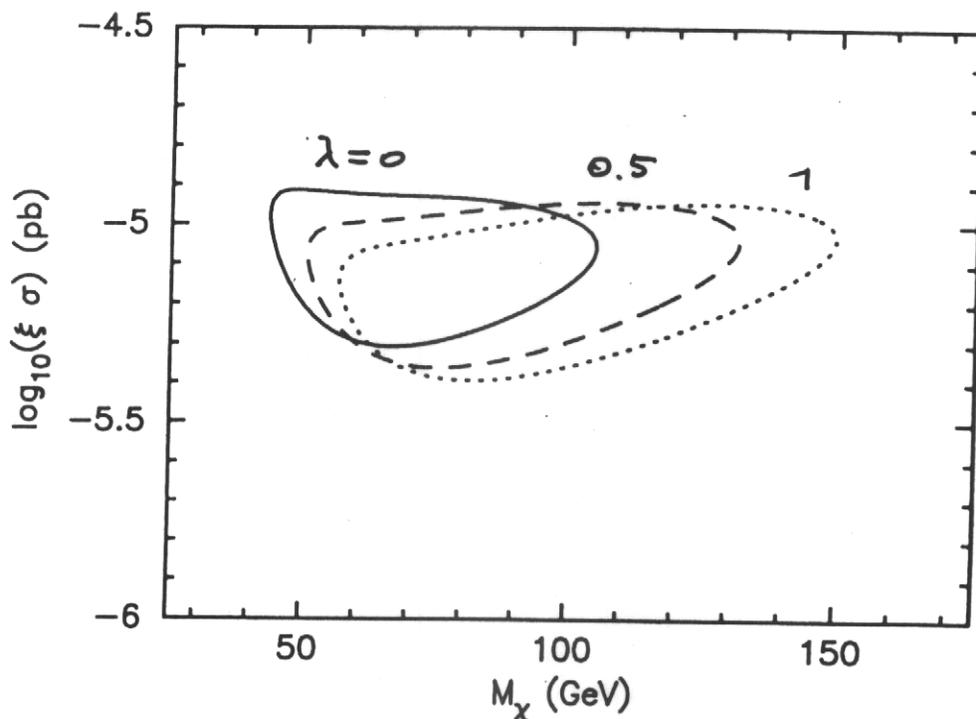


FIG. 4. The  $\kappa = 35$  contour, delineating the region of  $m_\chi - \xi\sigma$  parameter space compatible with the DAMA annual modulation signal, for asymmetric halo models with  $\lambda = 0, 0.5, 1$  (solid, dashed and dotted lines respectively).

► Previous arguments show that for WIMP masses in the range

$$40 \text{ GeV} \lesssim m_{\chi} \lesssim 200 \text{ GeV}$$

current experiments of direct detection are sensitive to

$$10^{-9} \text{ nbarn} \lesssim \rho_{\chi} \sigma_{\text{scalar}}^{(nucleon)} \lesssim 10^{-8} \text{ nbarn}$$

$$\Rightarrow 4 \times 10^{-10} \text{ nbarn} \lesssim \sigma_{\text{scalar}}^{(nucleon)} \lesssim 2 \times 10^{-8} \text{ nbarn}$$

► Questions:

1) Is this range of  $\sigma_{\text{scalar}}^{(nucleon)}$  compatible with relic neutralinos?

2) Does it involve neutralino relic abundances of cosmological interest?

Answers to both questions are: Yes!

## Supersymmetry

- ▷ strong theoretical motivations
  - \* fermion-boson symmetry
  - \* stability of scalar masses
  - \* unification with gravity in supergravity theories
  
- ▷ it would help unification of coupling constants at  $M_{GUT}$
  
- ▷ but no experimental confirmation is available yet
  - \* only a number of constraints on Susy parameters are derivable from accelerators

# Supersymmetry

► Susy with R-parity conservation entails that the Lightest Susy Particle is stable.

► Depending on the Susy scheme and on the sector of the Susy parameter space the LSP could be:

squark

slepton (charged)

sneutrino

neutralino

gravitino

axino

...

} good candidates  
for  
dark matter

► The neutralino is a particularly interesting case of WIMP, since:

\* it may be of cosmological relevance

$$(0.05 \lesssim \Omega_\chi h^2 \lesssim 0.3)$$

\* it may be detectable (direct & indirect)

Definition: linear combination

$$\chi = a_1 \tilde{B} + a_2 \tilde{W}^{(3)} + a_3 \tilde{H}_1^{(0)} + a_4 \tilde{H}_2^{(0)}$$

of lowest mass  $m_\chi$ .

## Susy schemes (gravity-mediated)

- ▷ Universal SUGRA: unification conditions for the soft Susy-breaking terms at  $M_{\text{GUT}} \sim 10^{16}$  GeV
- ▷ However, the unification scale is largely uncertain.

This implies that at  $M_{\text{GUT}}$ , significant deviations from universality may occur; typically, for scalar soft masses.

The resulting Susy phenomenology at the EW scale is largely affected by these deviations.       $\nu$ SUGRA

- ▷ Effective model: MSSM at the EW scale  
a few mass parameters which set the most relevant scales:  $\text{effMSSM}$
- ▷ Extensions:

- \* deviations from gaugino unification
- \* CP-violating phases

...  
...

## (universal) SUGRA

$m_{1/2}$  gaugino mass

$m_0$  scalar mass

$A_0$  trilinear coupling

$$\tan \beta = \frac{\langle H_2 \rangle}{\langle H_1 \rangle}$$

$\text{sign}(\mu)$  ( $\mu =$  Higgs-mixing coupling)

## nu SUGRA

deviations from universality in the Higgs masses at  $M_{\text{GUT}}$  is allowed

$$m_{H_i}^2(M_{\text{GUT}}) = m_0^2 (1 + \delta_i)$$

## eff MSSM

\* Minimal Supersymmetric extension of the Standard Model (MSSM) at the electroweak scale ( $M_Z$ ), described by

$$\tan \beta = \frac{\langle H_2 \rangle}{\langle H_1 \rangle}$$

$M_2$  SU(2) gaugino mass ( $M_1 = \frac{5}{3} \tan^2 \theta_w \cdot M_2$  is assumed)

$\mu$  Higgs-mixing parameter

$m_A$  CP-odd neutral Higgs boson (or  $m_h$ )

$m_{0\tilde{q}}, m_{0\tilde{\ell}}$  squark, slepton masses

$A$  trilinear coupling

\* the supersymmetric parameter space is constrained

by

□ experimental bounds from accelerators on supersymmetric and Higgs searches

□ constraints from  $b \rightarrow s + \gamma$

□ condition that neutralino is the LSP

□ cosmological bound  $\Omega_x h^2 < 0.7$



muon anomalous magnetic moment  
( $g-2$ ) : deviation from SM prediction ?

In Susy we can calculate

\* for the neutralino-nucleus interaction

$$\sigma_{\text{coherent}} > \sigma_{\text{spin-dependent}}$$

$$\downarrow \text{(nucleon)}$$
$$\sigma_{\text{scalar}}$$

( $\sigma_{\text{coherent}} \gg \sigma_{\text{spin-dependent}}$  in the range for  $\sigma$  considered here)

\* for neutralino-neutralino annihilation

$$\sigma_{\text{ann}} \rightarrow \Omega_{\chi} h^2 \sim \frac{1}{\langle v \sigma_{\text{ann}} \rangle}$$

▷ Notice that  $\sigma_{\text{scalar}}^{(\text{nucleon})} \sim \sigma_{\text{ann}}$

(i.e.  $\sigma_{\text{scalar}}^{(\text{nucleon})}$  &  $\sigma_{\text{ann}}$  are both increasing or decreasing functions in terms of typical Susy parameters)

thus

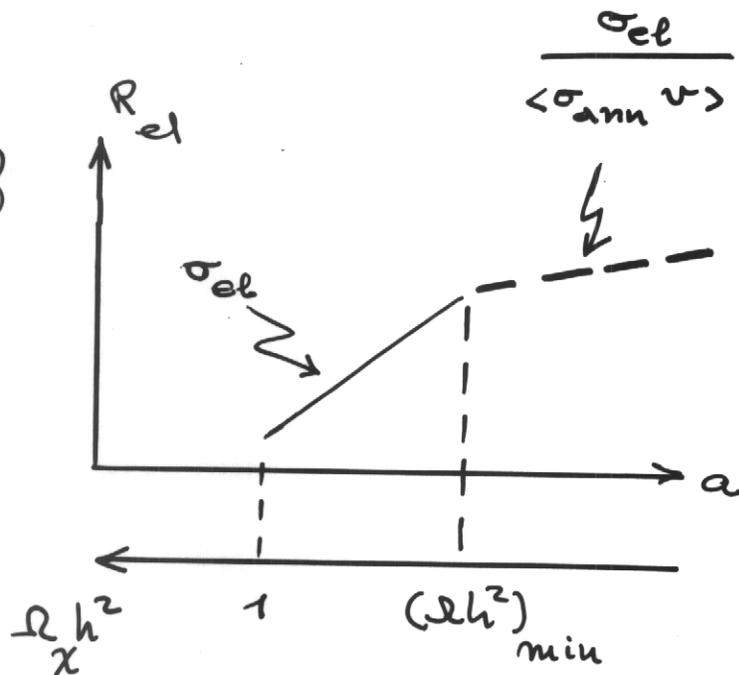
$$\Omega_{\chi} h^2 \sim \frac{1}{\sigma_{\text{scalar}}^{(\text{nucleon})}}$$

## Estimate of neutralino local density (rescaling)

$$\rho_\chi = \xi \rho_\ell = \begin{cases} \rho_\ell & \text{if } \Omega_\chi h^2 \geq (\Omega h^2)_{\min} \\ \frac{\Omega_\chi h^2}{(\Omega h^2)_{\min}} \rho_\ell \propto \frac{1}{\langle \sigma_{\text{ann}} v \rangle} \rho_\ell & \text{if } \Omega_\chi h^2 < (\Omega h^2)_{\min} \end{cases}$$

$$R_{\text{el}} \propto \rho_\chi \sigma_{\text{el}} \propto \begin{cases} \sigma_{\text{el}} & \text{if } \Omega_\chi h^2 \geq (\Omega h^2)_{\min} \\ \frac{\sigma_{\text{el}}}{\langle \sigma_{\text{ann}} v \rangle} & \text{if } \Omega_\chi h^2 < (\Omega h^2)_{\min} \end{cases}$$

a is a generic parameter (e.g.,  $\tan \beta$ )



Neutralinos of lower densities ( $\Omega_\chi h^2$  &  $\rho_\chi$ ) may be more easily detected by WIMP direct detection

A.B., de Alfaro, Fornengo, Mignola and Scopel,

Astrop. Phys. 2 (1994) 77

Some recent theoretical papers on evaluation  
of  $\Omega_{\tilde{\chi}} h^2$  and  $\sigma_{\text{scalar}}^{(\text{nucleon})}$  in various susy schemes:

Bottino, Donato, Fornengo and Scopel:

Phys. Lett. B 423(1998) 109; Phys. Rev. D 59(1999) 095003;

Phys. Rev. D 59(1999) 095004; Astrop. Phys. 13(2000) 215;

Phys. Rev. D 62(2000) 056006

Belli et al.: Phys. Rev. D 61(1999) 023512

Arnowitz and Nath: Phys. Rev. D 60(1999) 044002

Bednyakov and Klapdor-Kleingrothaus: Phys. Rev. D 62  
(2000) 043524

Ellis, Ferstl and Olive: Phys. Lett. B 481(2000) 304;

Phys. Rev. D 63(2001) 065016

Accomando, Arnowitz, Dutta and Santofo: Nucl. Phys. B 585  
(2000) 124

Corsetti and Nath: hep-ph/0003186

Gabrielli, Khalil, Muñoz and Torrente-Lujan:

Phys. Rev. D 63(2001) 025008

Feng, Matchev and Wilczek: Phys. Lett. B 482(2000) 388

Mandic, Pierce, Gondolo and Murayama, hep-ph/0008022

v2

Gómez and Vergados: hep-ph/0012020

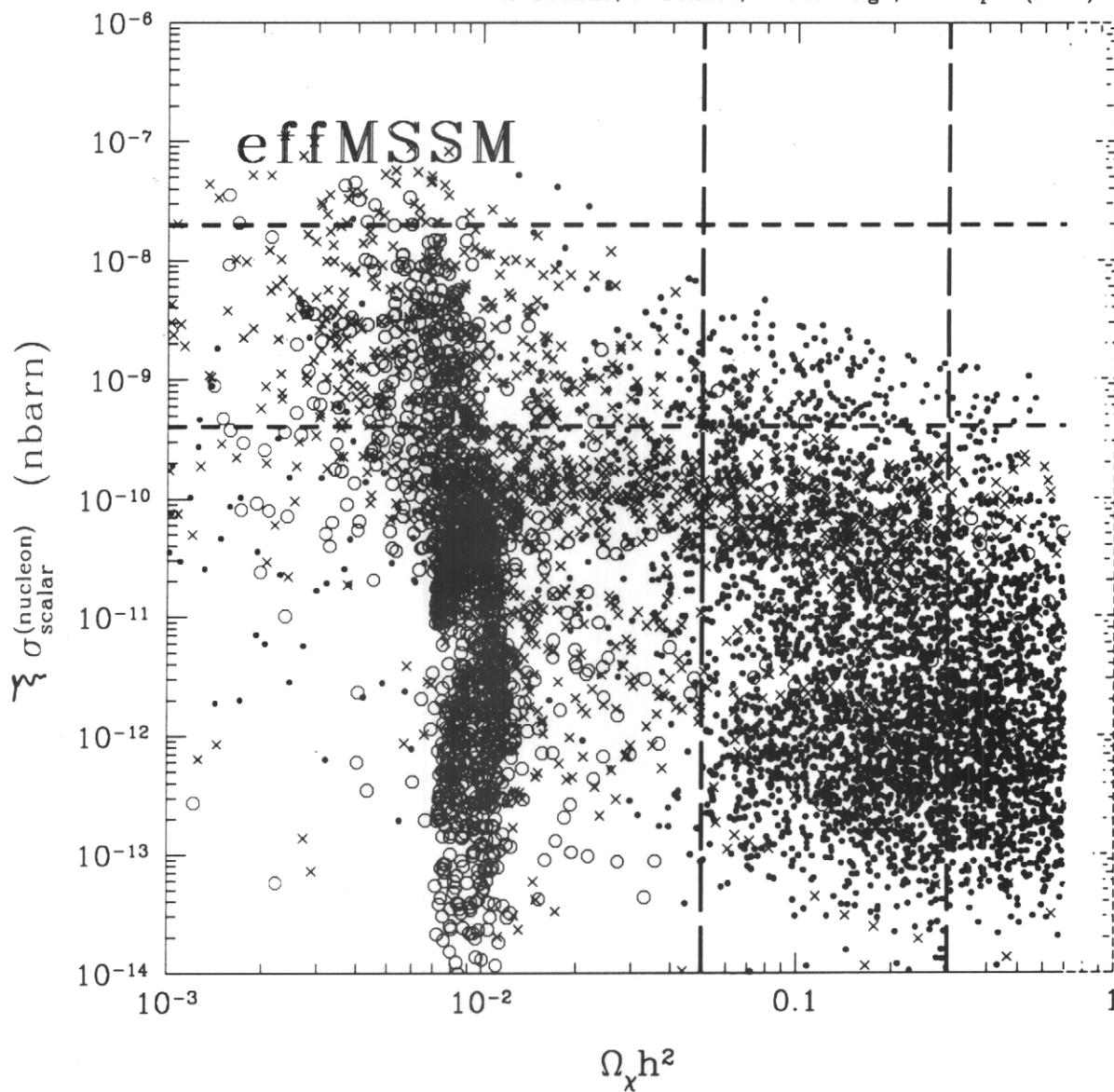
Murakami and Wells: hep-ph/0011082

Lahanas, Nanopoulos and Spanos: hep-ph/000965

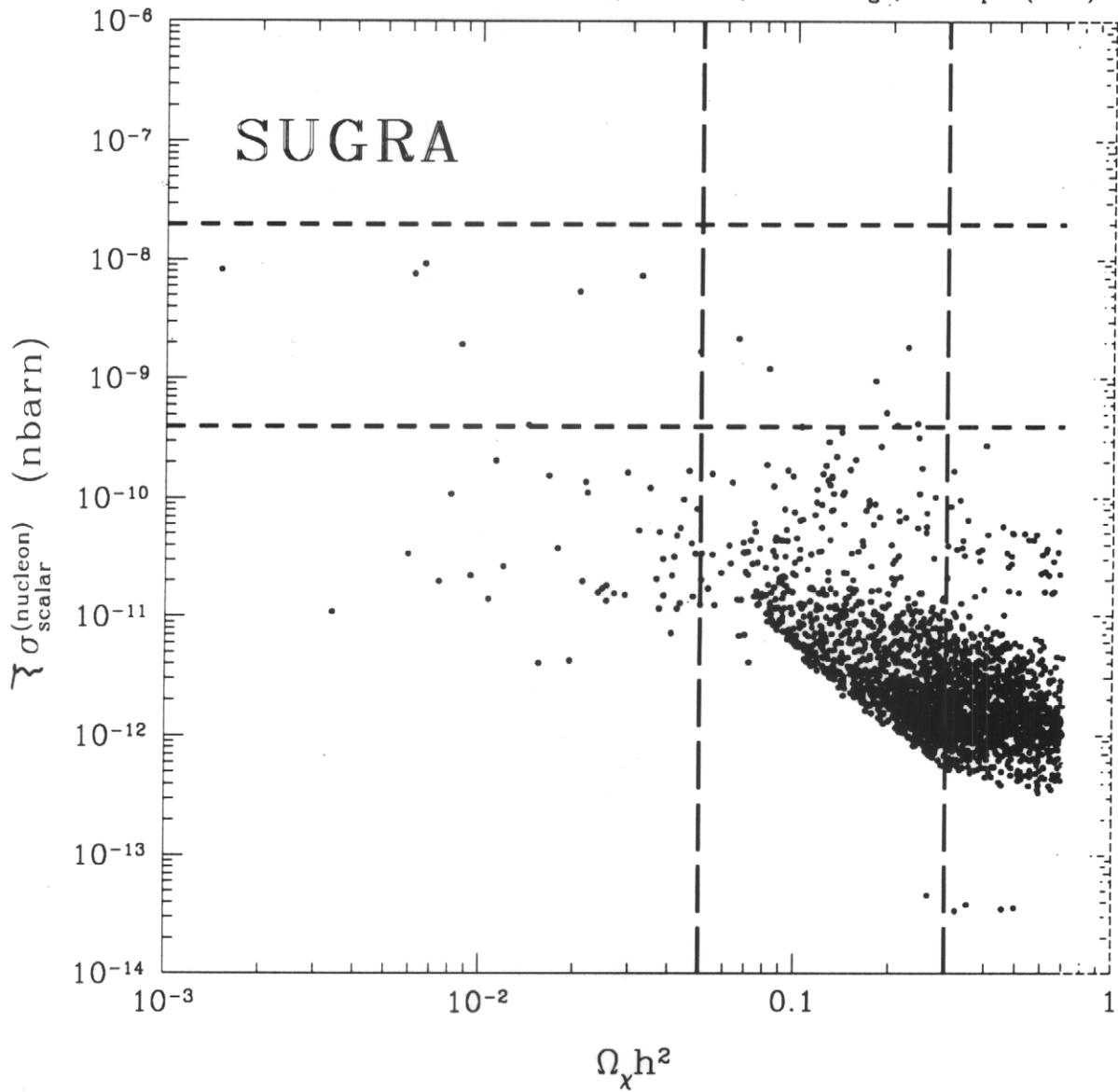
In the following we present the results  
obtained in

A.B., Donato, Fornengo and Scopel

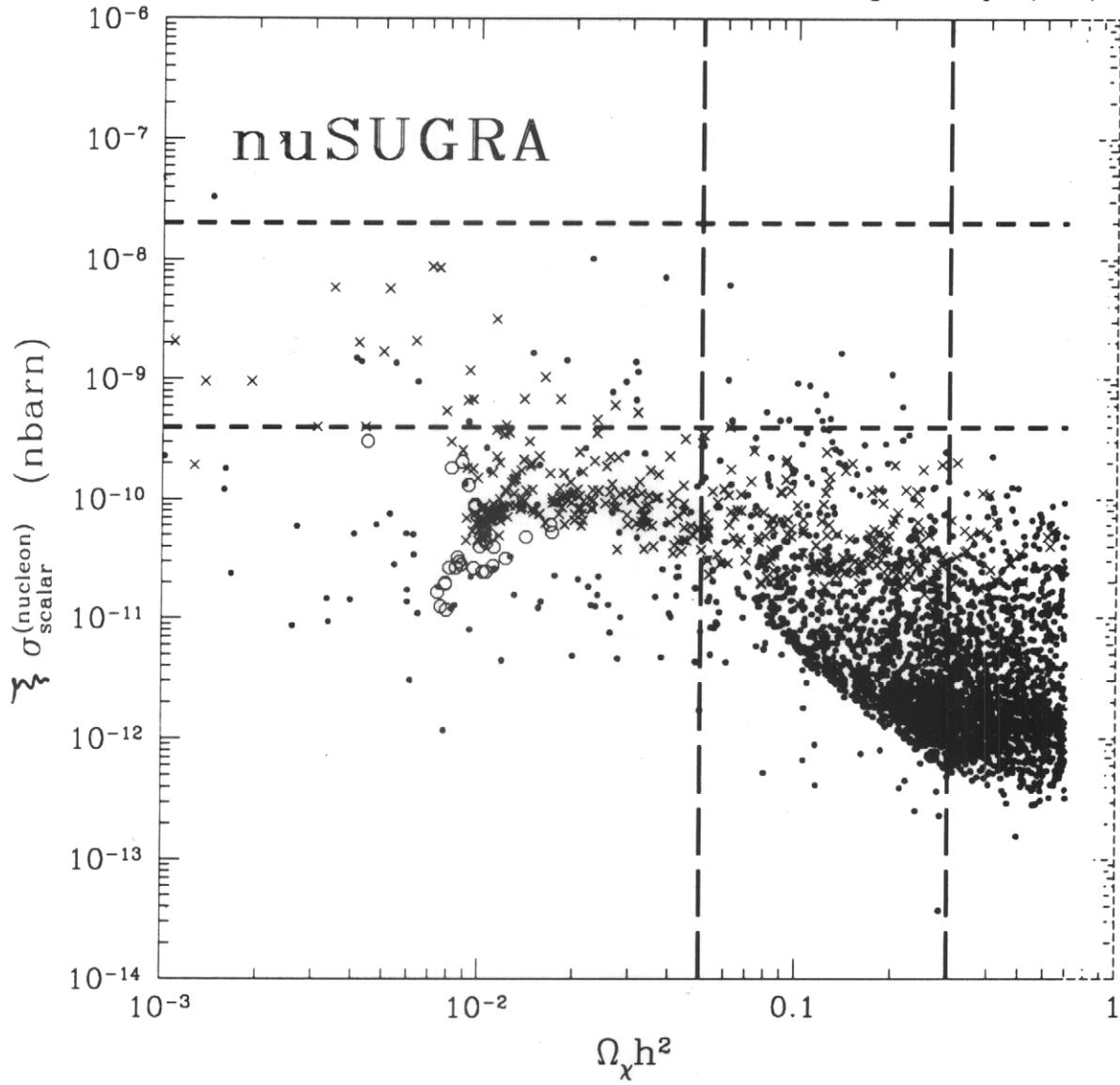
hep-ph/0010203, to appear in Phys. Rev. D



- Gaugino configurations
- × Mixed configurations
- Higgsino configurations



• Gaugino configurations



- Gaugino configurations
- × Mixed configurations
- Higgsino configurations

Once  $\rho_\chi \sigma_{\text{scalar}}^{(\text{nucleon})}$  is measured, we can evaluate

$\rho_\chi$  as

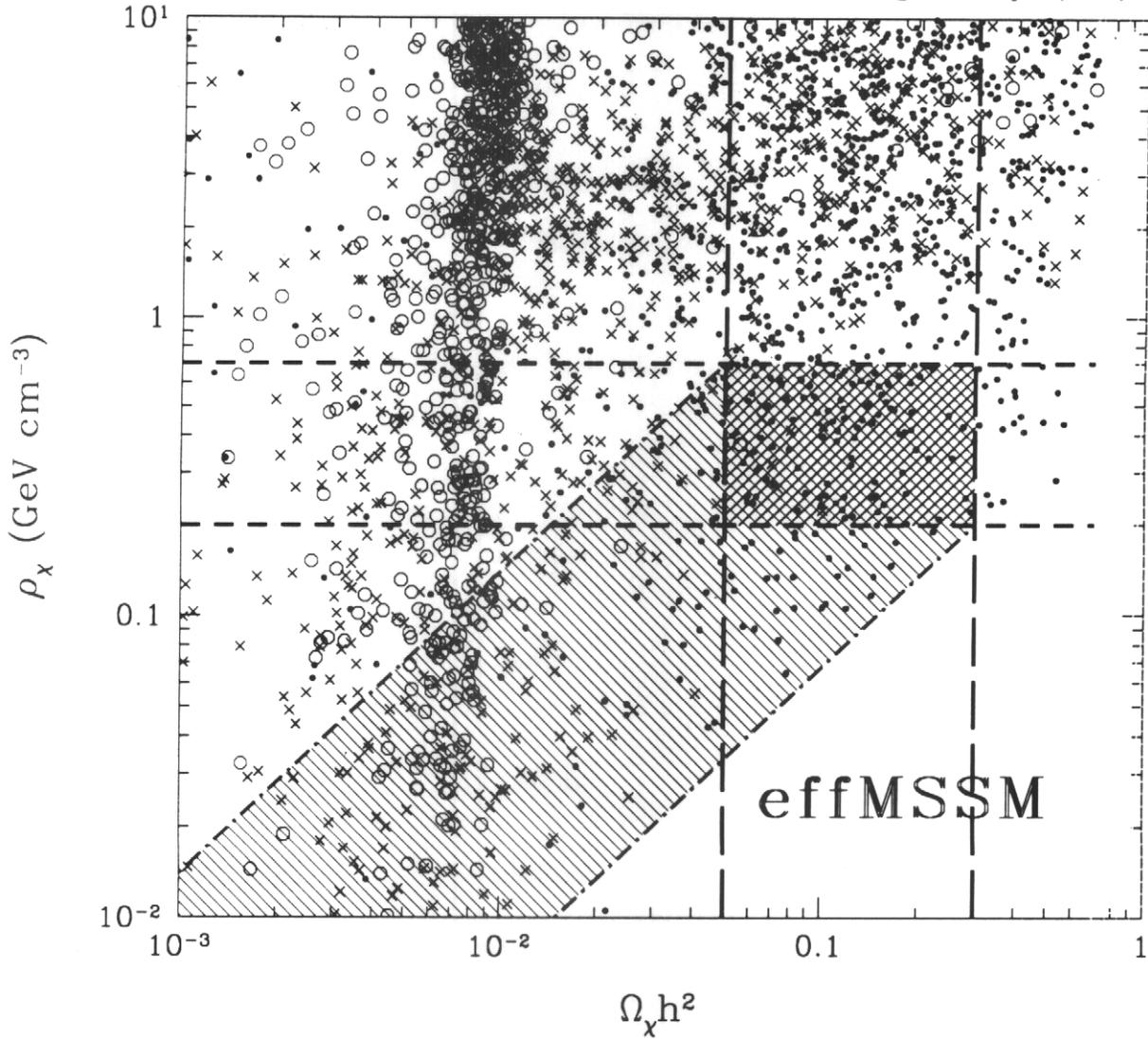
$$\rho_\chi = \frac{[\rho_\chi \sigma_{\text{scalar}}^{(\text{nucleon})}]_{\text{expt}}}{\sigma_{\text{scalar}}^{(\text{nucleon})}}$$

← calculated  
in Susy

and then give a

$\rho_\chi$  vs  $\Omega_\chi h^2$  scatter plot

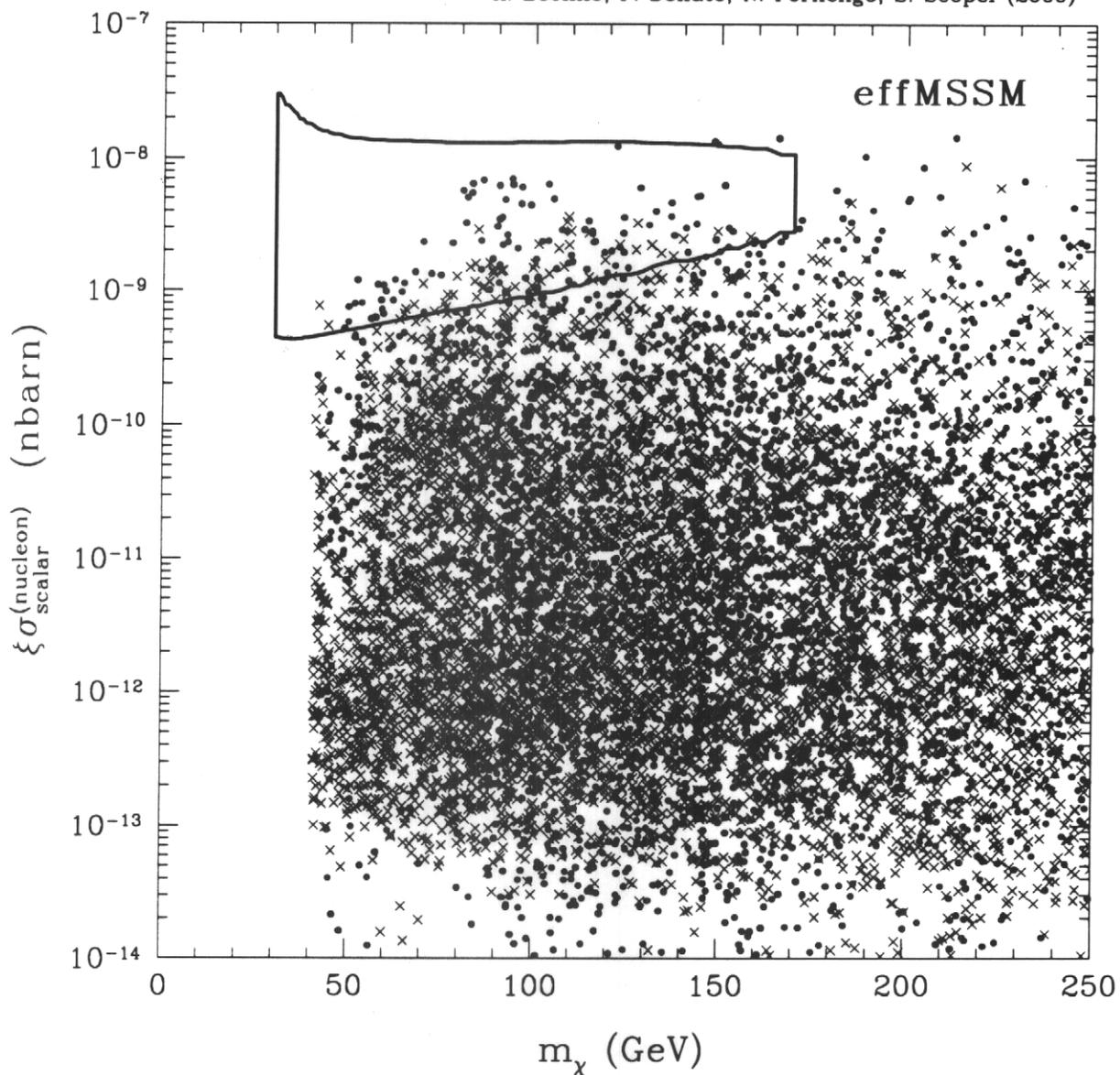
where galactic and average cosmological properties for relic neutralinos are displayed.



$$[\rho_\chi / (0.3 \text{ GeV cm}^{-3}) \cdot \sigma_{\text{scalar}}^{(\text{nucleon})}]_{\text{exp}} = 1 \cdot 10^{-9} \text{ nbarn}$$

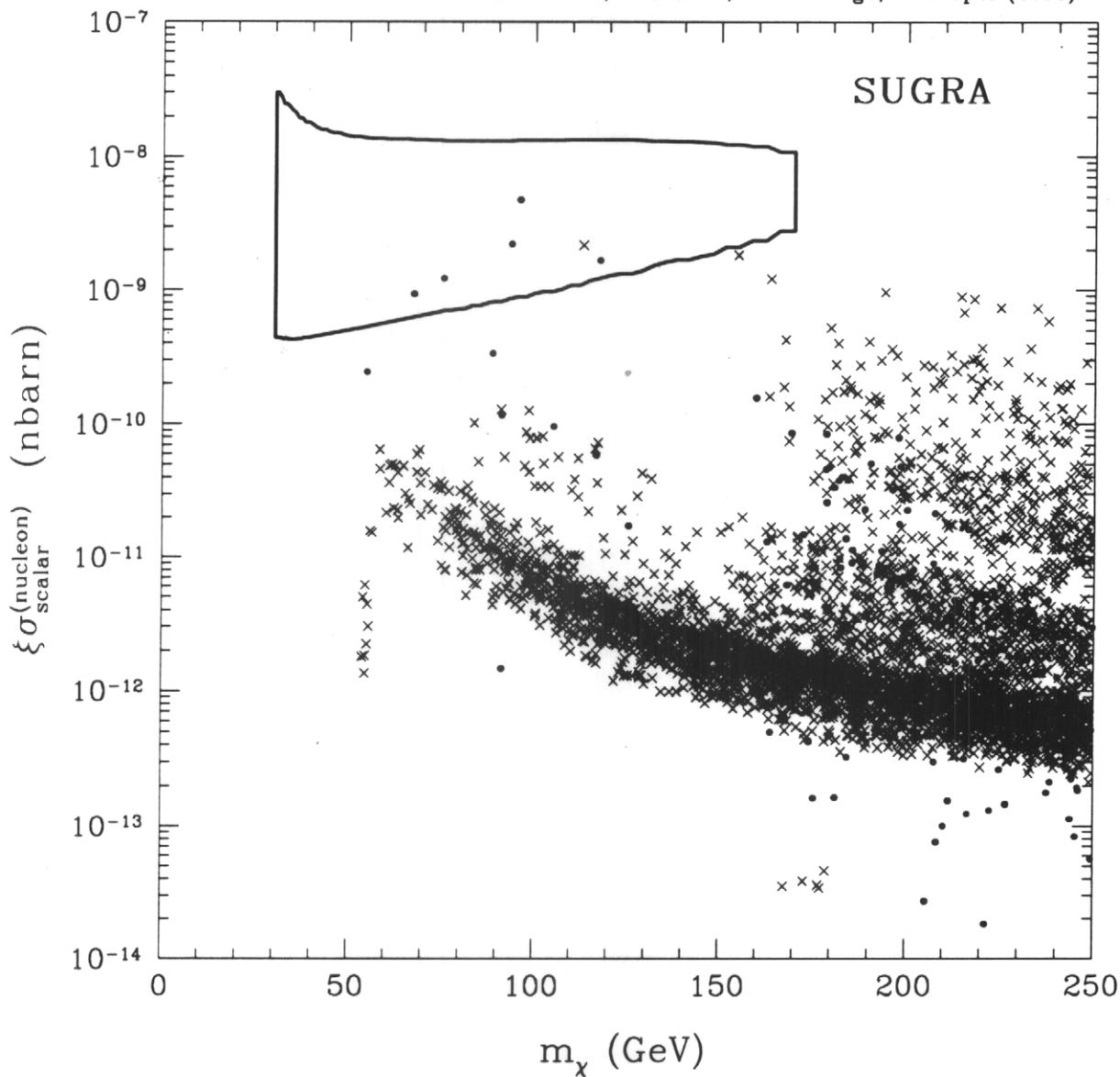
$$40 \text{ GeV} \leq m_\chi \leq 200 \text{ GeV}$$

- Gaugino configurations
- × Mixed configurations
- Higgsino configurations



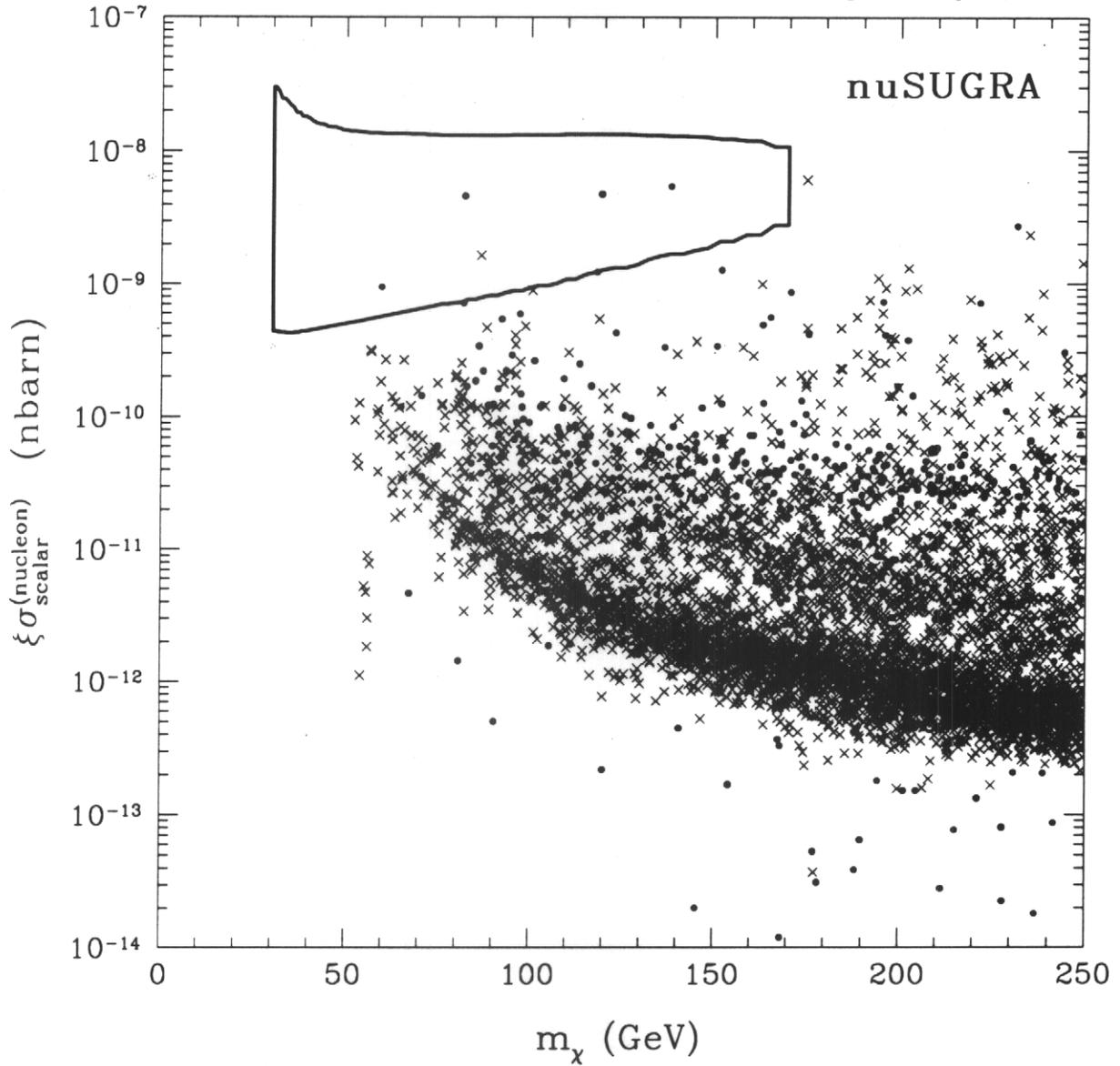
- ×  $\Omega_\chi h^2 \geq 0.05$
- $\Omega_\chi h^2 < 0.05$

The solid contour denotes the DAMA 3  $\sigma$  annual modulation region



- $\times \Omega_\chi h^2 \geq 0.05$
- $\bullet \Omega_\chi h^2 < 0.05$

The solid contour denotes the DAMA  $3\sigma$  annual modulation region



- $\times \Omega_\chi h^2 \geq 0.05$
- $\bullet \Omega_\chi h^2 < 0.05$

The solid contour denotes the DAMA  $3\sigma$  annual modulation region

## Conclusions

- ▷ WIMP direct searches are probing quite significant regions of the supersymmetric parameter space, well beyond those explored by accelerators
- ▷ Part of the relevant susy configurations entail local and average densities of relic neutralinos of cosmological interest
- ▷ A fortiori, present WIMP direct detection experiments are sensitive to relic neutralinos with sub-dominant local and average densities
- ▷ DAMA annual modulation effect is compatible with relic neutralinos as dominant (or sub-dominant) CDM candidates
- ▷ Indirect WIMP searches may add further information on the relevant susy configurations